# Prompt electromagnetic emission of binary black hole mergers

Giuseppe Lodato - Universita' degli Studi di Milano Davide Gerosa - University of Cambridge Marco Tazzari - ESO



- Part 1: Likelihood of fast recoils after a BH binary mergers
  - Importance of including non-linear warp dynamics to estimate alignment timescale
  - Lodato and Gerosa, MNRAS, 429, L30 (2013)
- Part 2: Estimating the fossil circumprimary disc mass at decoupling
  - Importance of correctly implementing the tidal torque in 1D models
  - Tazzari and Lodato, in preparation

#### Part 1: Spin evolution in gaseous environments Lodato & Gerosa (2013)

- Bogdanovic, Reynolds and Miller (2007): in gas rich mergers, the two BH spin likely end up aligned (alignment time much shorter than merger time t<sub>merge</sub>~10<sup>7</sup> yrs; Dotti et al 2009, Escala et al 2005) due to the Bardeen-Petterson effect.
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- Perego et al. (2009): more detailed investigation  $t_{\rm align}$   $\sim$

$$\sim 10^6 \left(\frac{\dot{M}}{\dot{M}_{\rm Edd}}\right)^{-1} {\rm yrs}$$

• Key role is played by the diffusion coefficient of the warp  $\alpha_2$ 

$$t_{\rm align} \simeq 7 \times 10^6 \left(\frac{a}{\alpha_2}\right)^{2/3} \left(\frac{\alpha}{0.1}\right) \left(\frac{H/R}{0.01}\right)^{2/3} \left(\frac{\dot{M}}{0.1\dot{M}_{\rm Edd}}\right)^{-1} \left(\frac{\epsilon}{0.1}\right) {\rm yr}$$

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- Several theories have been developed for warp propagation in discs
- Papaloizou and Pringle (1983) estimate α<sub>2</sub> ~1/2α, for small warps and small viscosity
- Ogilvie (1999) provides a fully non-linear theory of warp propagation
  - For large warps, the warp diffusion coefficient is severely reduced (longer diffusion time-scale)
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## Our approach

- As in previous works, only study the alignment of a single BH with its own disc
- Assume that the disc inclination varies on the scale R (no sharp warp):  $\psi pprox heta$ 
  - A more complete analysis would require a self-consistent calculation of the disc shape
- For low viscosities, the disc may break (Nixon et al, Lodato and Price, Larwood and Papaloizou): assume no alignment in this case
- All above assumptions tend to **favour alignment** (very optimistic)
- Now, alignment time does depend on the initial misalignment  $\theta$

#### Results for constant Eddington ratio

- Perform Monte Carlo simulation varying the initial misalignment
- Given a (viscosity parameter), a (spin parameter) and  $f_{\rm Edd}=\dot{M}/\dot{M}_{\rm Edd}$  we compute the alignment time



- Here assume *f<sub>Edd</sub>*=0.1, *a*=1
- Perego et al: *t<sub>align</sub>*~10 Myr
- When dependence on misalignment in included, the timescale becomes longer by up to an order of magnitude
- Alignment would seem unlikely in this case for a large fraction (~50%) of the cases

## Varying the Eddington ratio

• Here we also Monte Carlo over the Eddington ratio f<sub>Edd</sub> in [10<sup>-4</sup>,1]



- In the fully non-linear case, much weaker dependence on  $\boldsymbol{\alpha}$
- Highly spinning black holes highly unlikely to align within a merger time
- If a > 0.4, BH keep misalignment in more than 40% of the times

#### Conclusions: Part 1

#### Spin alignment of binary black holes

- Earlier claims that gaseous discs are extremely effective in aligning the spins are not confirmed
- Taking into account non-linearity in warp propagation leads to alignment times comparable to merger times, especially for rapidly spinning black holes
- In order to avoid strong recoils, the BH must have a spin parameter a < 0.4
- Note: aligning effect of binary torques (Miller & Krolik 2013) only efficient at small binary separations (<< 0.01 pc)</li>
- To do list
  - Simple approximation for disc shape, needs to be computed consistently
  - Dependence of merger time on system parameters

## Part 2: Estimating the fossil disc mass

Tazzari & Lodato (2014)

- Armitage and Natarajan (2002): Large flare when circumprimary disc is accreted much faster than its own viscous time during GW driven merger
- Chang et al (2010): Fossil disc mass is very small (< 1M<sub>Jupiter</sub>), so very small flare expected
- Both Armitage and Natarajan (2002) and Lodato et al (2009) estimate much larger masses at decoupling
- Origin of the discrepancy?
- Re-do step by step and using exactly identical conditions of Chang et al
  - 1D evolution, using a simple diffusion equation for the disc density + tidal torques

#### Results

- Example evolution for  $M_p = 10^7 M_{Sun}$ , q = 0.1
- Inner disc mass discrepant by a factor ~ 1000 !
- Large exploration of parameter space: while Chang et al always predict sub-Eddington flares, we estimate flare luminosities  $1 < L/L_{Edd} < 30$



- Chang et al use an incorrect torque approximation in their 1D code
- Allow the torque to be significant also at distances from the secondary much larger than the outermost Lindblad resonance ---> too large gap sizes
- In our approach, we truncate the torque in such a way to recover the correct gap size as estimated numerically by Artymowicz and Lubow (1994).



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- It can be shown analytically that the fossil disc mass scales with the outer edge of the inner disc as R<sub>edge<sup>7/2</sup></sub>, fully explaining the discrepancy
- **Big caveat**: these simulations neglect completely any mass flow through the gap!
  - Artymowicz and Lubow (1994): reduction in mass flux by a factor 10
  - D'Orazio et al (2013) strong dependence on mass ratio.
  - Need to explore mass flow though gaps as a function of H/R

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## Conclusions: Part 2

#### Fossil disc mass

- Earlier claims that fossil discs have very small masses (below 1 M<sub>Jupiter</sub>) are not confirmed
- Care should be taken in computing the tidal torque for non extreme mass ratios, in order to compute gap sizes accurately
- Accretion of fossil disc leads to strongly super-Eddington flares during GW driven evolution
- To do list
  - Consider mass flow through the gap (possibly already in 1D codes)
  - Evaluate mass flow as a function of *H*/*R*
  - Is the whole fossil disc accreted during GW phase (Baruteaou et al. 2012)?