

# Structure Formation with Scalar Field Dark Matter

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Tonatiuh Matos

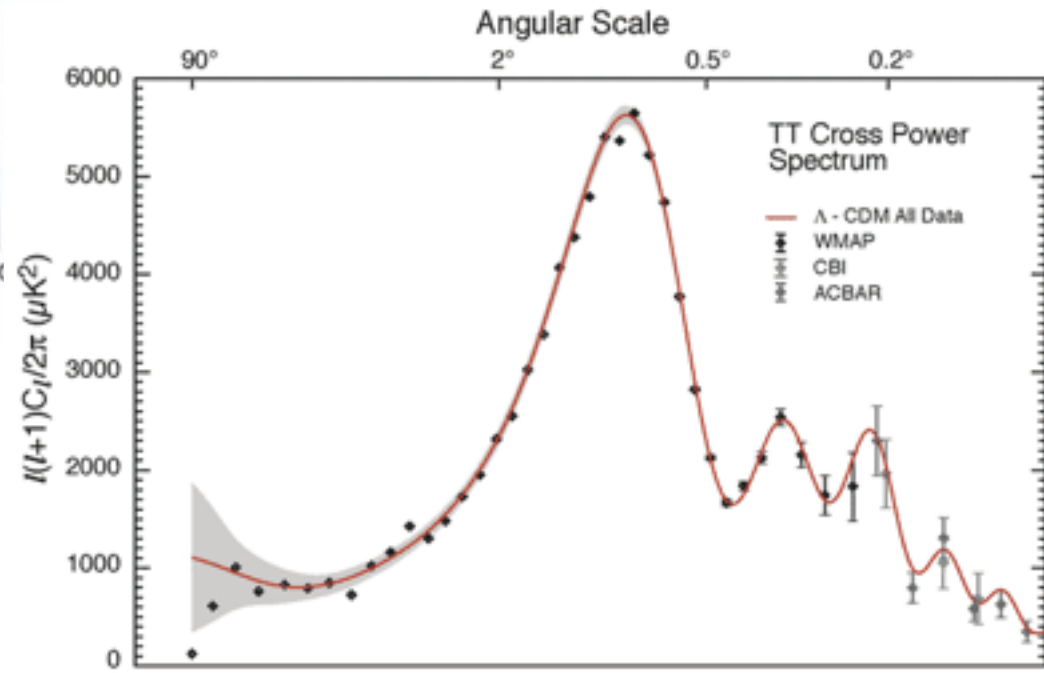
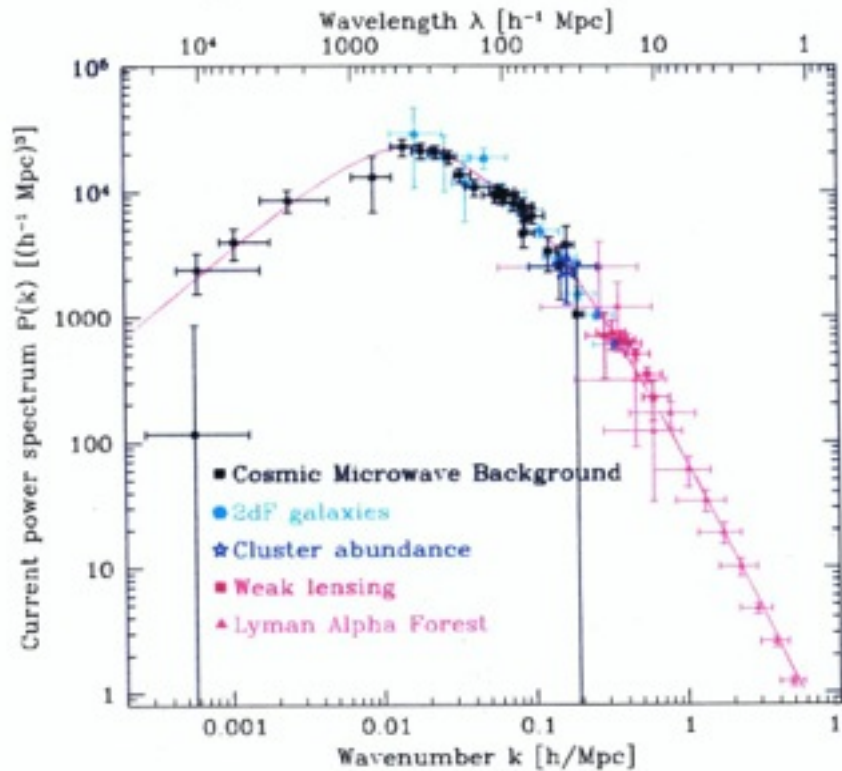
<http://www.fis.cinvestav.mx/~tmatos/>

<http://www.iac.edu.mx>

Some Problems of the LCDM

SFDM

# The Standard Model of Cosmology: LCDM



# The Standard Model of Cosmology: Problems

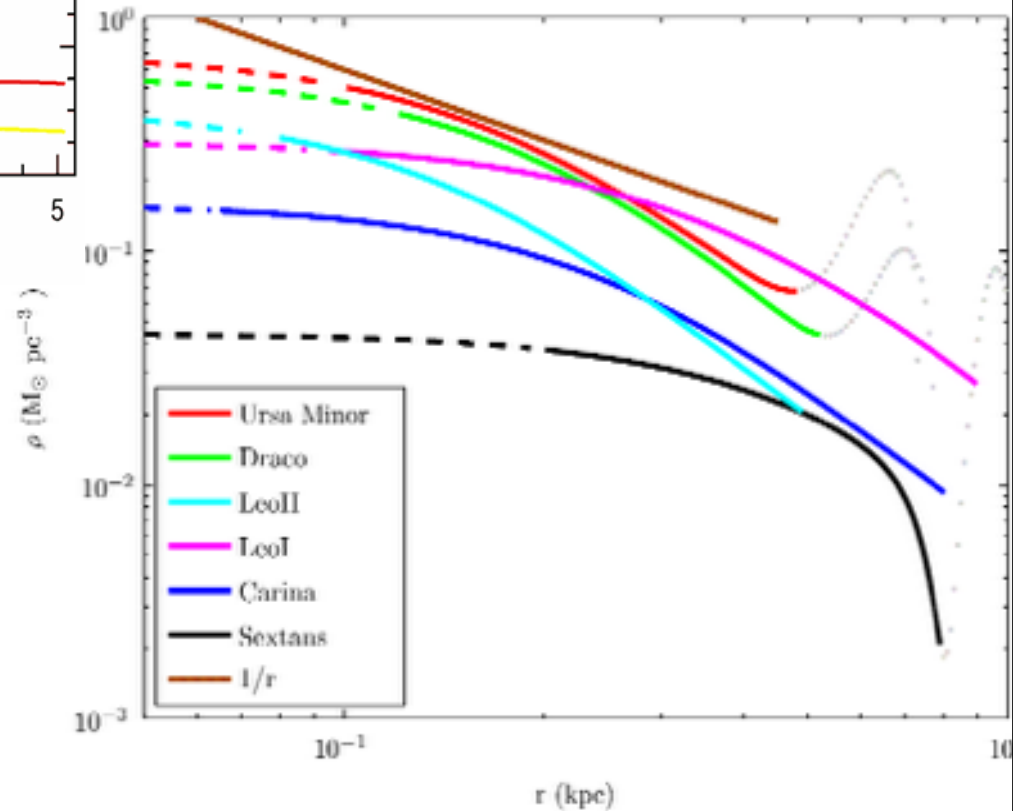
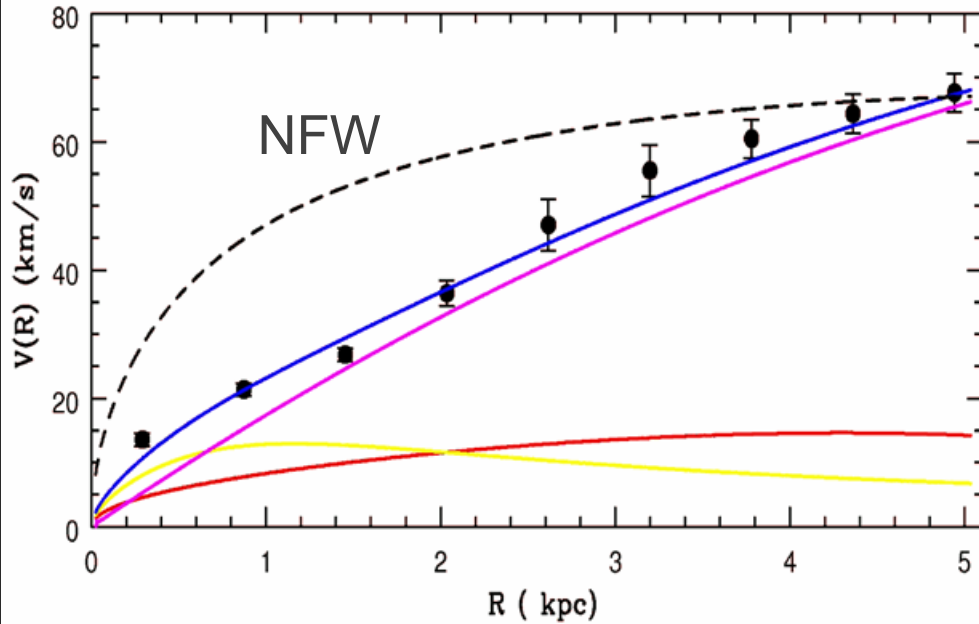
- Extreme fine tuning
- Coincidence
- Cuspy central density profiles
- Missing Satellites Problem
- Satellites stability
- Too big to fail
- No-detection of DM
- etc.

# The Standard Model of Cosmology: Problems

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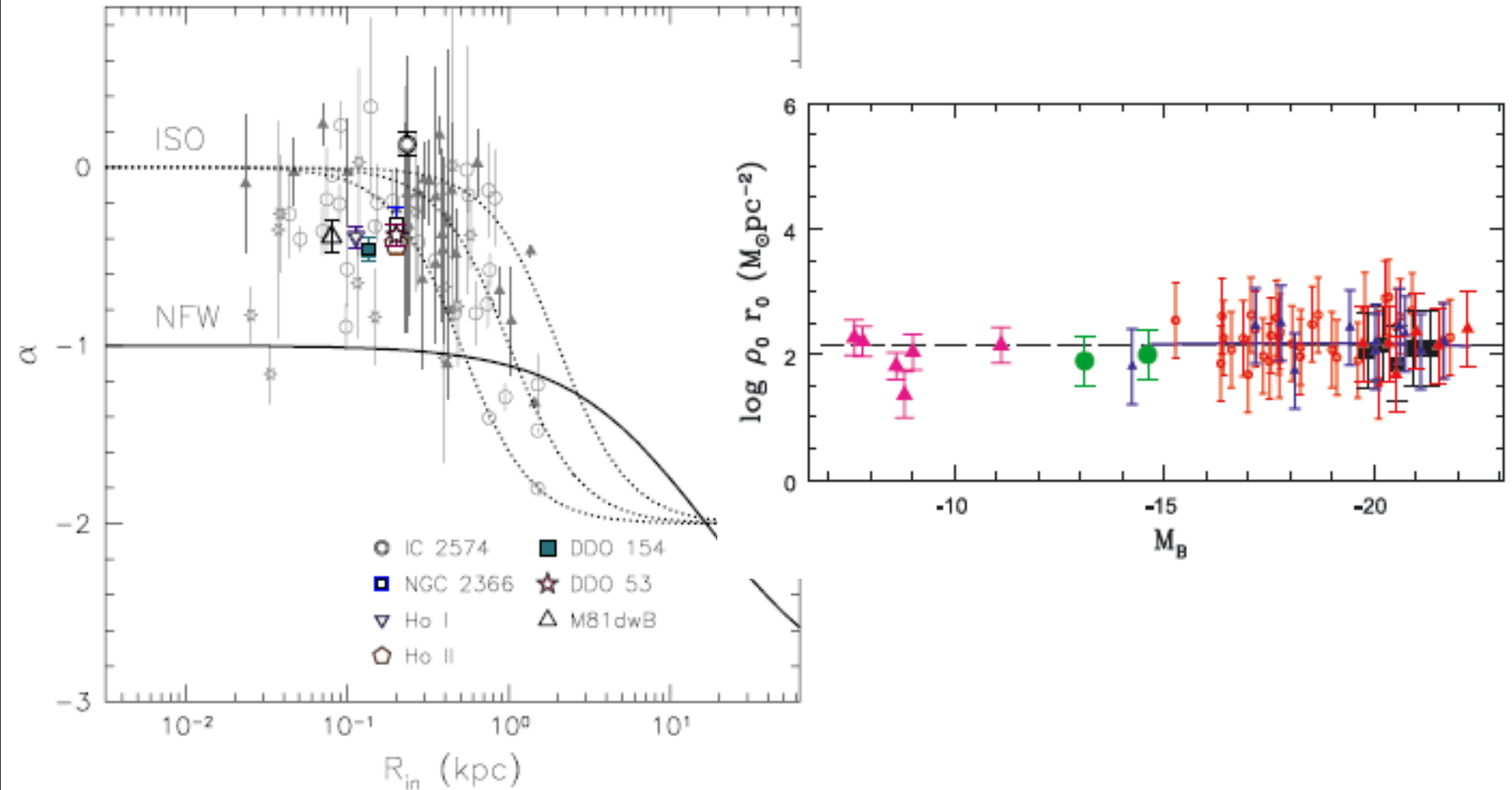
- Cuspy central density profiles
- Missing Satellites Problem
- Satellites stability

# Galaxy's Center: Observations



# Galaxy's Center: Observations

Gentile G., Tonini C. and Salucci P., A&A, 467, 925-931 (2007).



# Galaxy's Center: Simulations

F. Governato, et. al., NATURE, Vol 463, 14 January 2010

## THE FORMATION OF A BULGELESS GALAXY WITH A SHALLOW DARK MATTER CORE

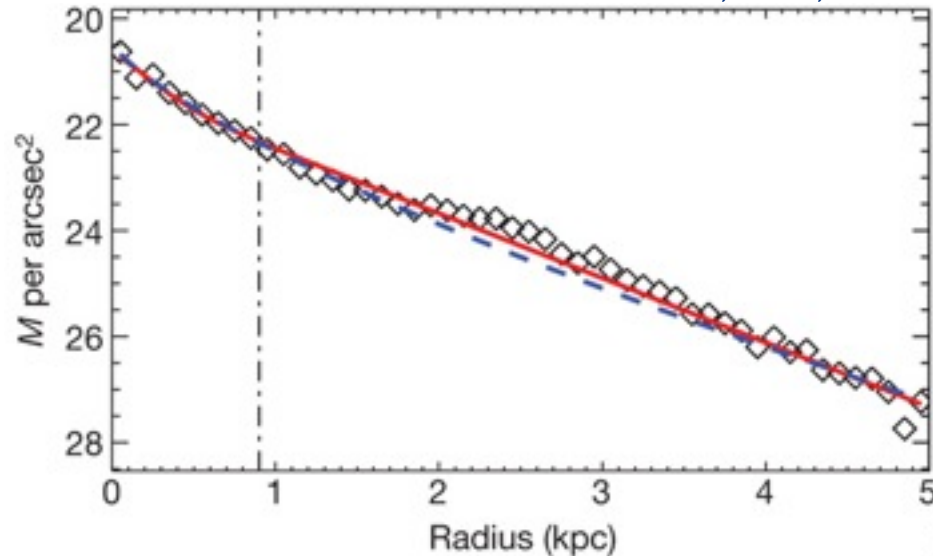
**Fabio Governato** (University of Washington)  
**Chris Brook** (University of Central Lancashire)  
**Lucio Mayer** (ETH and University of Zurich)  
and the N-Body Shop

KEY: Blue: gas density map. The brighter regions represent gas that is actively forming stars. The clock shows the time from the Big Bang. The frame is 50,000 light years across.

Simulations were run on Columbia (NASA Advanced Supercomputing Center) and at ARSC

# Galaxy's Center: Simulations

F. Governato, et. al., NATURE, Vol 463, 14 January 2010

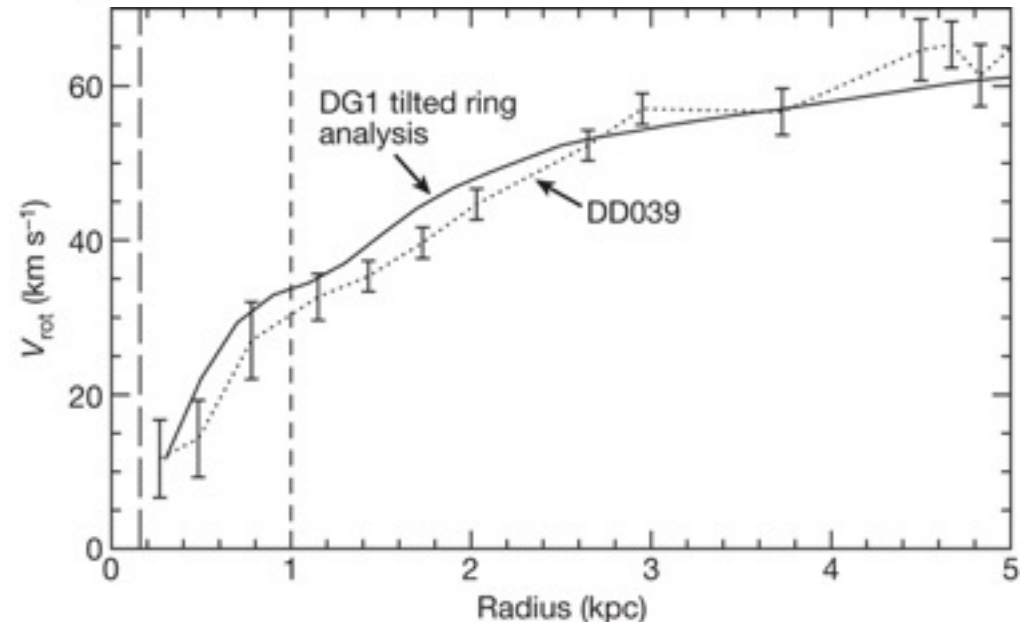


Einasto profile

$$\rho = \rho_0 e^{-A r^\alpha}$$

No evidence for internal features or star formation that could be the result of tidal processes or star formation induced by the cluster environment.

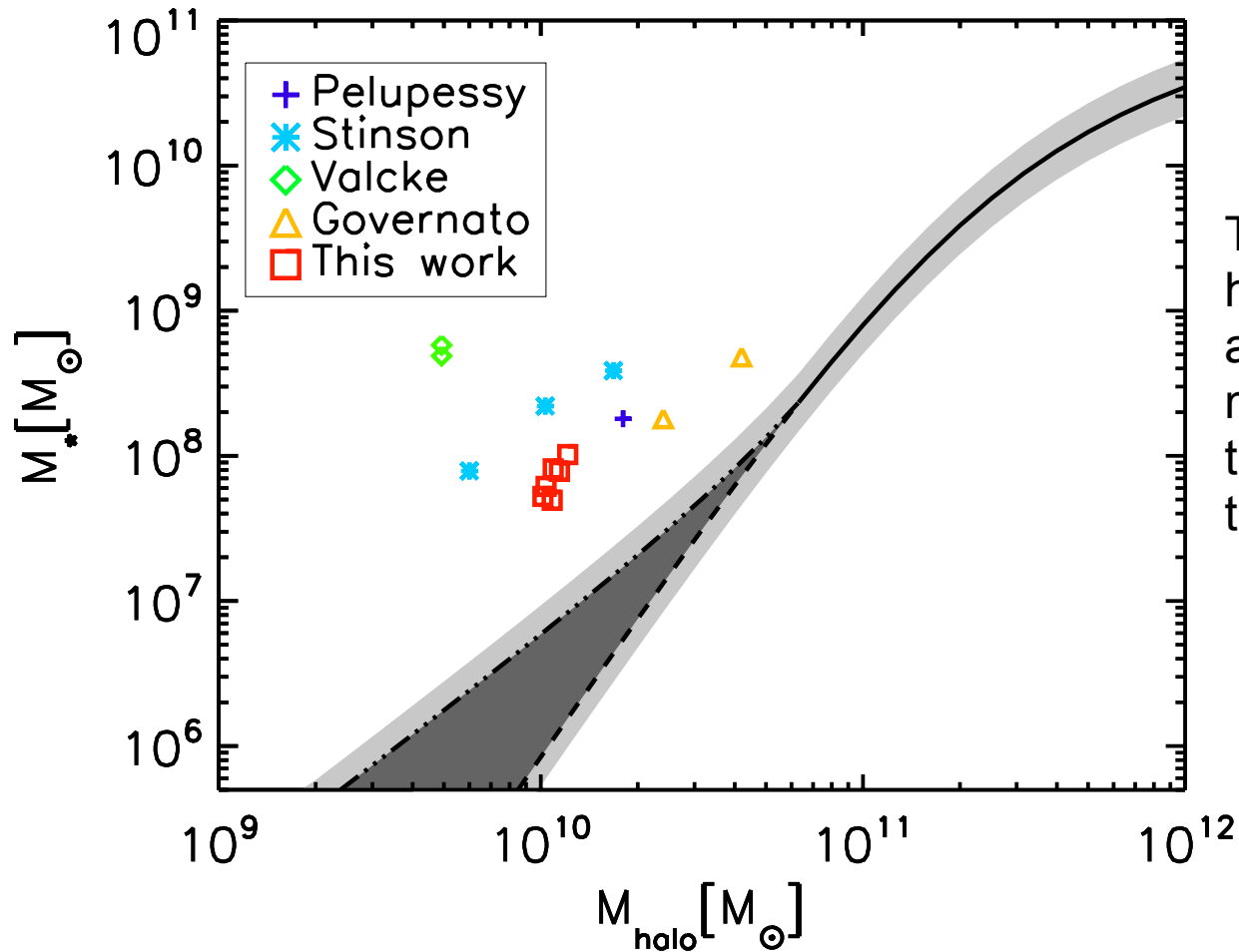
ej: Samantha J. Penny, Christopher J. Conselice, Sven De Rijcke and Enrico V. Held:  
Mon. Not. R. Astron. Soc. 393, 1054–1062 (2009), etc.





# Stellar Mass Predictions

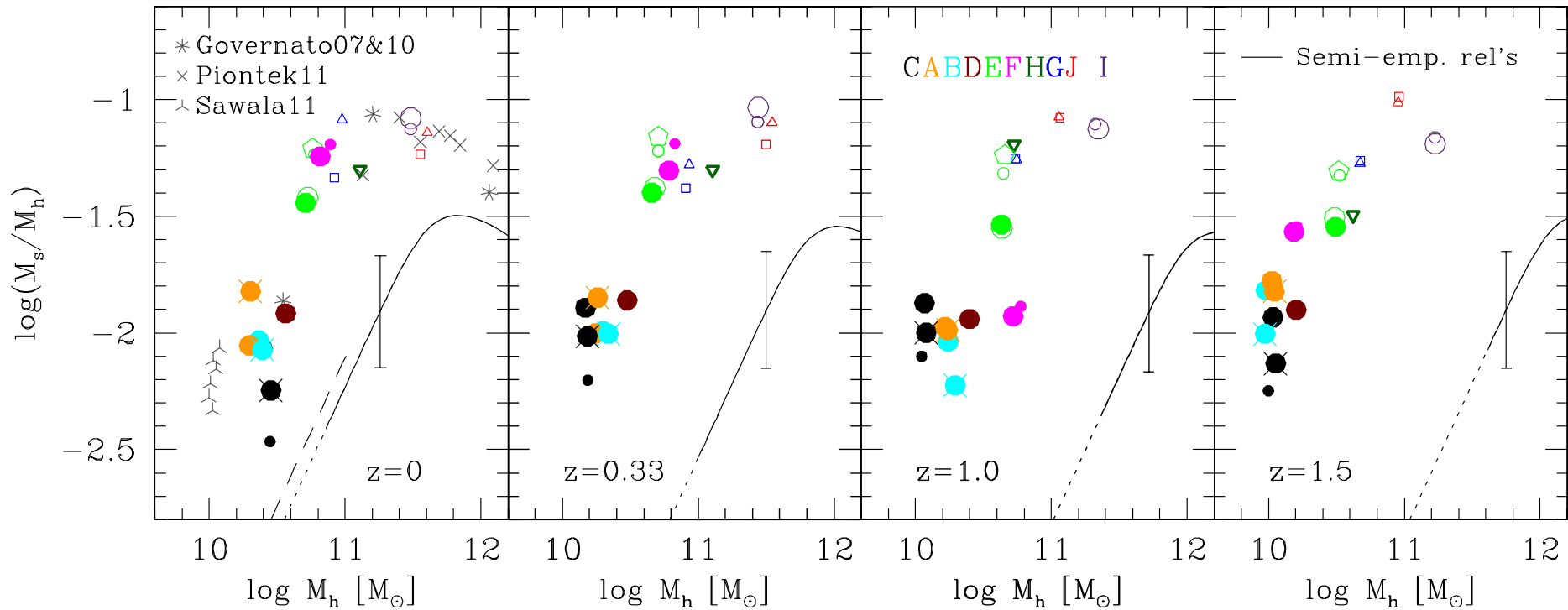
Till Sawala, Qi Guo, Cecilia Scannapieco, Adrian Jenkins and Simon White. *Mon. Not. Roy. Astron. Soc.* 413, (2011), 659



The dwarf galaxies formed in hydrodynamical simulations are almost two orders of magnitude more luminous than expected for haloes of this mass.

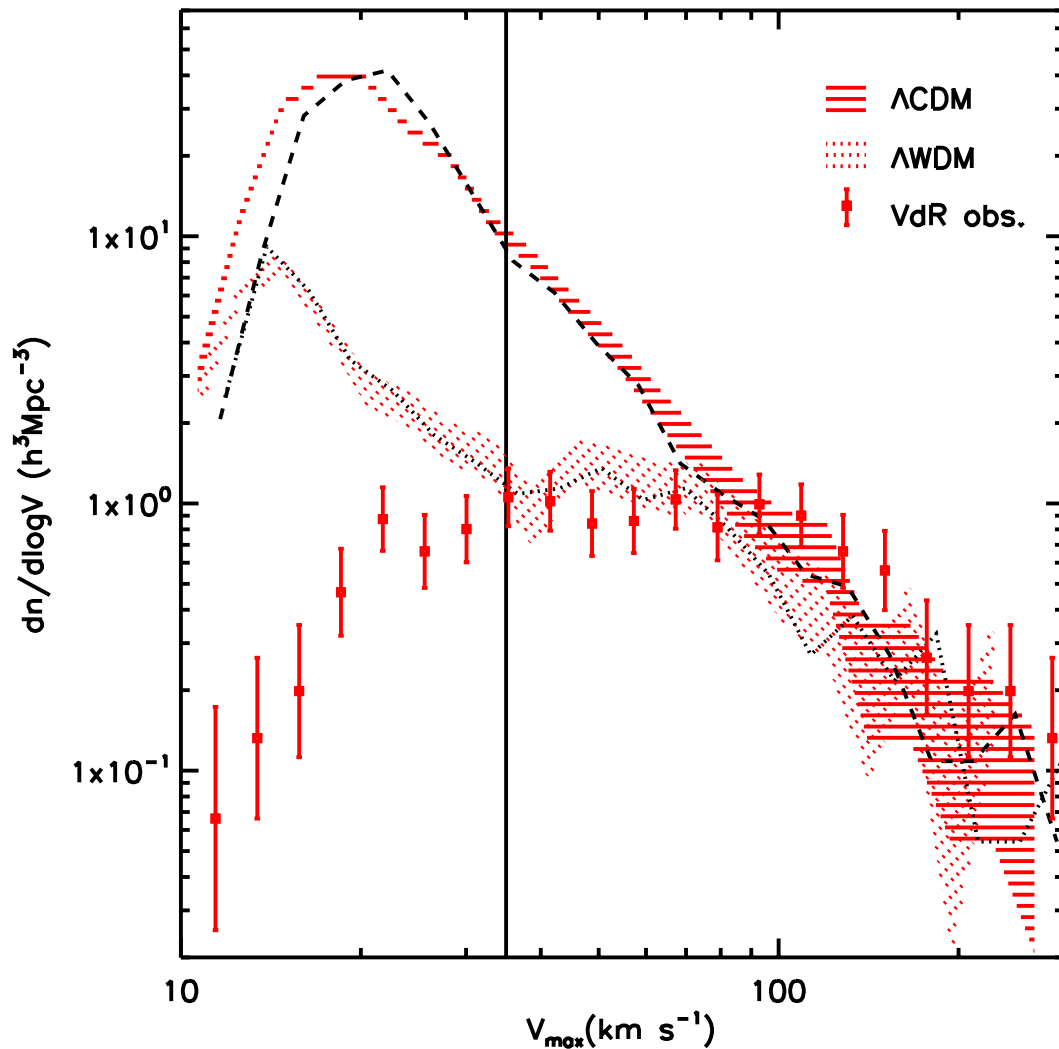
# Stellar Mass Predictions

V. Avila-Reese, P. Colín, A. González-Samaniego, O. Valenzuela, C. Firmani, H. Velázquez, & D. Ceverino. The ApJ, 736:134, (2011)



# Velocity predictions

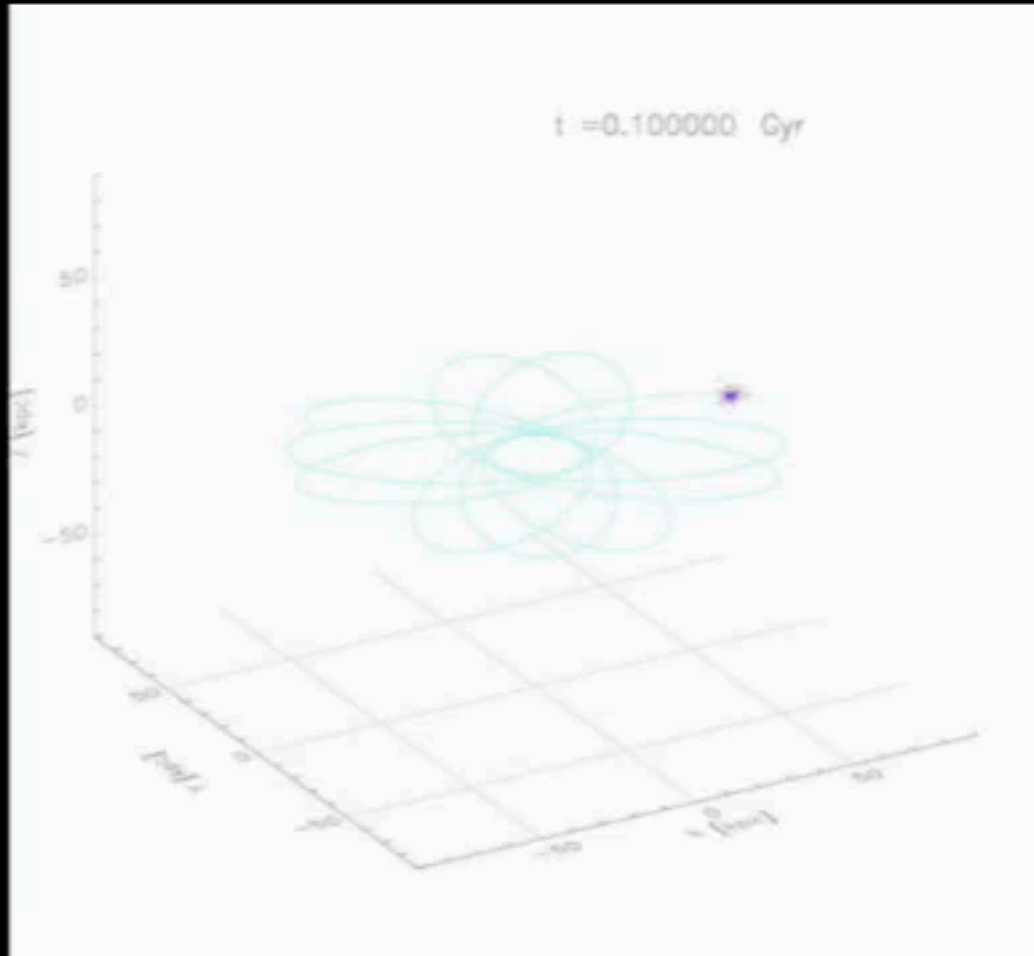
Jesús Zavala, et. al. ApJ, 700:1779–1793, 2009 August 1

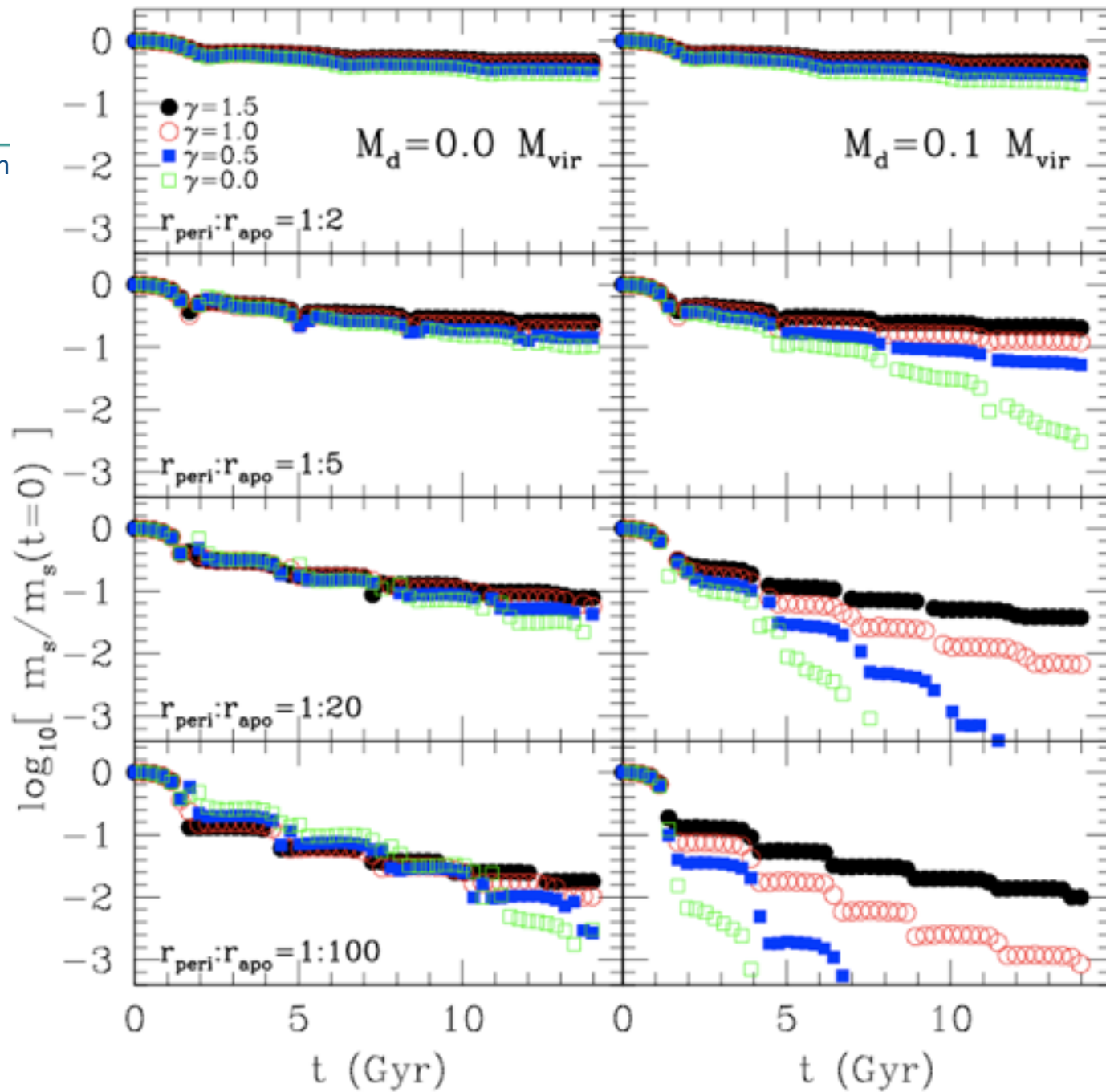


The simulation with CDM predicts a steep rise in the VF toward lower velocities; for  $V_{\text{max}} = 35 \text{ km/s}$ , it forecasts  $\sim 10$  times more sources than the ones observed. If confirmed by the complete ALFALFA survey, these results indicate a potential problem for the CDM paradigm

# Galactic Dynamics

J. Peñarrubia, A. J. Benson, M. G. Walker, G. Gilmore, A. W. McConnachie & L. Mayer. MNRAS 406(2010)1290





T. Matos and L. Ureña, Class. Q. Grav. 17(2000)L75

- Dark Matter:  $\rightarrow \frac{1}{2}m^2\Phi^2 + \frac{1}{4}\lambda\Phi^4$
- Dark Energy:  $\rightarrow \Lambda$
  
- Baryons, Radiation,
- Neutrinos, etc.
  
- $\Omega_\Phi \sim 0.23$
- $\Omega_\Lambda \sim 0.73$
- $\Omega_b \sim 0.04$

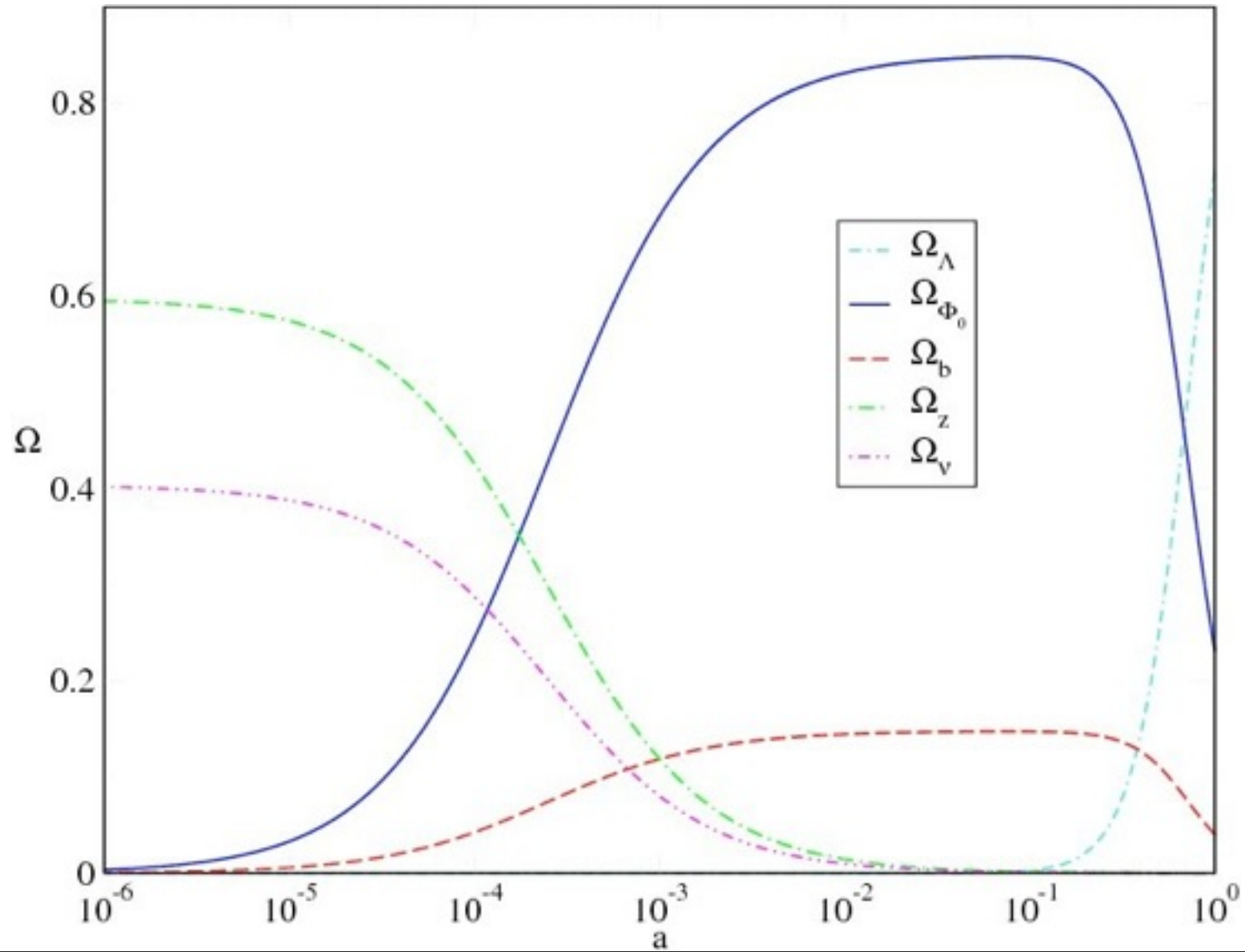
$$\square\Phi + \frac{dV}{d\Phi} = 0$$

$$\ddot{\Phi} + 3H\dot{\Phi} + \frac{dV}{d\Phi} = 0$$

$$k_B T_c = \frac{2\pi\hbar^2}{m^{\frac{5}{3}}} \left( \frac{\rho}{g_{\frac{3}{2}}(1)} \right)^{\frac{2}{3}}$$

# The Cosmology

$\Phi^2$  as Dark Matter. T. Matos, A. Vázquez & J.A. Magaña. *MNRAS*, 389, (2009) 13957.



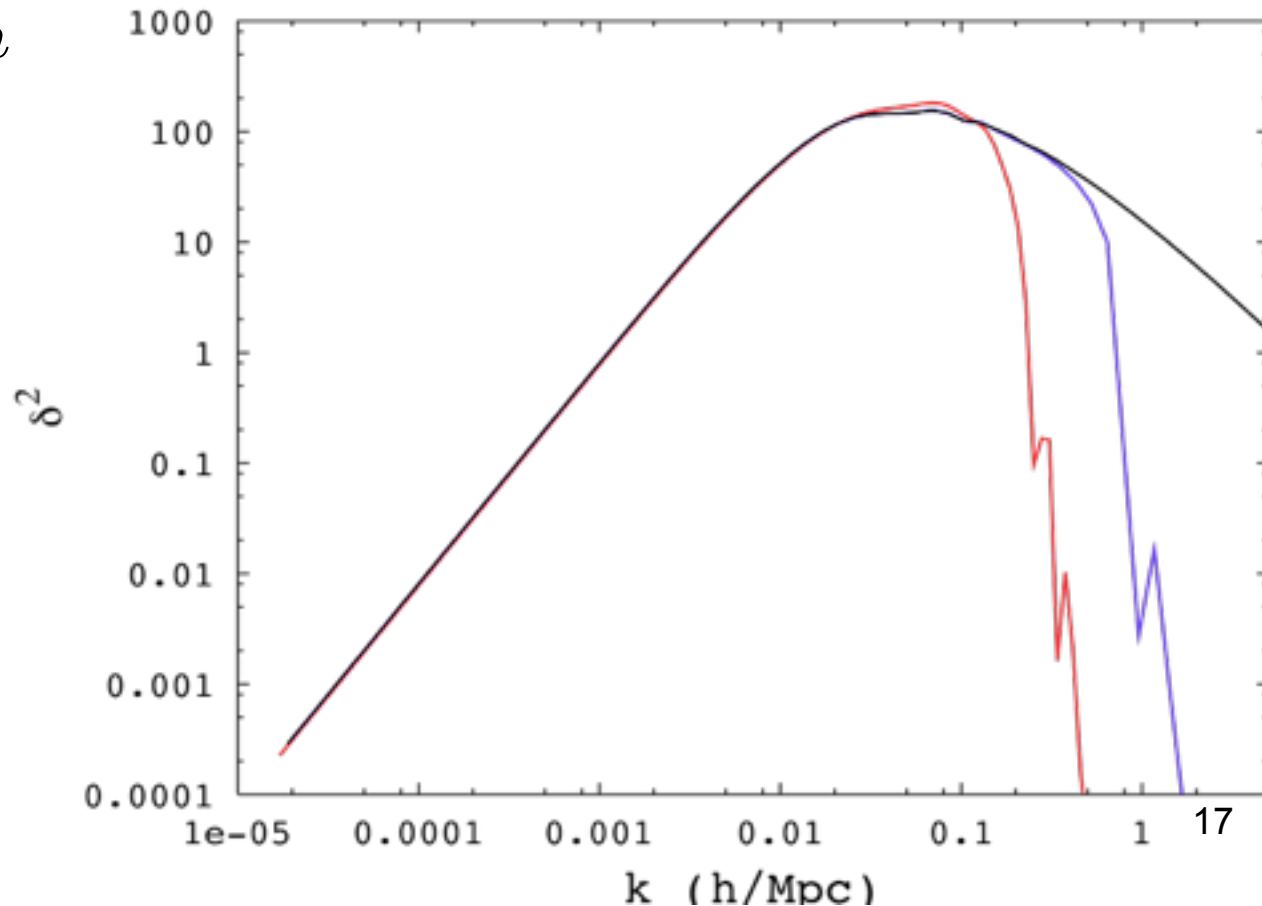


# Natural Cut off

Tonatiuh Matos and Luis A. Ureña. Phys Rev. D63, (2001), 063506. Available at: astro-ph/ 0006024

$$\delta\ddot{\Phi}_k + 3H\delta\dot{\Phi}_k + \left( \frac{k^2}{a^2} + V_{,\Phi\Phi} \right) \delta\Phi_k + 2V_{,\Phi} \phi_k - 4\Phi_0\dot{\phi}_k = 0$$

In  $\Phi_{min}$



$T \ll T_c$

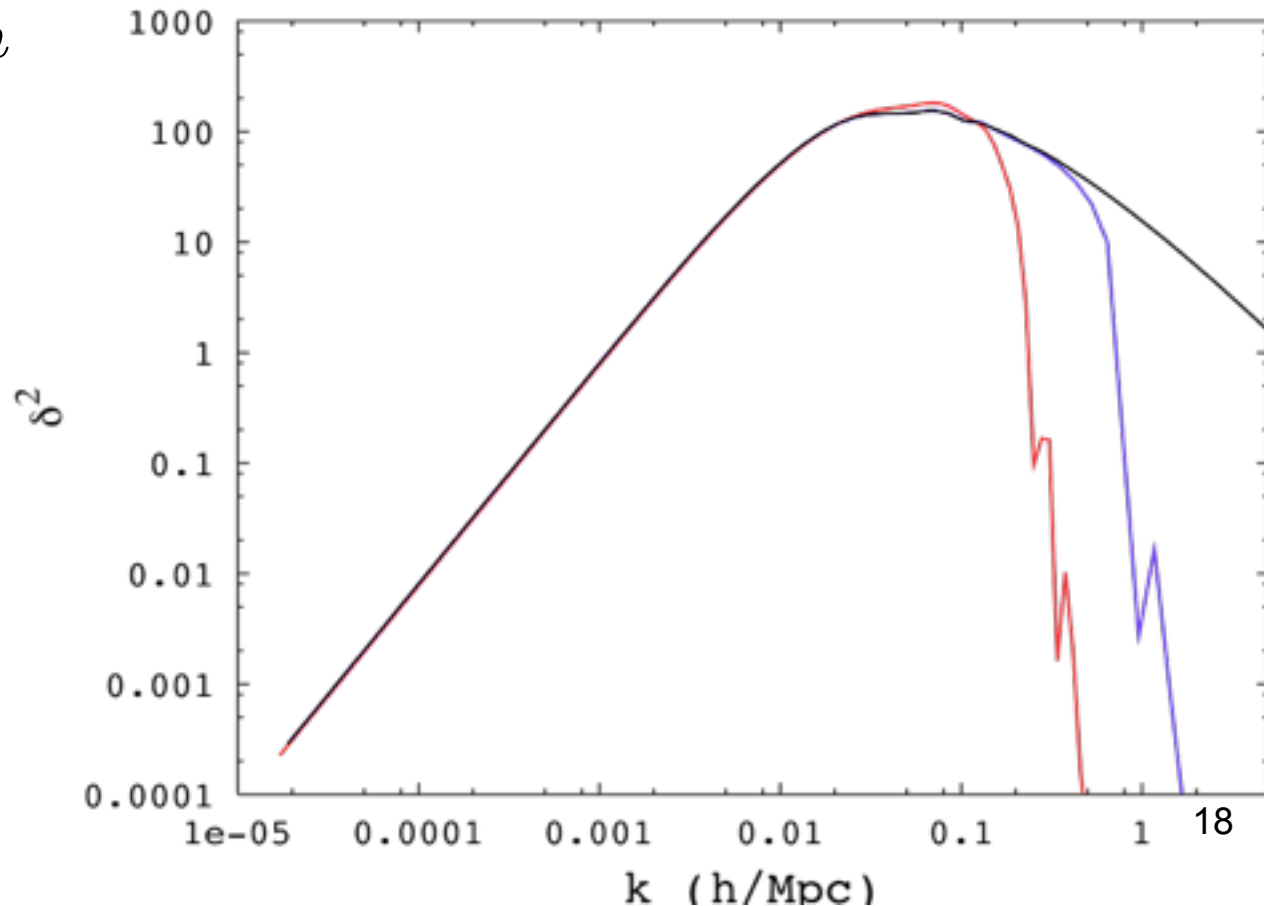
# Natural Cut off

Tonatiuh Matos and Luis A. Ureña. Phys Rev. D63, (2001), 063506. Available at: astro-ph/ 0006024

$$\delta\ddot{\Phi}_k + 3H\delta\dot{\Phi}_k + \left( \frac{k^2}{a^2} - m^2 + \frac{\lambda}{4}T^2 \right) \delta\Phi_k = 4\Phi_0\dot{\phi}_k$$

In  $\Phi_{min}$

$T \ll T_c$



# Structure Formation

Abril Suarez and TM MNRAS 311, (2011), 87

$$\delta\ddot{\Phi} + 3H\delta\dot{\Phi} - \frac{1}{a^2}\nabla^2\delta\Phi + V_{,\Phi\Phi}\delta\Phi + 2V_{,\Phi}\phi = 0$$

$$\delta\Phi = \sqrt{\hat{\rho}} \cos\left(\frac{mc^2 t}{\hbar} + S\right) \quad \vec{v} \equiv \frac{\hbar}{m} \nabla S$$

$$\vec{v} \equiv \frac{\hbar}{m} \nabla S$$

$$\begin{aligned} \frac{\partial \hat{\rho}}{\partial t} &+ \frac{1}{a^2} \nabla \cdot (\hat{\rho} \vec{v}) + 3H \hat{\rho} \\ &- \frac{\hbar}{m} \hat{\rho} (\ddot{S} + 3H \dot{S}) - \frac{\hbar}{m} \hat{\rho} \dot{S} = 0 \\ \frac{\partial \vec{v}}{\partial t} &+ \frac{1}{a^2} \vec{v} \nabla \cdot \vec{v} + \nabla \phi + \frac{\hbar^2}{2m^2} \nabla \left( \frac{\square \sqrt{\hat{\rho}}}{\sqrt{\hat{\rho}}} \right) \\ &- \frac{\hbar}{m} \dot{S} \frac{\partial \vec{v}}{\partial t} = 0, \end{aligned}$$

$$\vec{v} \equiv \frac{\hbar}{m} \nabla S$$

$$\frac{\partial \hat{\rho}}{\partial t} + \frac{1}{a^2} \nabla \cdot (\hat{\rho} \vec{v}) + 3H \hat{\rho} = 0$$

$$\frac{\partial \vec{v}}{\partial t} + \frac{1}{a^2} \vec{v} \nabla \cdot \vec{v} + \nabla \phi + \frac{\hbar^2}{2m^2} \nabla \left( \frac{\square \sqrt{\hat{\rho}}}{\sqrt{\hat{\rho}}} \right) = 0,$$

# Structure Formation

Abril Suarez and TM MNRAS 311, (2011), 87

$$\hat{\rho} = \hat{\rho}(t) \quad S = S(t) \quad \vec{v} \equiv \frac{\hbar}{m} \nabla S$$

$$\frac{\partial \hat{\rho}}{\partial t} + \frac{1}{a^2} \nabla \cdot (\hat{\rho} \vec{v}) + 3H \hat{\rho} = 0$$

$$\frac{\partial \vec{v}}{\partial t} + \frac{1}{a^2} \vec{v} \nabla \cdot \vec{v} + \nabla \phi + \frac{\hbar^2}{2m^2} \nabla \left( \frac{\square \sqrt{\hat{\rho}}}{\sqrt{\hat{\rho}}} \right) = 0,$$

# Structure Formation

Abril Suarez and TM MNRAS 311, (2011), 87

$$\hat{\rho} = \hat{\rho}(t) \quad S = S(t) \quad \vec{v} \equiv \frac{\hbar}{m} \nabla S$$

$$\frac{\partial \hat{\rho}}{\partial t} + 3H \hat{\rho} = 0$$

$$\hat{\rho} \sim \frac{1}{a^3}$$

$$\vec{v} \equiv \frac{\hbar}{m} \nabla S$$

$$\frac{\partial \hat{\rho}}{\partial t} + \frac{1}{a^2} \nabla \cdot (\hat{\rho} \vec{v}) = 0$$

$$\frac{\partial \vec{v}}{\partial t} + \frac{1}{a^2} \vec{v} \nabla \cdot \vec{v} + \nabla \phi + \frac{\hbar^2}{2m^2} \nabla \left( \frac{\square \sqrt{\hat{\rho}}}{\sqrt{\hat{\rho}}} \right) = 0,$$



$$\hat{\rho} = \hat{\rho}_0 + \rho_1(t) \exp(i\vec{k} \cdot \vec{x}/a)$$

$$\vec{v} = \vec{v}_0 + \vec{v}_1(t) \exp(i\vec{k} \cdot \vec{x}/a)$$

$$\phi = \phi_0 + \phi_1(t) \exp(i\vec{k} \cdot \vec{x}/a)$$

$$\vec{v}_1 = \lambda \vec{k} + \vec{v}_2$$

$$\frac{\partial \rho_1}{\partial t} + 3H\rho_1 + i\frac{\hat{\rho}_0}{a^2}k^2\lambda = 0$$

$$\frac{\partial \lambda}{\partial t} + i\left(\frac{v_q^2}{\hat{\rho}_0} - 4\pi G\frac{a^2}{k^2}\right)\rho_1 = 0,$$

$$\delta = \frac{\rho_1}{\hat{\rho}}$$

**SFDM**

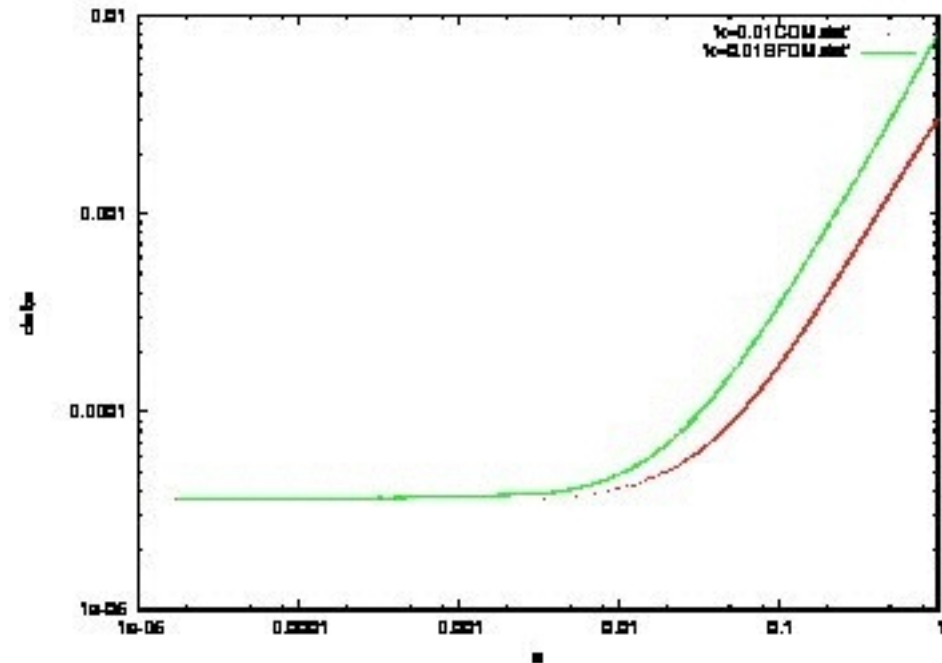
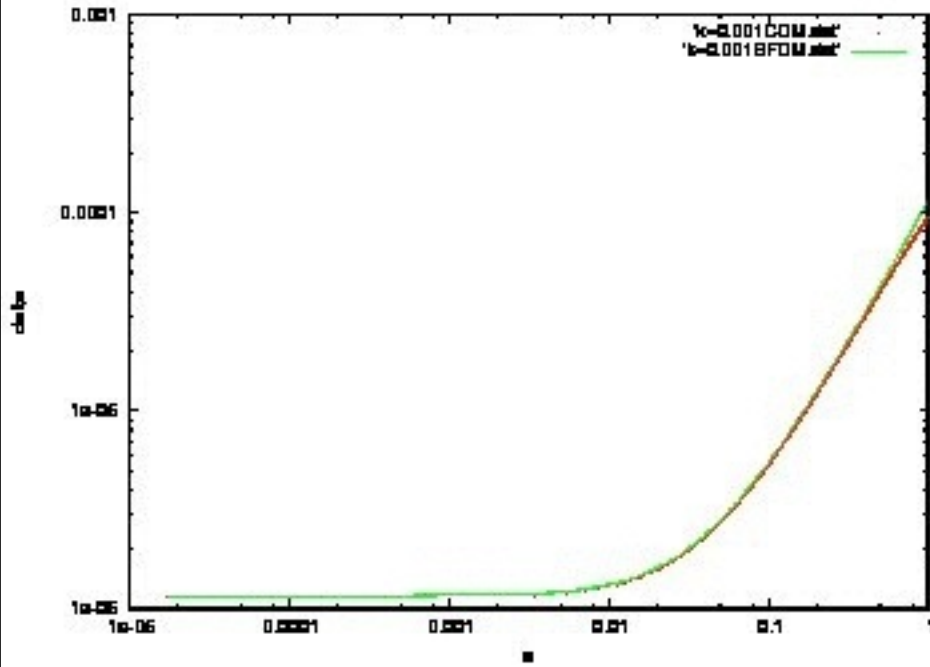
$$\frac{d^2\delta}{dt^2} + 2H\frac{d\delta}{dt} + \left(v_q^2\frac{k^2}{a^2} - 4\pi G\hat{\rho}_0\right)\delta = 0, \quad v_q^2 = \frac{\hbar^2 k^2}{4a^2 m^2}$$

**CDM**

$$\frac{d^2\delta}{dt^2} + 2H\frac{d\delta}{dt} + \left(v_s^2\frac{k^2}{a^2} - 4\pi G\hat{\rho}_0\right)\delta = 0,$$

# Structure Formation

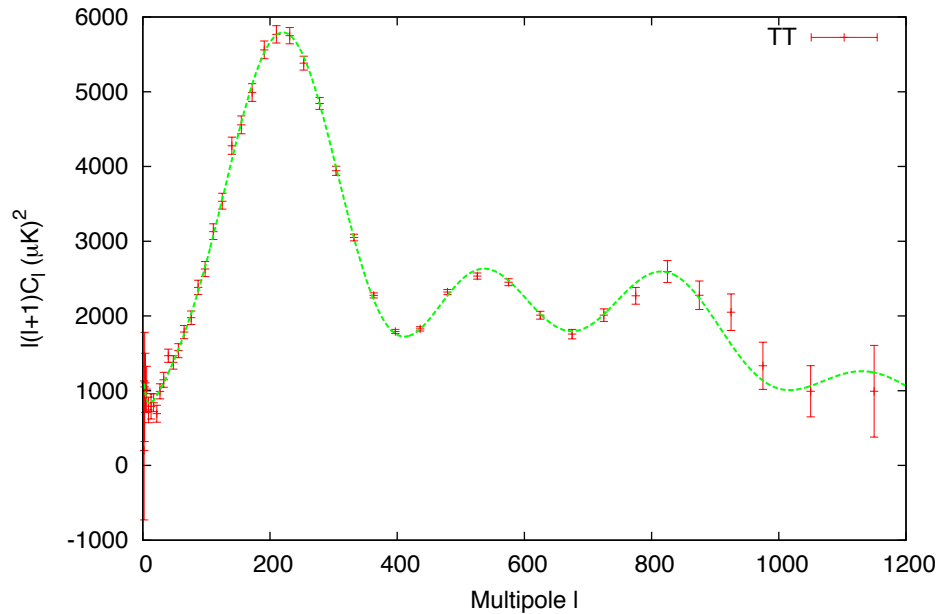
Abril Suarez and TM MNRAS 311, (2011), 87



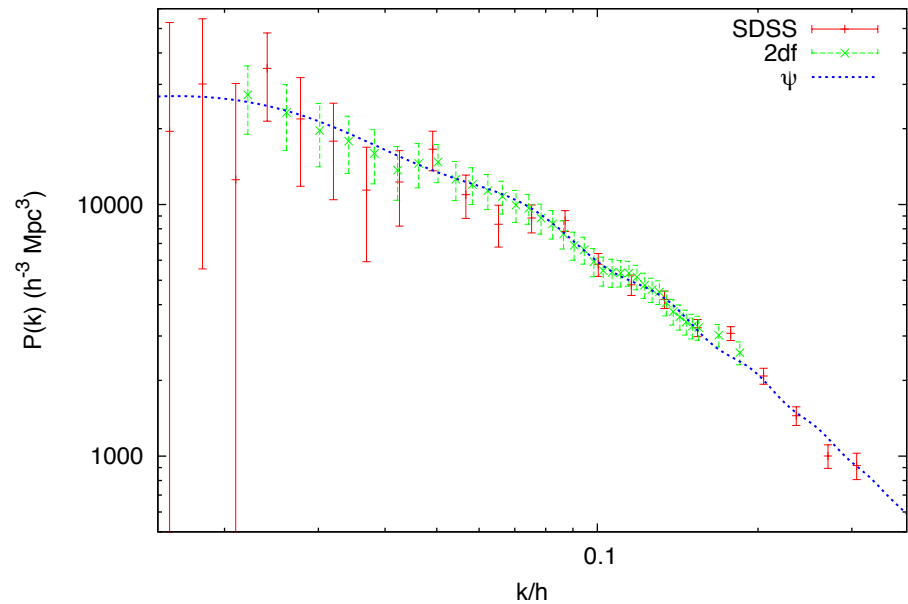
# The Cosmology

I. Rodriguez, A. Pérez-Lorenzana, E. de la Cruz, Y. Giraud-Héraud and TM. Bosonic Cosmic Dark Matter.  
 Phys. Rev. D87(2013)025009. [arXiv:1110.2751](https://arxiv.org/abs/1110.2751)

CMB anisotropies



Power Spectrum



# Scalar Field Fluctuation = Halo

J. Balakrishna, E. Seidel and W. Suen. PRD 58(1998)104004

M. Alcubierre, F. S. Guzmán, T. Matos, D. Núñez, L. A. Ureña and P. Wiederhold.  
Galactic Collapse of Scalar Field Dark Matter. [CQG 19\(2002\)5017](#). [arXiv:gr-qc/0110102](#).

Pau Amaro-Seoane, Juan Barranco, Argelia Bernal and Luciano Rezzolla.  
Constraining scalar fields with stellar kinematics and collisional dark matter. JCAP11 (2010)002

$$m \sim 1\text{eV} \quad \Rightarrow \quad \lambda = 1 \times 10^{-6}$$

$$M \sim 0.06 \sqrt{\lambda} \frac{m_{pl}^3}{m^2}$$

$$T_c = \frac{2m}{\sqrt{\lambda}}$$

$$M \sim 10^{14} M_{\odot}$$

$$T_c \sim 2000 \text{ eV}$$

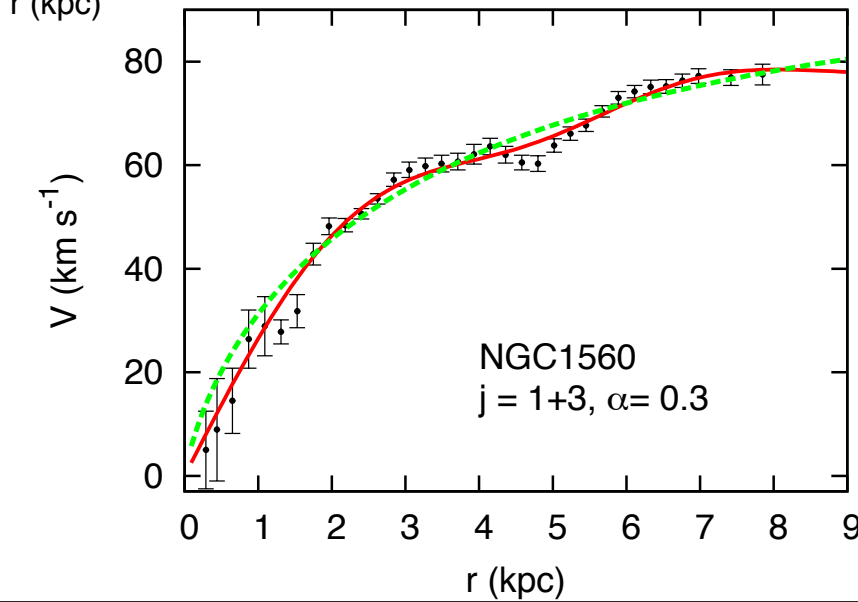
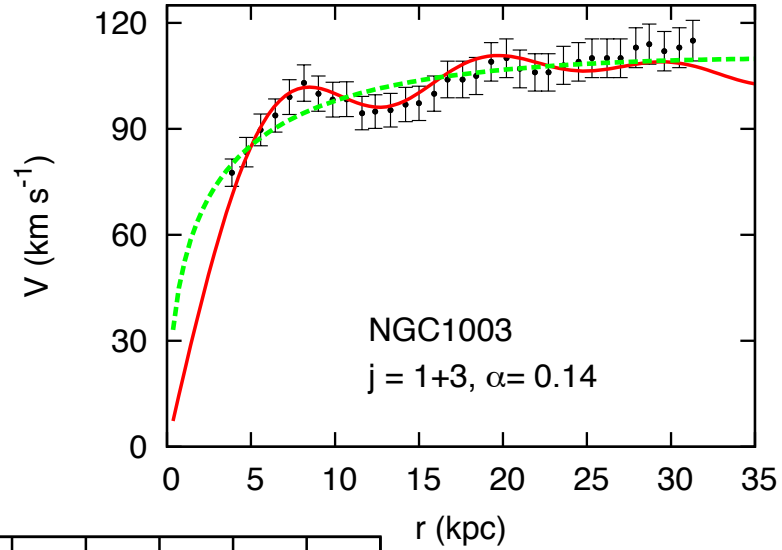
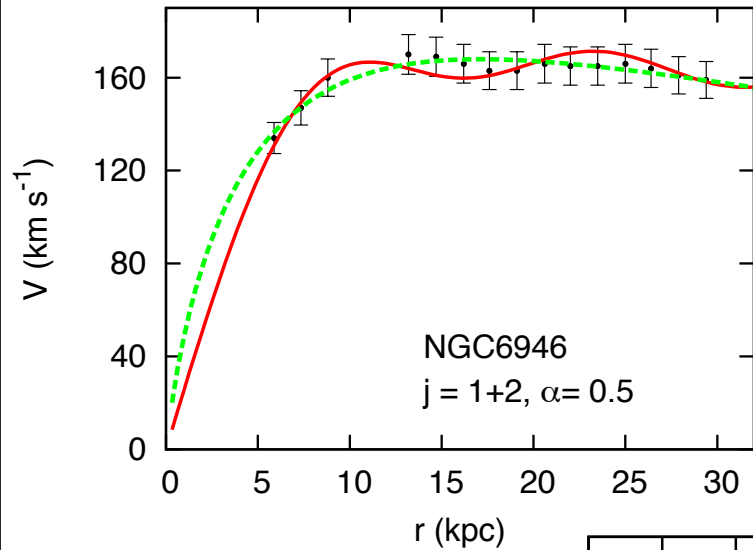
# Axions vs SFDM

Barranco and Bernal, PRD 83,(2011)043525



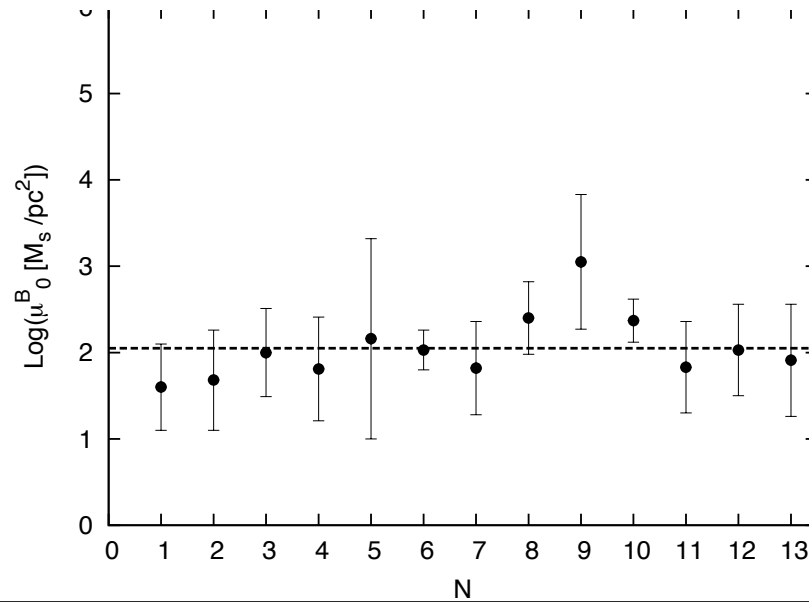
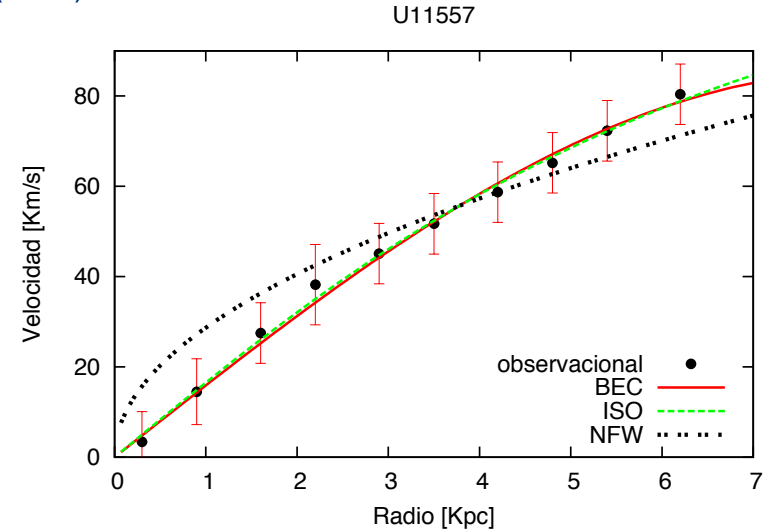
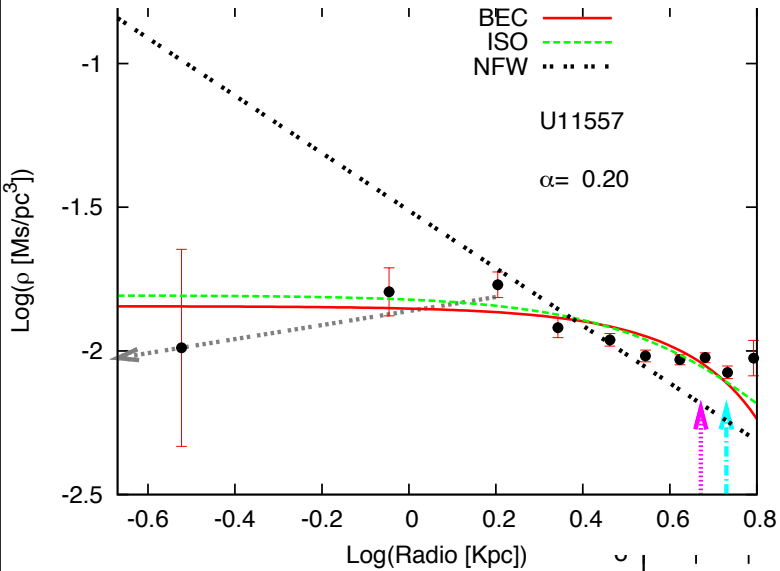
# Galaxy Formation

V. H. Robles and TM. MNRAS 392, (2012) in press. arXiv:1201.3032



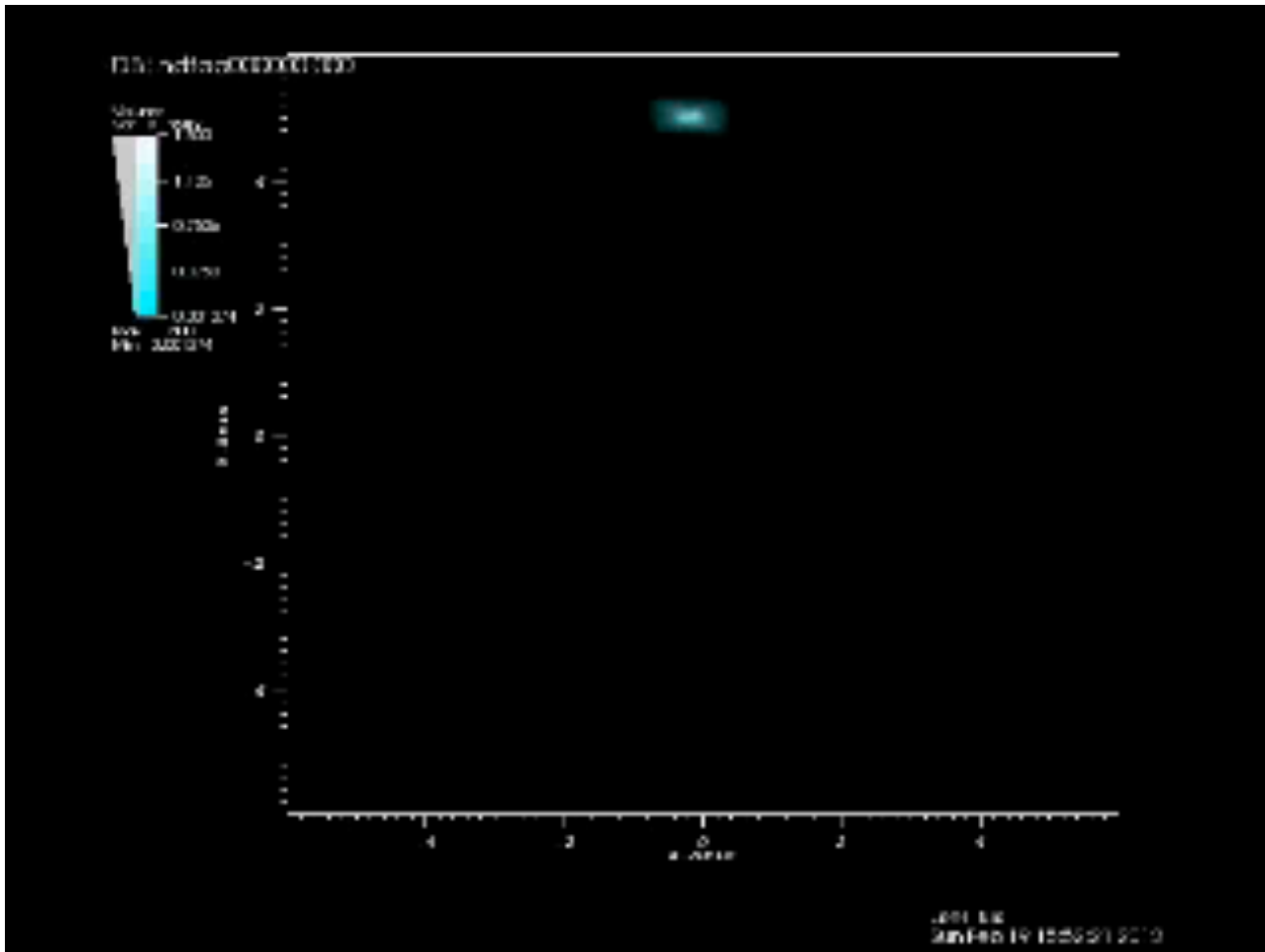
# Galaxy Formation

V. H. Robles and TM. MNRAS 422, (2012) 282. arXiv:1201.3032



# Scalar Field Fluctuation=Halo

M.Alcubierre, F. S. Guzmán, T. Matos, D. Núñez, L. A. Ureña and P. Wiederhold.  
 Galactic Collapse of Scalar Field Dark Matter. [CQG 19\(2002\)5017](#). [arXiv:gr-qc /0110102](#).

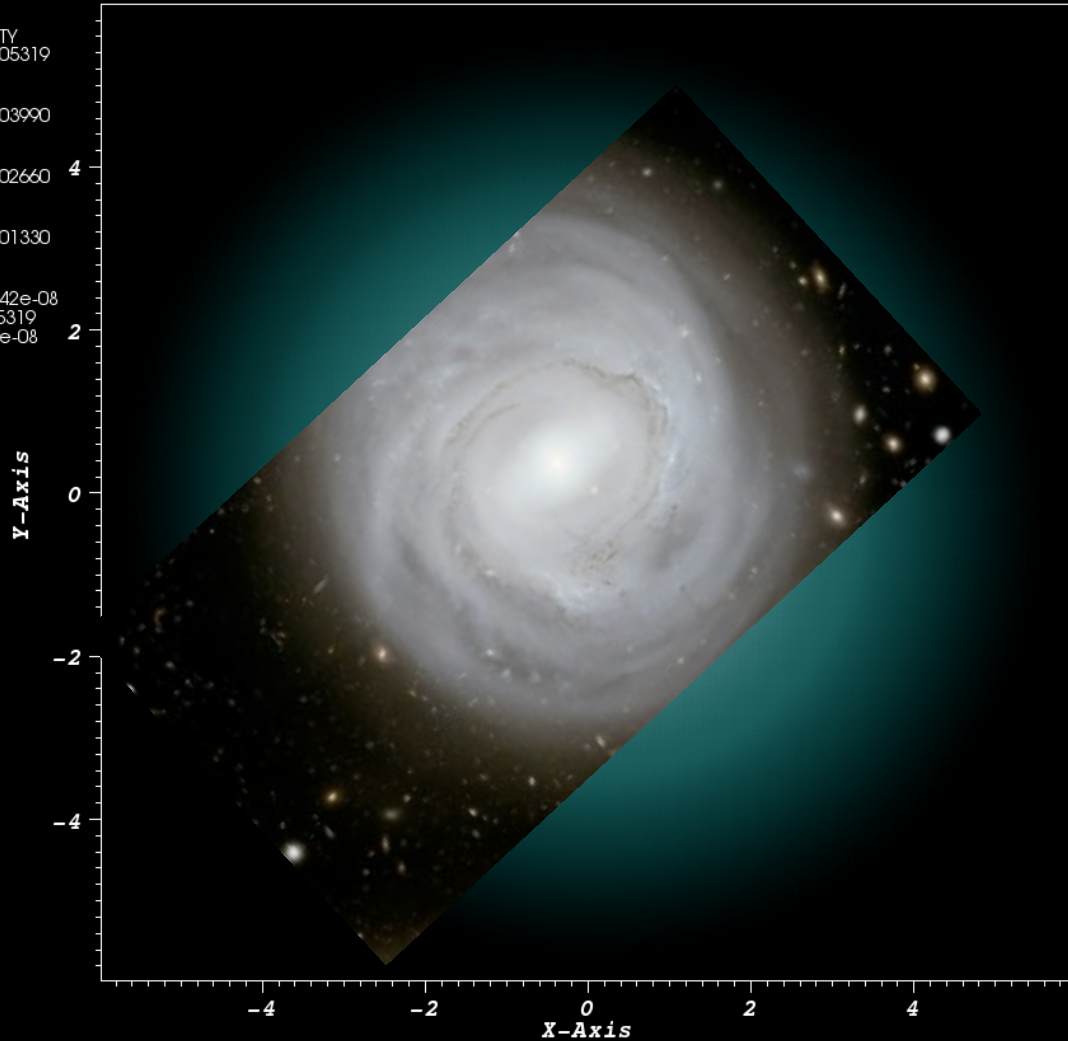




# Scalar Field Fluctuation=Halo

DB: hdfaa000000.331

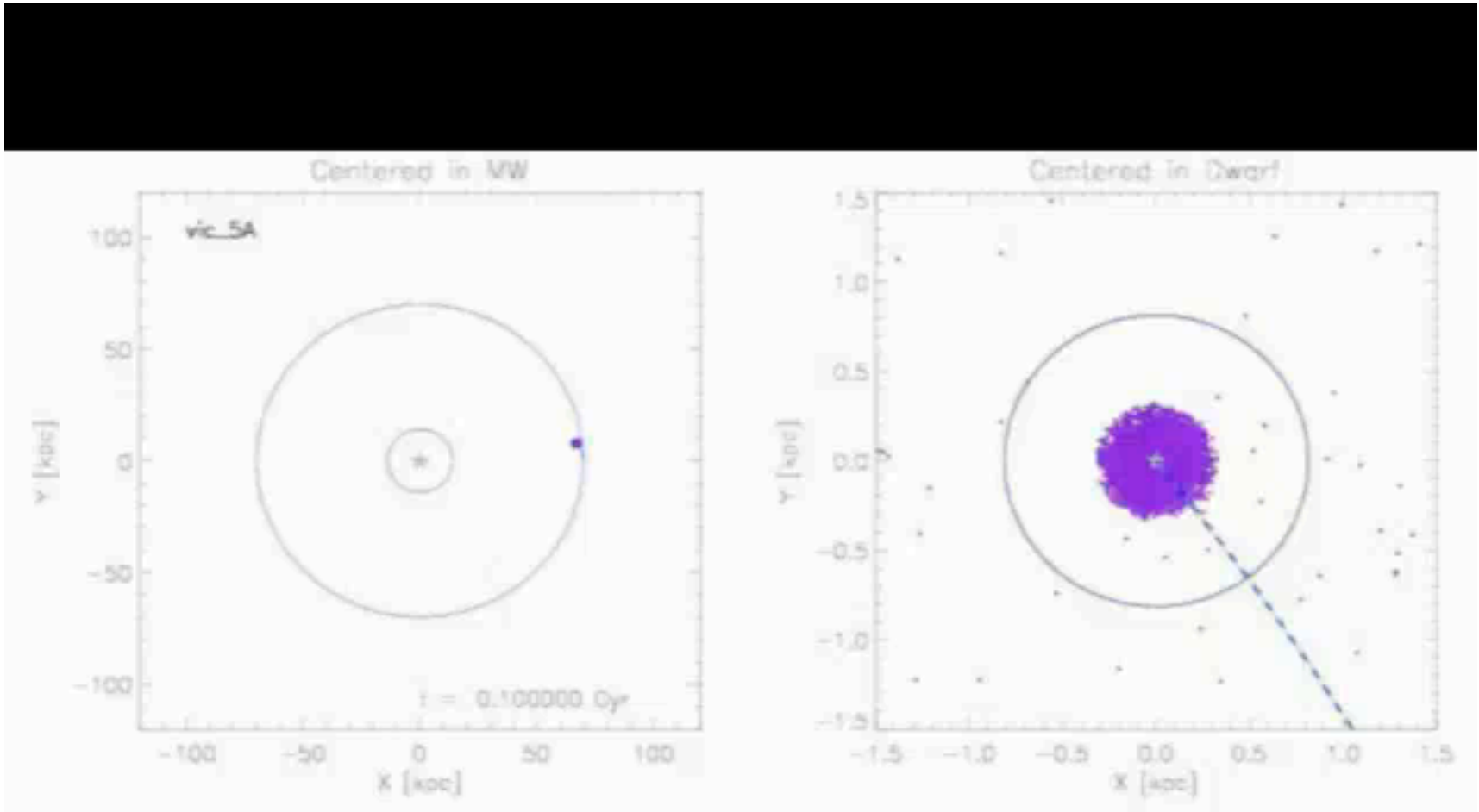
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Var: DENSITY  
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0.003990  
0.002660  
0.001330  
2.542e-08  
Max: 0.005319  
Min: 2.542e-08





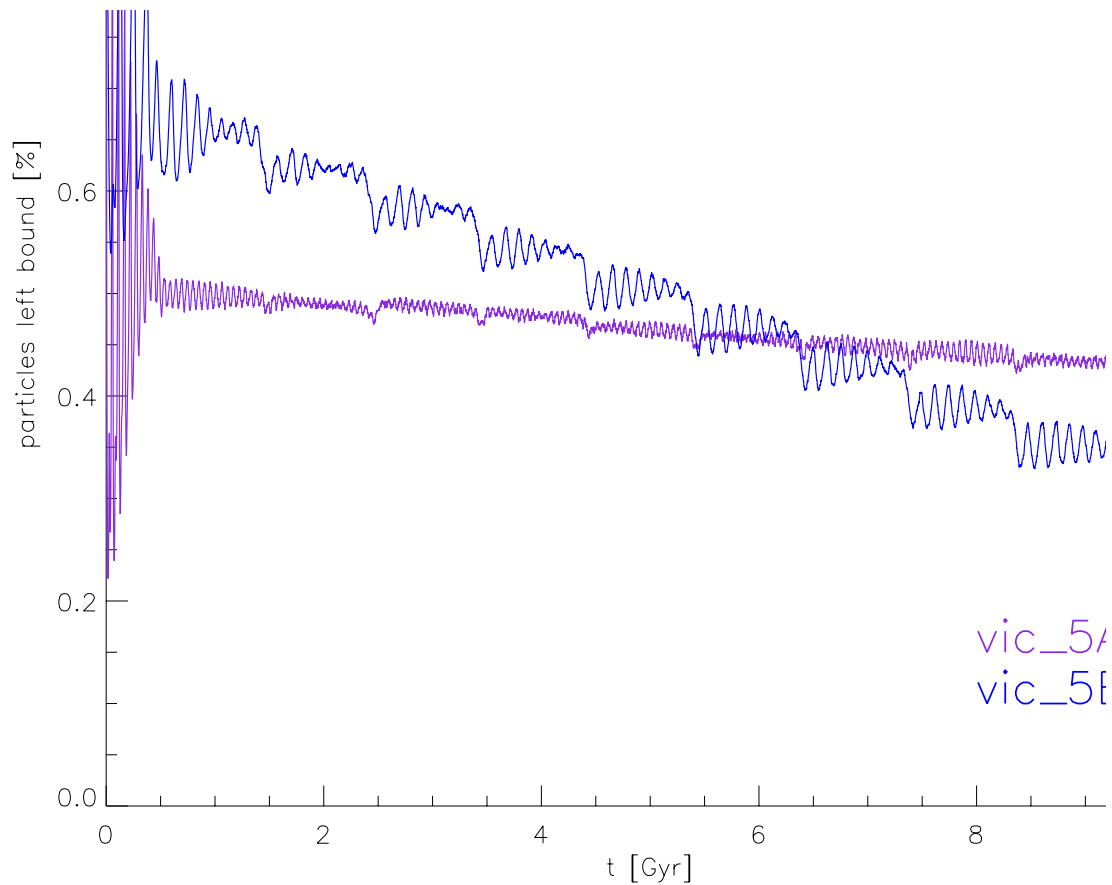
# Galactic Dynamics

V. Lora, V. Robles, F.J. Sanchez-Salcedo and TM. In preparation



MW Potential + Dwarf DM Potential + Dwarf stellar component + Miyamoto-Nagai Disc  
 $\rho_{\text{Dwarf}} = 0.16 \text{ Msun/pc}^3$ ,  $\text{peri} = 14 \text{ kpc}$ ,  $\text{apo} = 70 \text{ kpc}$  (Peri/Apo = 1/5)

V. Lora, V. Robles, F.J. Sanchez-Salcedo and TM. In preparation



A brief Review of the Scalar Field Dark Matter model. Juan Magana, Tonatiuh Matos, Victor Robles, Abril Suarez. arXiv:1201.6107

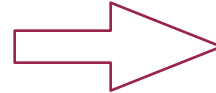
Behaves like dust at  
cosmological level

Clusters form by hierarchy

Galaxies form by  
condensation of the SF

Haloed are BEC drops

MPS has a natural cut off



Same predictions for CMB  
and MPS

Same predictions for  
structure formation

Galaxies haloed form  
earlier and are similar

Galaxies are core

Substructure is restricted

- **Scalar Field Dark Matter**  
is so far an excellent candidate to  
be the Dark Matter in the Universe