

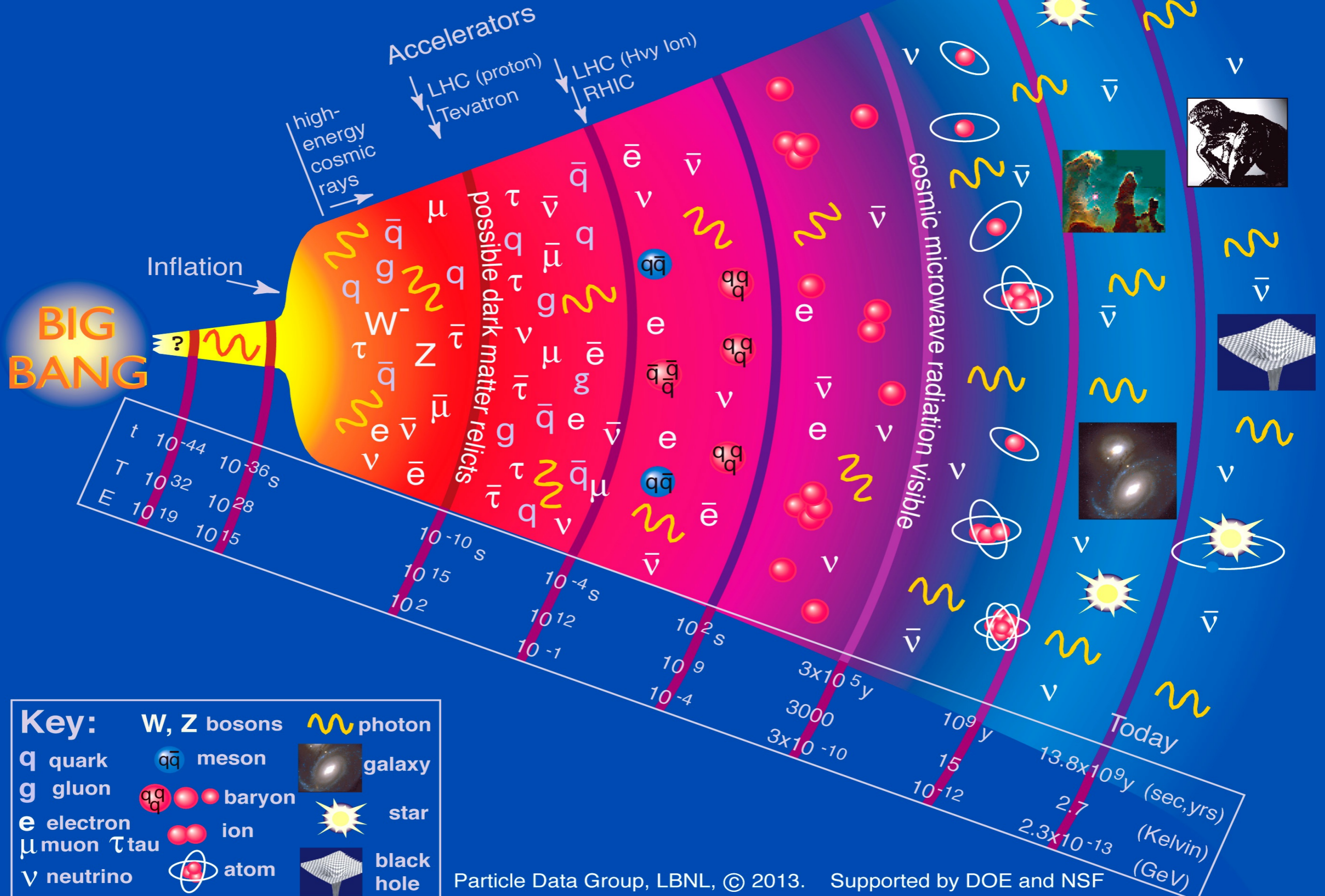
COSMOLOGICAL CONSTRAINTS ON BOSE-EINSTEIN-CONDENSED SCALAR FIELD DARK MATTER

Bohua Li

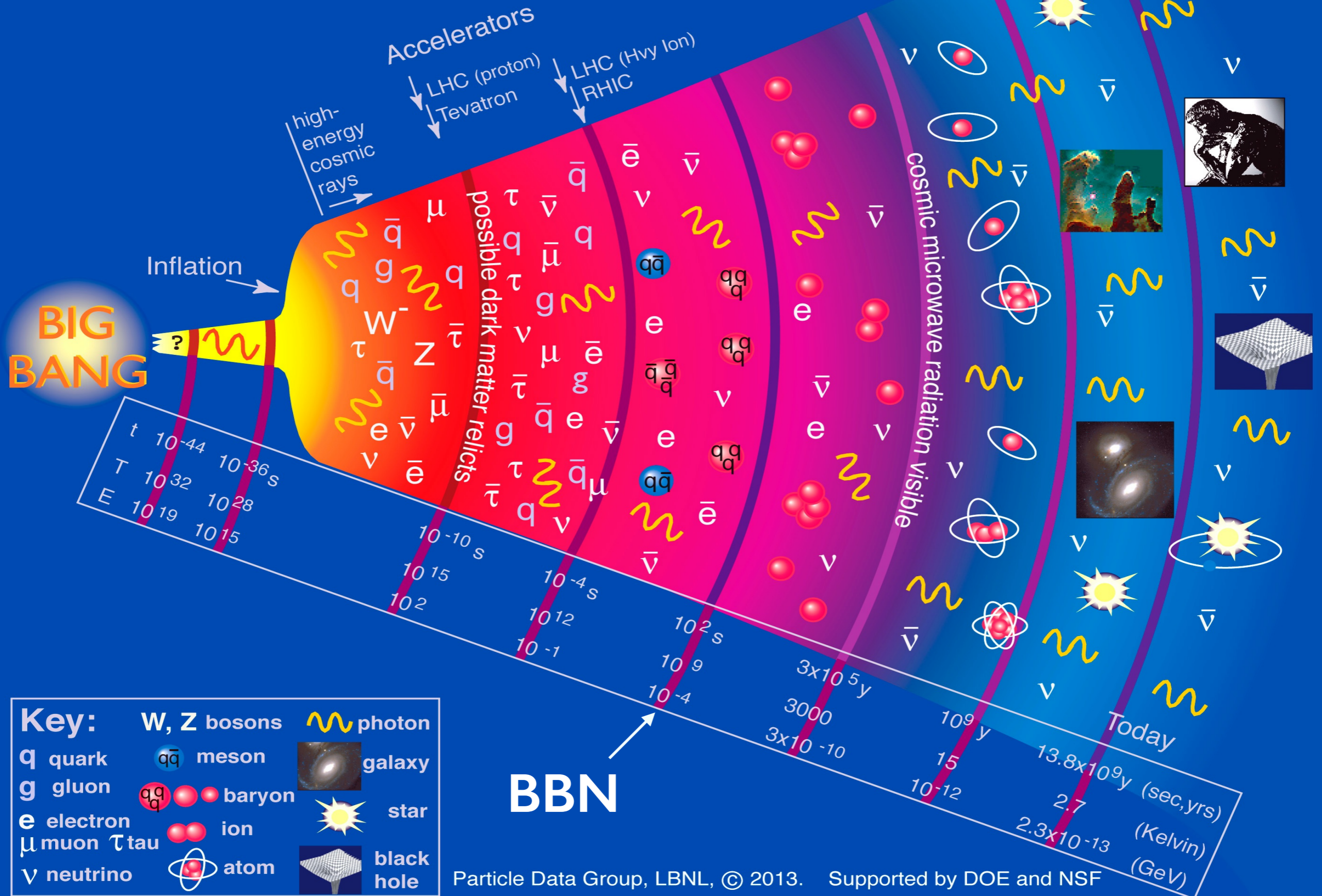
Department of Astronomy, the University of Texas at Austin
Texas Symposium, Dec 11th, 2013

(with Dr. Tanja Rindler-Daller and Dr. Paul Shapiro)
arXiv: 1310.6061, submitted to PRD

History of the Universe



History of the Universe



History of the Universe

CMB

BIG BANG

Key:

- W, Z bosons
- q quark
- g gluon
- e electron
- μ muon
- τ tau
- ν neutrino
- photon
- meson
- baryon
- ion
- atom
- galaxy
- star
- black hole

t	10^{-44}	10^{-36} s
T	10^{32}	10^{28}
E	10^{19}	10^{15}

Accelerators
 LHC (proton)
 Tevatron
 LHC (Hvy Ion)
 RHIC

high-energy cosmic rays

Inflation

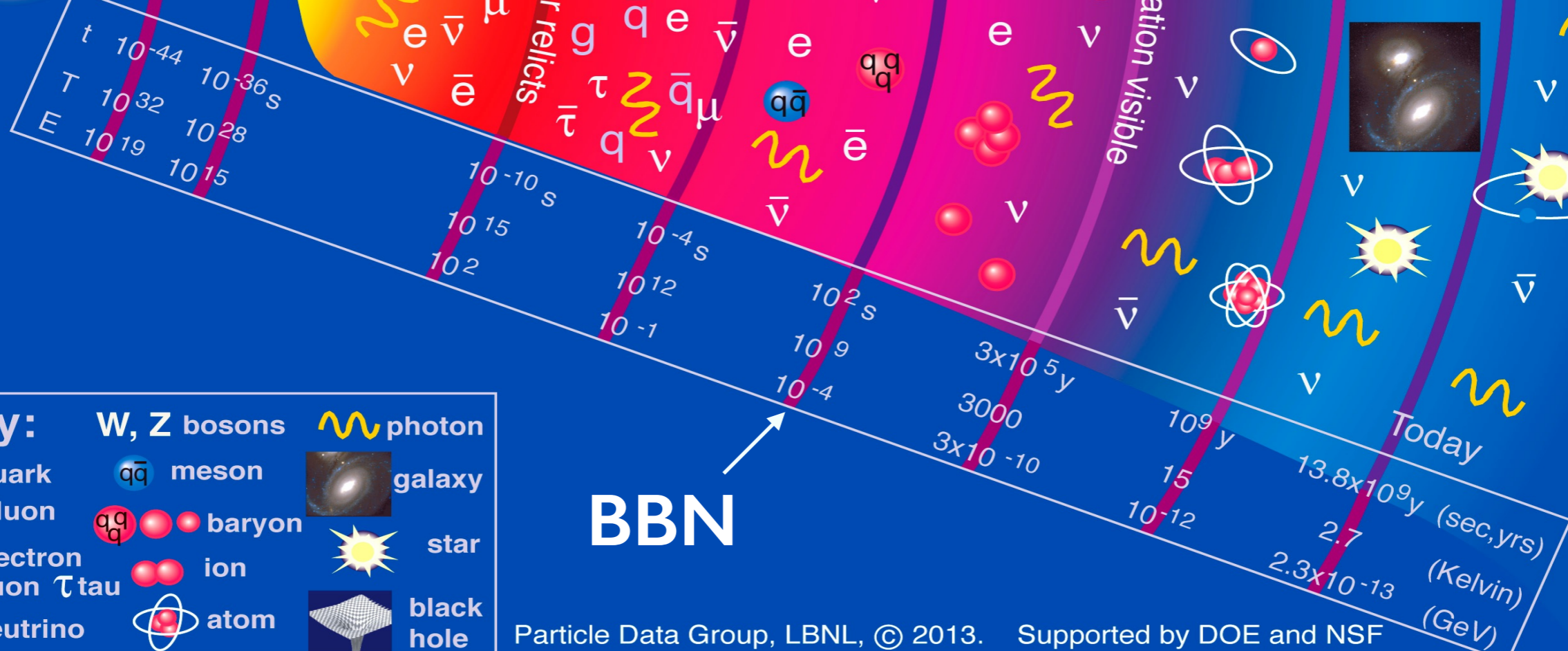
possible dark matter relicts

cosmic microwave radiation visible

BBN

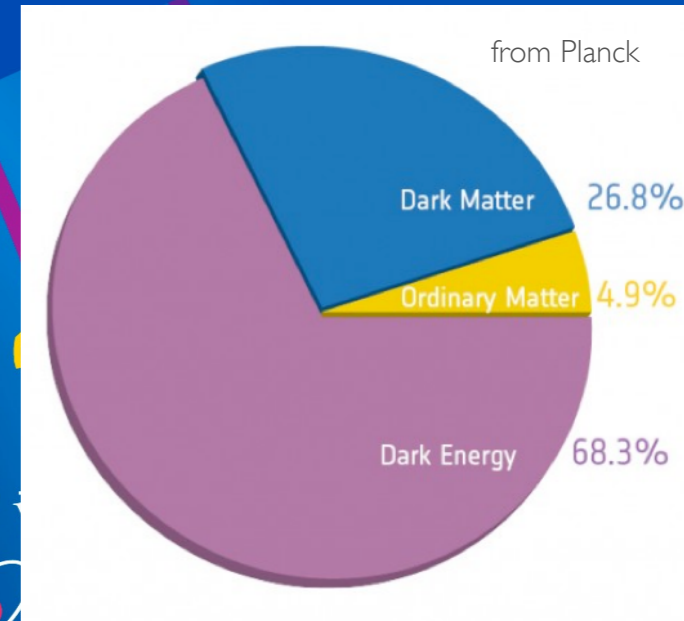
Today

Particle Data Group, LBNL, © 2013. Supported by DOE and NSF



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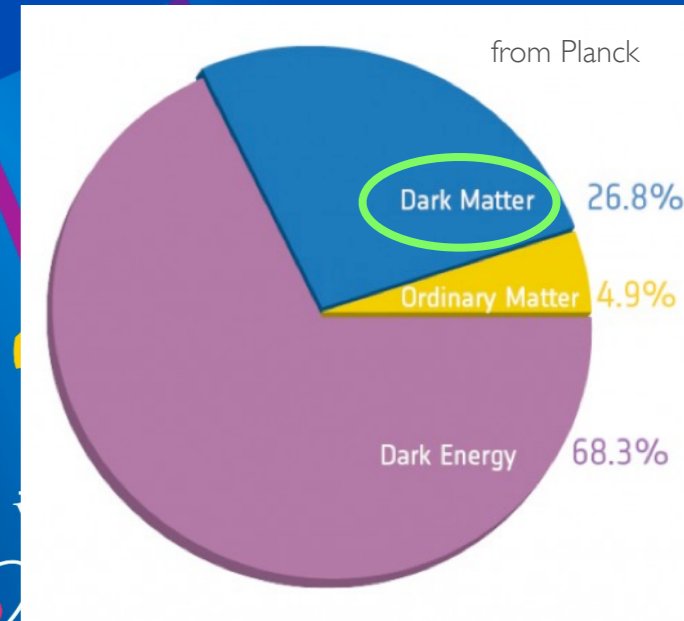
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e electron		ion	
μ muon		atom	
ν neutrino		black hole	
		galaxy	
		star	

Today	
13.8×10^9 y (sec, yrs)	
2.7	(Kelvin)
2.3×10^{-13}	(GeV)
10^{-12}	
15	
10^9 y	
3×10^5 y	
3000	
3×10^{-10}	
10^2 s	
10^9	
10^{-1}	
10^{12}	
10^{15}	
10^{-10} s	

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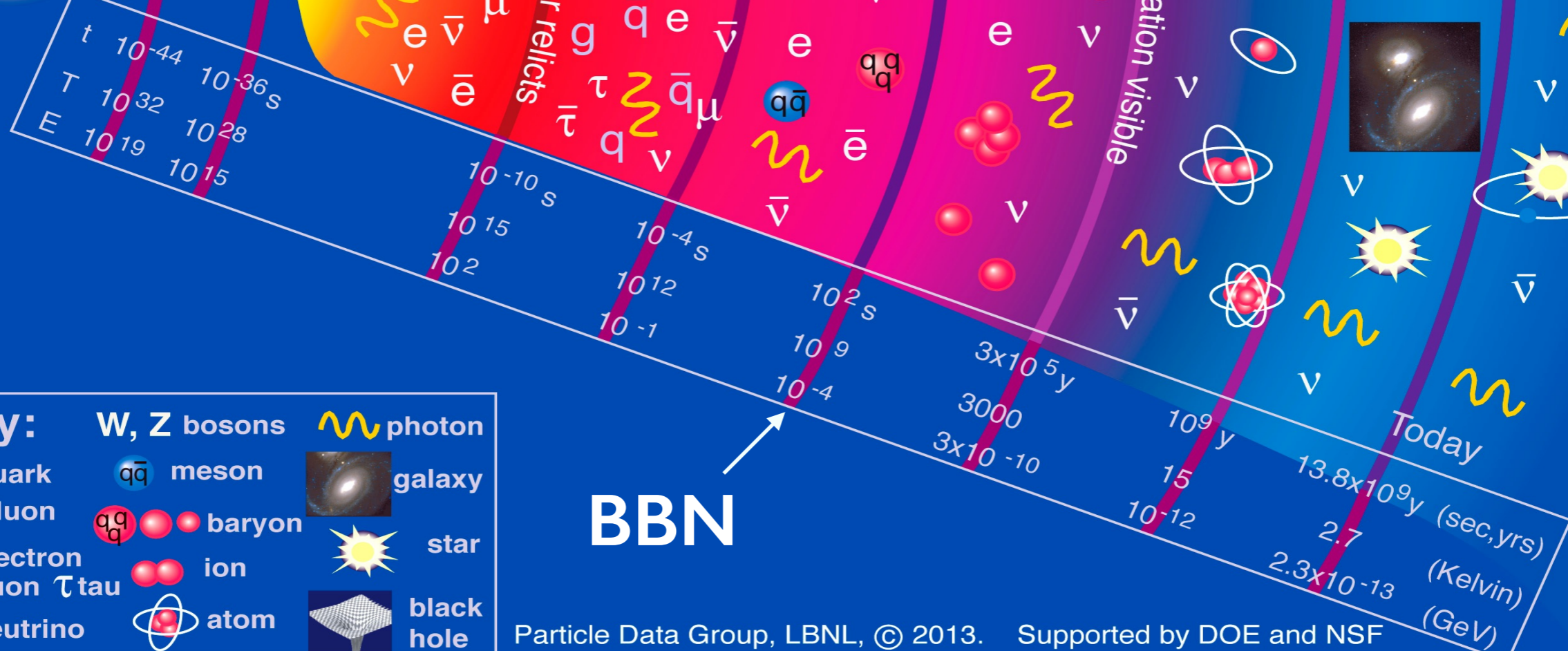
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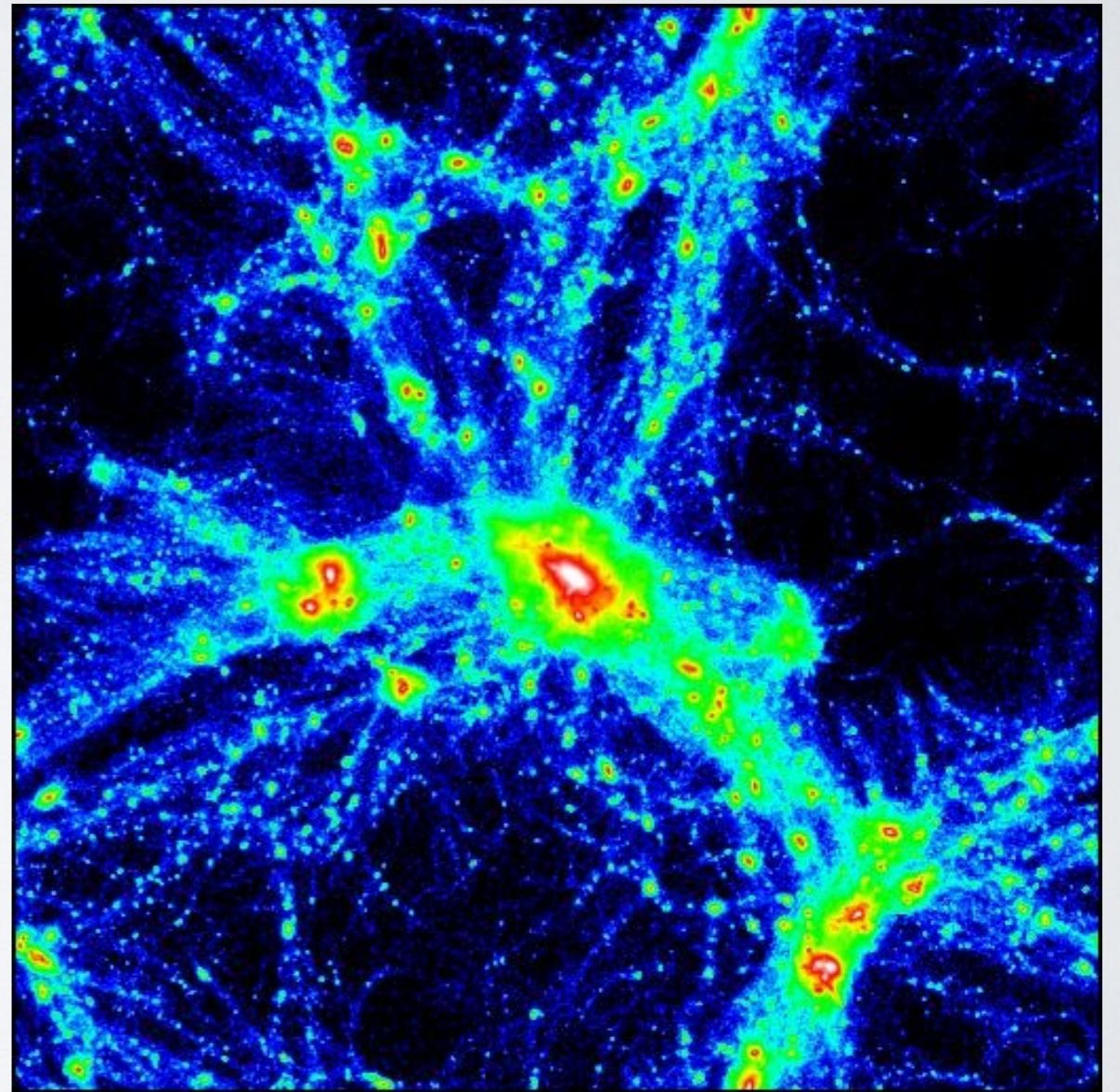
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COLD DARK MATTER

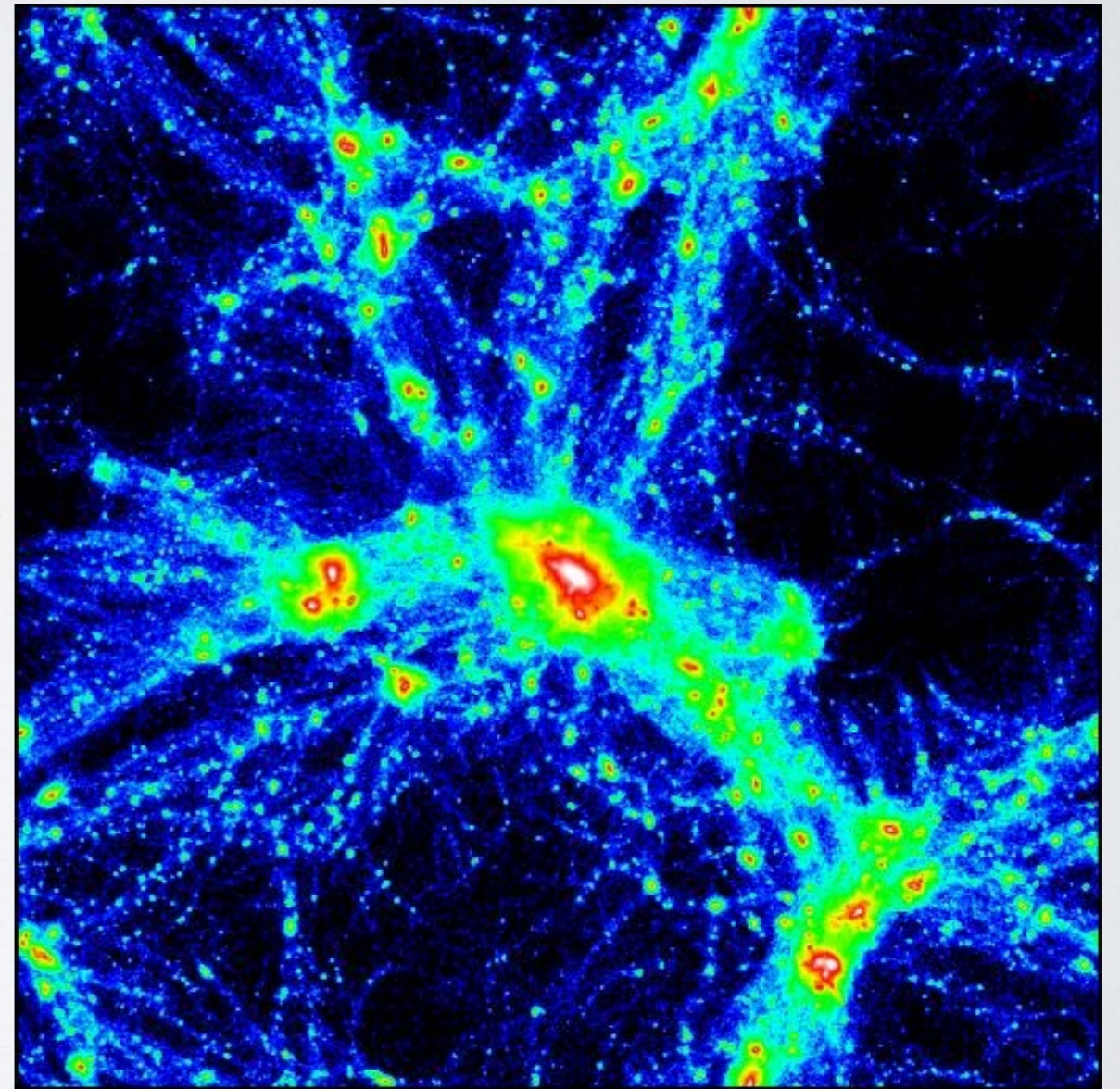
- Non-relativistic, pressureless
- Form structure gravitationally
- Beyond Standard Model of particle physics



COLD DARK MATTER

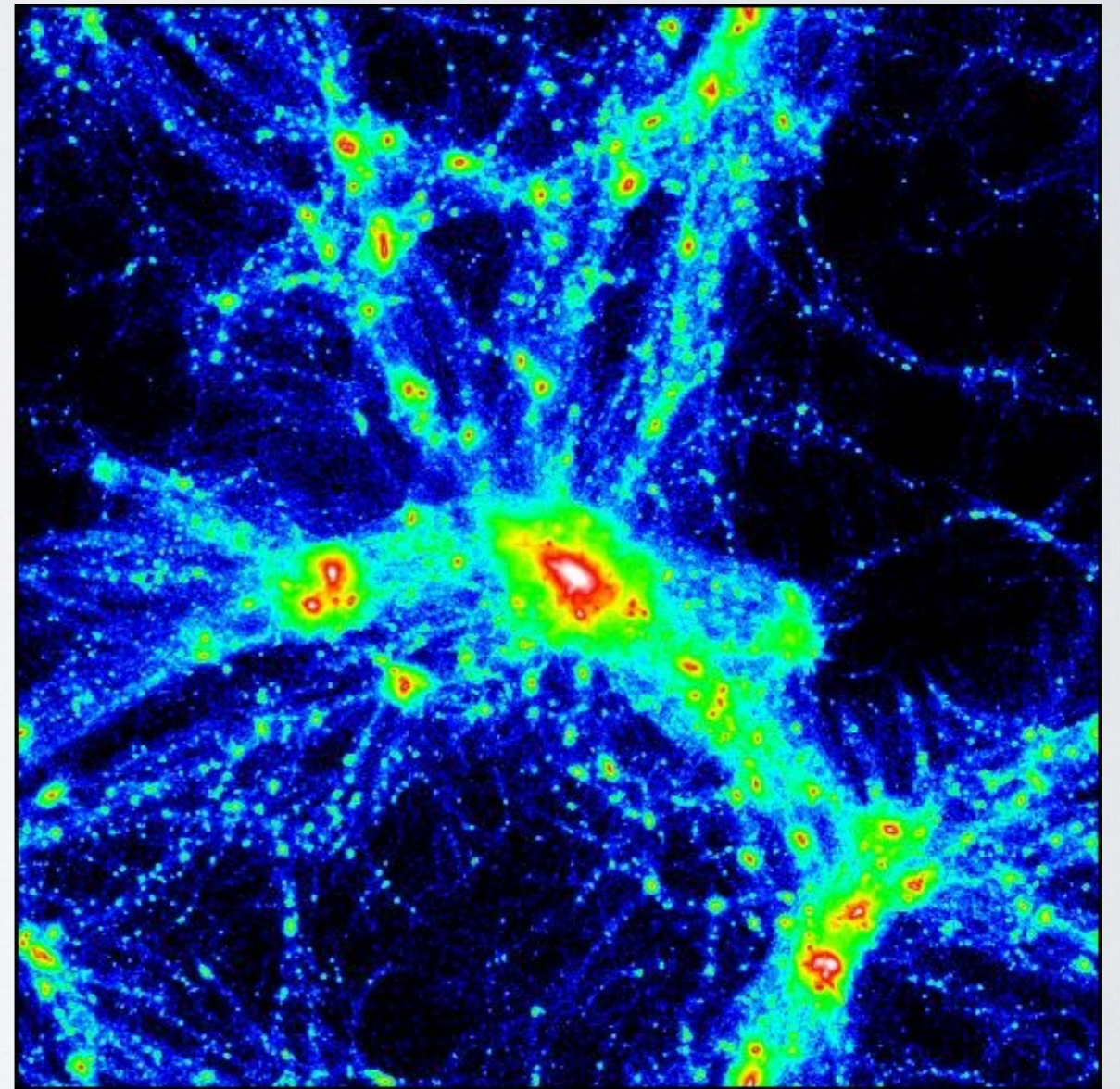
- Non-relativistic, pressureless
- Form structure gravitationally
- Beyond Standard Model of particle physics
- Candidates:
 - Weakly-interacting massive particles (WIMPs)
 - QCD Axions
 - Condensed ultralight bosons

No positive detections yet from various experiments



COLD DARK MATTER

- Non-relativistic, pressureless
- Form structure gravitationally
- Beyond Standard Model of particle physics
- Candidates:
 - Weakly-interacting massive particles (WIMPs)
 - QCD Axions
 - Condensed ultralight bosons, described by coherent classical scalar field



BEC SCALAR FIELD DARK MATTER

- Early works

- Peebles (2000), ApJ Letters, 534, L127
- Goodman (2000), New Astronomy, 5, 103
- Hu, Barkana & Gruzinov (2000), Physical Review Letters, 85, 1158

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- Particle origin of spin-0 ultralight bosons

- String axions
Arvanitaki et al. (2010), Physical Review D, 81, 123530
- Gravitationally produced by inflation
Peebles & Vilenkin (1999), Physical Review D, 60, 103506
- Gravitational exciton from multidimensional cosmological models
Günther, Starobinsky & Zhuk et al. (2004), Physical Review D, 69, 044003
- etc.

BEC SCALAR FIELD DARK MATTER

- Complex scalar field

- Conserved charge Q due to $U(1)$ symmetry
- Asymmetric dark matter
- Richer structure dynamics, e.g., vortex

Rindler-Daller & Shapiro (2012), MNRAS, 422, 135

$$Q \equiv n - \bar{n}$$

n : number density of bosons

\bar{n} : number density of anti-bosons

At later times $Q \approx n$ because anti-bosons are annihilated away

BEC SCALAR FIELD DARK MATTER

- Complex scalar field
 - Conserved charge Q due to $U(1)$ symmetry
 - Asymmetric dark matter
 - Richer structure dynamics, e.g., vortex
- Tiny mass
 - $m > 10^{-33} \text{ eV} \sim H_0$
 - ↑
required since SFDM should be cold at present

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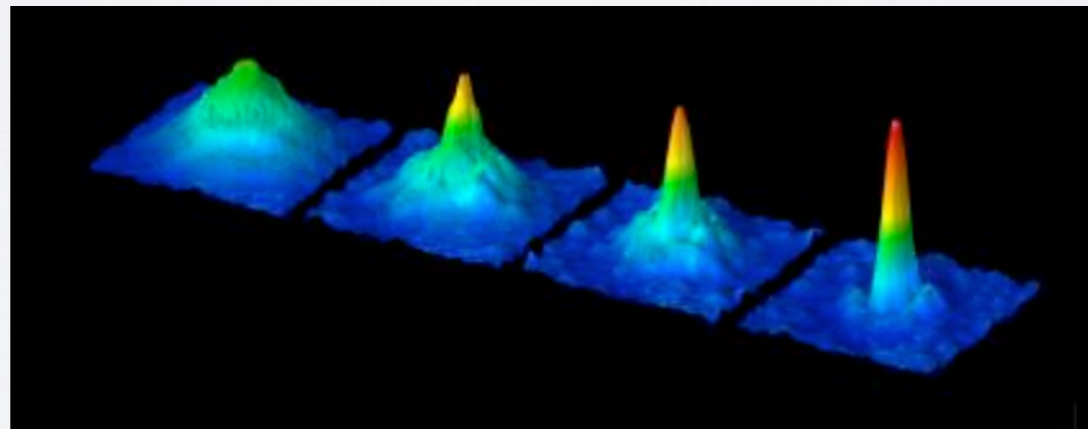
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- Bose-Einstein Condensate if initially $mQ / S \gg 1$

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BEC SCALAR FIELD DARK MATTER

- Formalism from Lagrangian

$$\mathcal{L} = \frac{\hbar^2}{2m} g^{\mu\nu} \partial_\mu \psi^* \partial_\nu \psi - V(\psi).$$

$$V(\psi) = \frac{1}{2} m c^2 |\psi|^2 + \frac{\lambda}{2} |\psi|^4.$$

- in SI units, $[\lambda] = \text{eV cm}^3$
- Fiducial model:

$$\lambda / (m c^2)^2 = 2 \times 10^{-18} \text{ eV}^{-1} \text{ cm}^3$$

$$m = 3 \times 10^{-21} \text{ eV} / c^2$$



$$\lambda = 1.8 \times 10^{-59} \text{ eV cm}^3$$

or dimensionless value
 $\hat{\lambda} \sim 10^{-80}$

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Why these values?

Small-scale controversies of collisionless CDM

- Cusp/core problem: *too steep a central density profile of dark matter halos*
- Missing satellites problem: *too many substructures predicted*
- 'Too big to fail': *biggest subhalos have too high circular velocities to hold classical MW satellites*
- etc.

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- etc.

Potentially resolvable through SFDM

SFDM provides minimum clustering scales

- de Broglie wave length l_{deB}
- self-interaction Jeans length $l_{\text{SI}} \propto \sqrt{\lambda / (m c^2)^2}$

HOMOGENEOUS Λ SFDM UNIVERSE

- FRW metric $ds^2 = c^2 dt^2 - a^2(t)(dx^2 + dy^2 + dz^2)$
- Friedmann equation

$$H^2(t) \equiv \left(\frac{da/dt}{a} \right)^2 = \frac{8\pi G}{3c^2} [\bar{\rho}_r(t) + \bar{\rho}_b(t) + \bar{\rho}_\Lambda(t) + \bar{\rho}_{\text{SFDM}}(t)],$$

Radiation: $\bar{\rho}_r = \bar{\rho}_{r,0} / a^4$
(photons+3 SM neutrinos)

Baryons: $\bar{\rho}_b = \bar{\rho}_{b,0} / a^3$

Cosmological constant: $\bar{\rho}_\Lambda = \bar{\rho}_{\Lambda,0}$

present-day cosmological parameters from Planck

Basic		Derived	
h	0.673	$\Omega_m h^2$	0.14187
$\Omega_b h^2$	0.02207	$\Omega_r h^2$	4.184×10^{-5}
$\Omega_c h^2$	0.1198	z_{eq}	3390
T_{CMB}/K	2.7255	Ω_Λ	0.687

EVOLUTION OF HOMOGENEOUS SFDM

- Ideal fluid

$$\bar{\rho} = T^0_0 = \frac{\hbar^2}{2mc^2} |\partial_t \psi|^2 + \frac{1}{2} mc^2 |\psi|^2 + \frac{1}{2} \lambda |\psi|^4,$$
$$\bar{p} = -T^i_i = \frac{\hbar^2}{2mc^2} |\partial_t \psi|^2 - \frac{1}{2} mc^2 |\psi|^2 - \frac{1}{2} \lambda |\psi|^4.$$

- Klein-Gordon equation

$$\frac{\hbar^2}{2mc^2} \partial_t^2 \psi + \frac{\hbar^2}{2mc^2} \frac{3da/dt}{a} \partial_t \psi + \frac{1}{2} mc^2 \psi + \lambda |\psi|^2 \psi = 0$$

SFDM EVOLUTIONARY PHASES

- Fast-oscillation regime ($\omega / H \gg 1$)

Define:

$$\psi = |\psi|e^{i\theta}$$
$$\omega \equiv \partial_t \theta$$

SFDM EVOLUTIONARY PHASES

- Fast-oscillation regime ($\omega / H \gg 1$)

- temporal averaging approximation

Define:

$$\psi = |\psi|e^{i\theta}$$

$$\omega \equiv \partial_t \theta$$

Turner (1983), Physical Review D, 28, 1243

Peebles & Vilenkin (1999), Physical Review D, 60, 103506

$$\begin{aligned} \langle \bar{\rho} \rangle &= mc^2 \langle |\psi|^2 \rangle + \frac{3}{2} \lambda \langle |\psi|^4 \rangle \\ &\approx mc^2 \langle |\psi|^2 \rangle + \frac{3}{2} \lambda \langle |\psi|^2 \rangle^2, \\ \langle \bar{p} \rangle &= \frac{1}{2} \lambda \langle |\psi|^4 \rangle \approx \frac{1}{2} \lambda \langle |\psi|^2 \rangle^2. \end{aligned}$$

-Equation of state

$$\langle \bar{p} \rangle = \frac{m^2 c^4}{18\lambda} \left(\sqrt{1 + \frac{6\lambda \langle \bar{\rho} \rangle}{m^2 c^4}} - 1 \right)^2 \quad \text{or} \quad \langle \bar{w} \rangle \equiv \frac{\langle \bar{p} \rangle}{\langle \bar{\rho} \rangle} = \frac{1}{3} \left[\frac{1}{1 + \frac{2mc^2}{3\lambda \langle |\psi|^2 \rangle}} \right]$$

Colpi, Shapiro & Wasserman (1986), Physical Review Letters, 57, 2485

Matos & Arturo Ureña-López (2001), Physical Review D, 63, 063506

SFDM EVOLUTIONARY PHASES

- Fast-oscillation regime ($\omega / H \gg 1$)

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- CDM-like phase: non-relativistic

$$\frac{3}{2} \lambda \langle |\psi|^2 \rangle^2 \ll mc^2 \langle |\psi|^2 \rangle$$

$$\langle \bar{w} \rangle \equiv \langle \bar{p} \rangle / \langle \bar{\rho} \rangle = 0$$

$$\langle \bar{\rho} \rangle \propto a^{-3}$$

SFDM EVOLUTIONARY PHASES

- Fast-oscillation regime ($\omega / H \gg 1$)

$$\begin{aligned}\langle \bar{\rho} \rangle &= mc^2 \langle |\psi|^2 \rangle + \frac{3}{2} \lambda \langle |\psi|^4 \rangle \\ &\approx mc^2 \langle |\psi|^2 \rangle + \frac{3}{2} \lambda \langle |\psi|^2 \rangle^2, \\ \langle \bar{p} \rangle &= \frac{1}{2} \lambda \langle |\psi|^4 \rangle \approx \frac{1}{2} \lambda \langle |\psi|^2 \rangle^2.\end{aligned}$$

- Radiation-like phase: relativistic

$$\frac{3}{2} \lambda \langle |\psi|^2 \rangle^2 \gg mc^2 \langle |\psi|^2 \rangle$$

$$\langle \bar{w} \rangle = 1/3$$

$$\langle \bar{\rho} \rangle \propto a^{-4}$$

SFDM EVOLUTIONARY PHASES

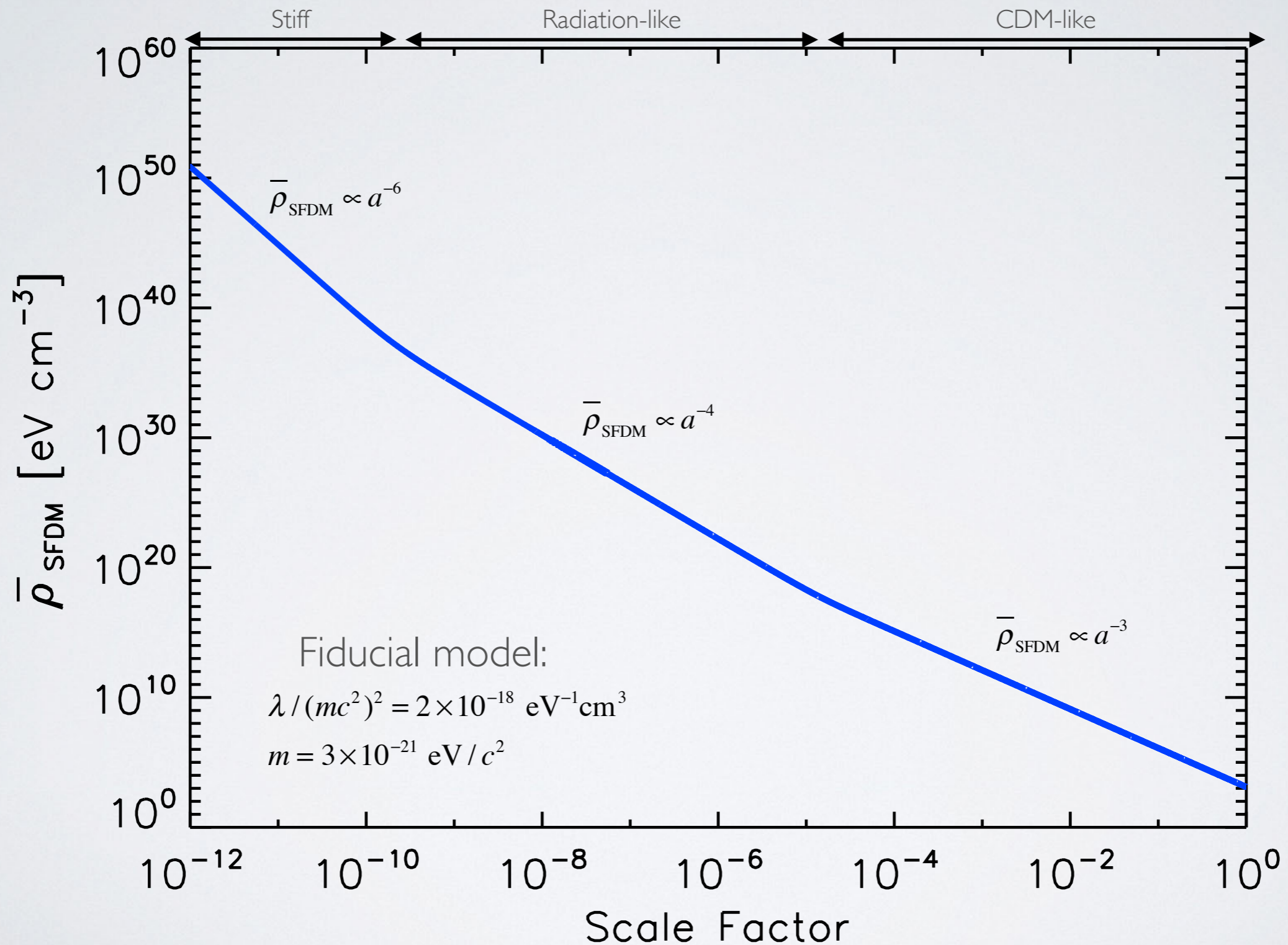
- Slow-oscillation regime ($\omega / H \ll 1$)

$$\bar{p} \approx \bar{\rho} \approx \frac{\hbar^2}{2mc^2} |\partial_t \psi|^2.$$

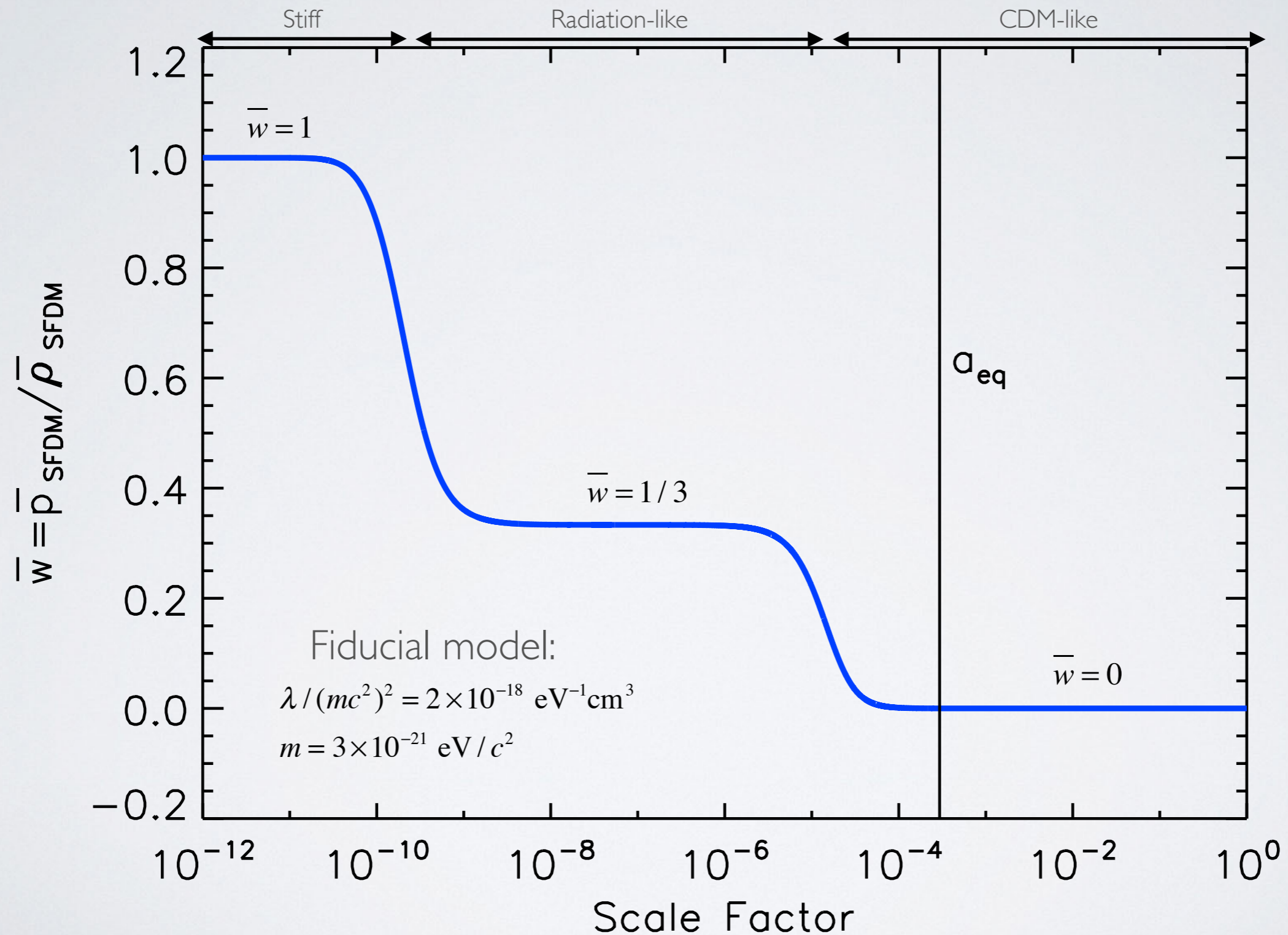
- Stiff phase: relativistic

$$\bar{w} = 1 \quad \bar{\rho} \propto a^{-6}$$

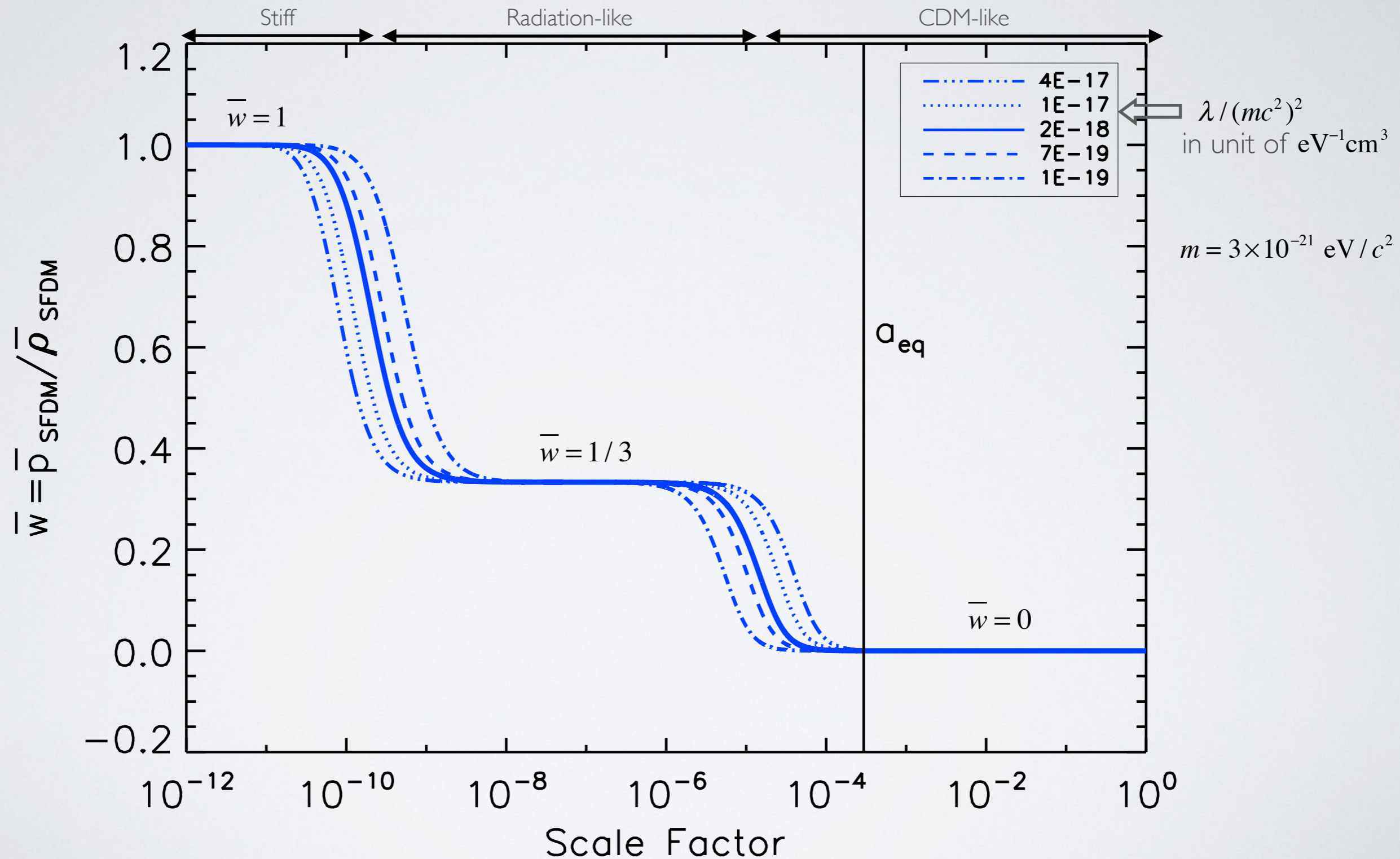
SOLUTION: Λ SFDM EVOLUTION



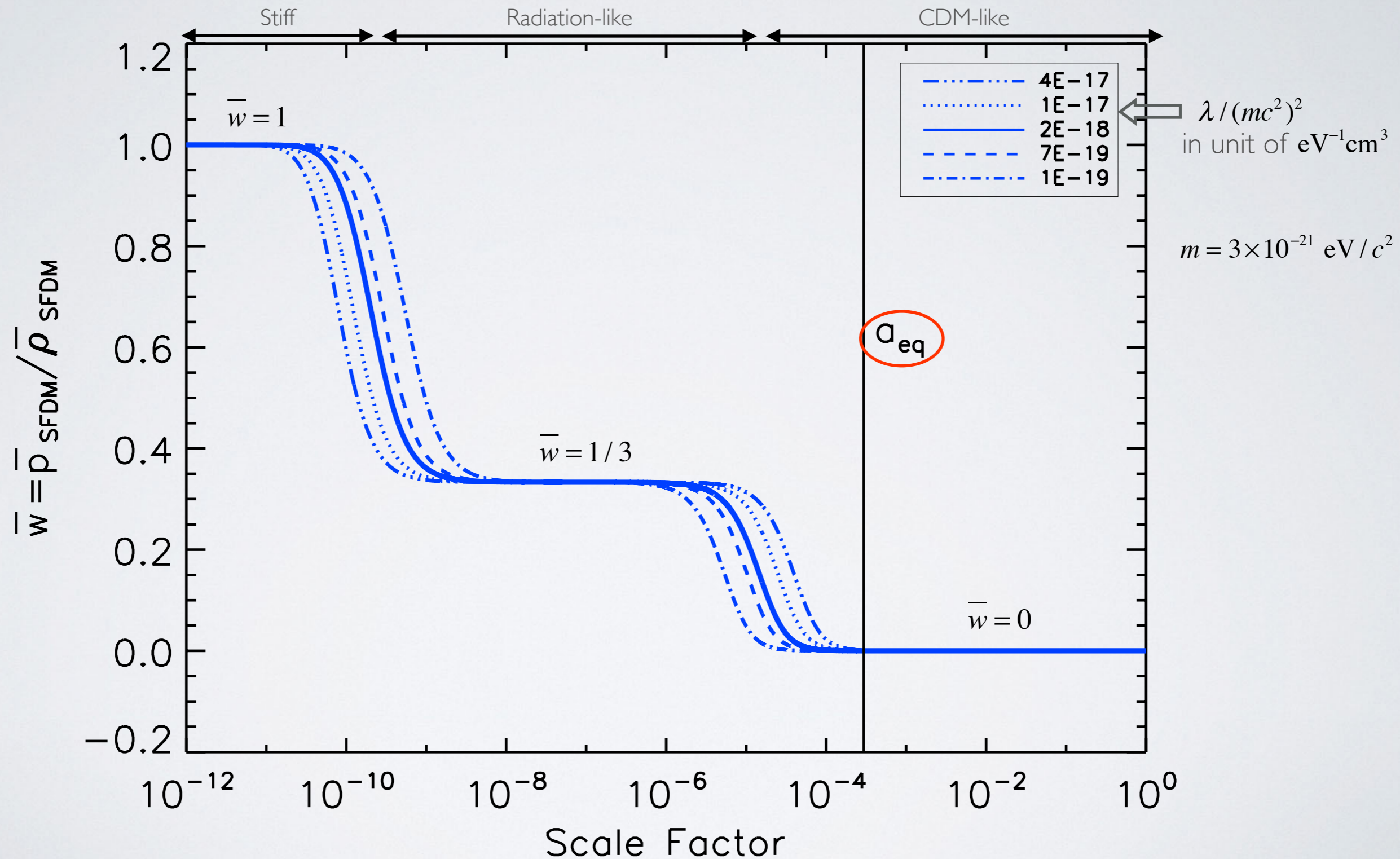
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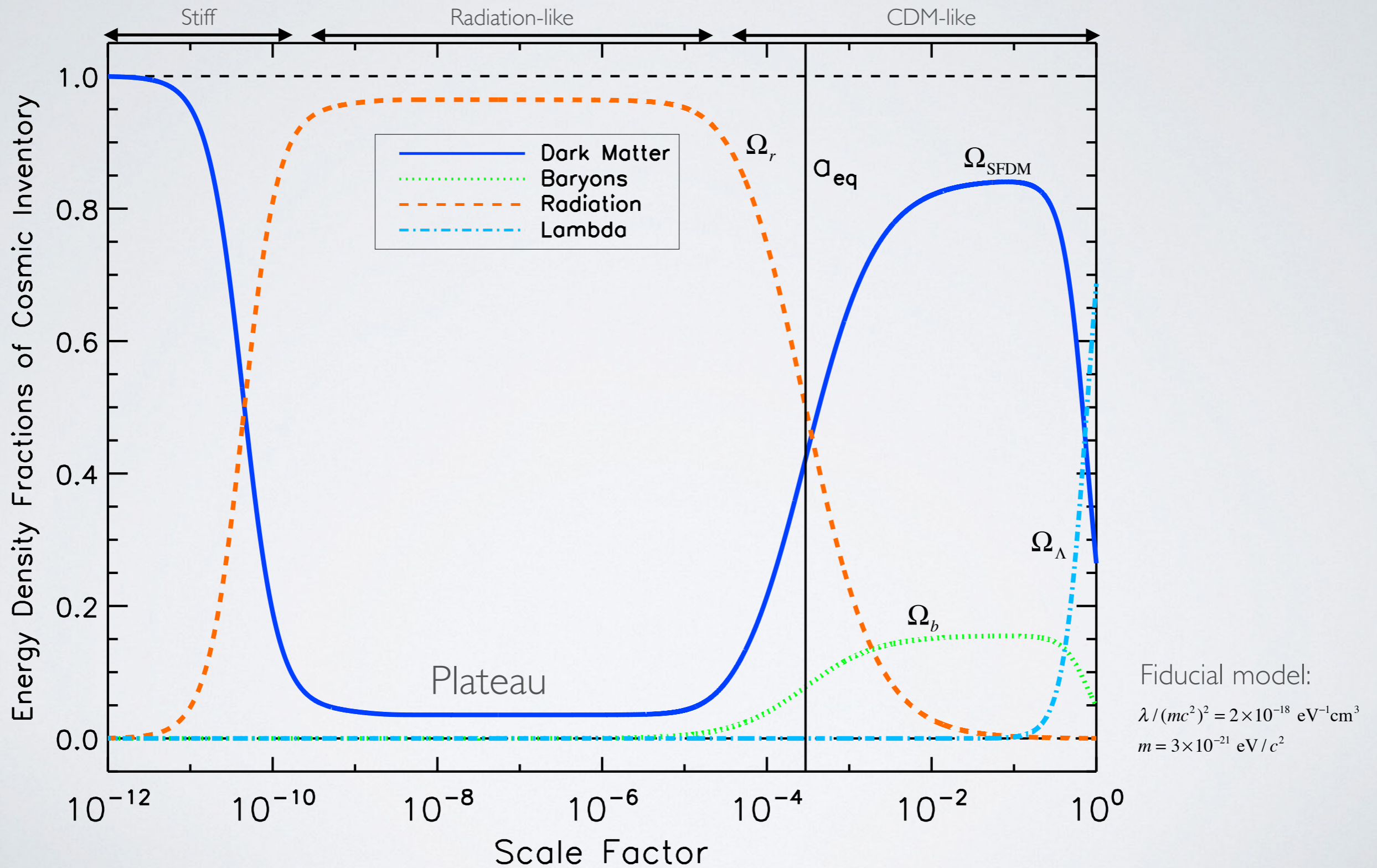
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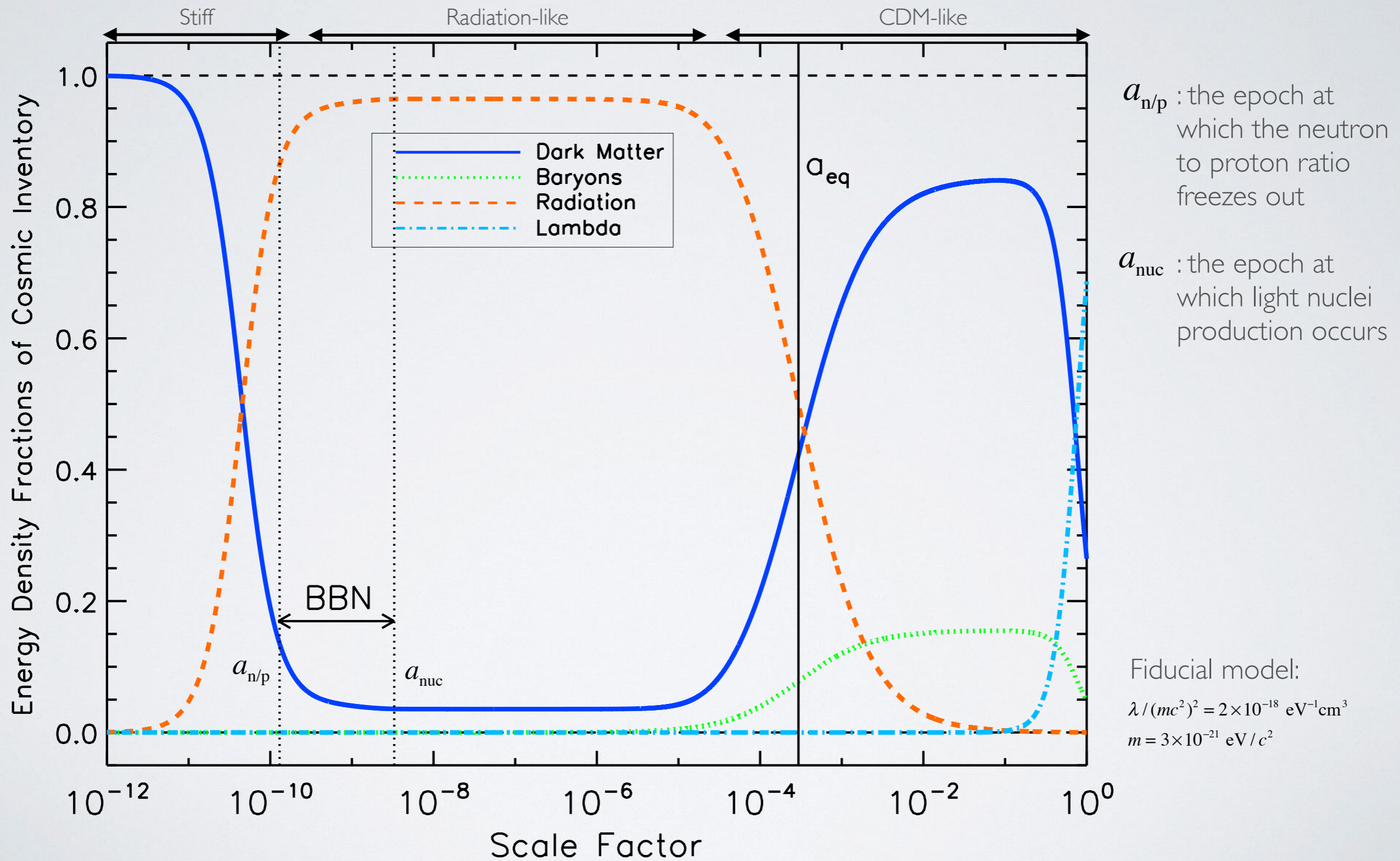
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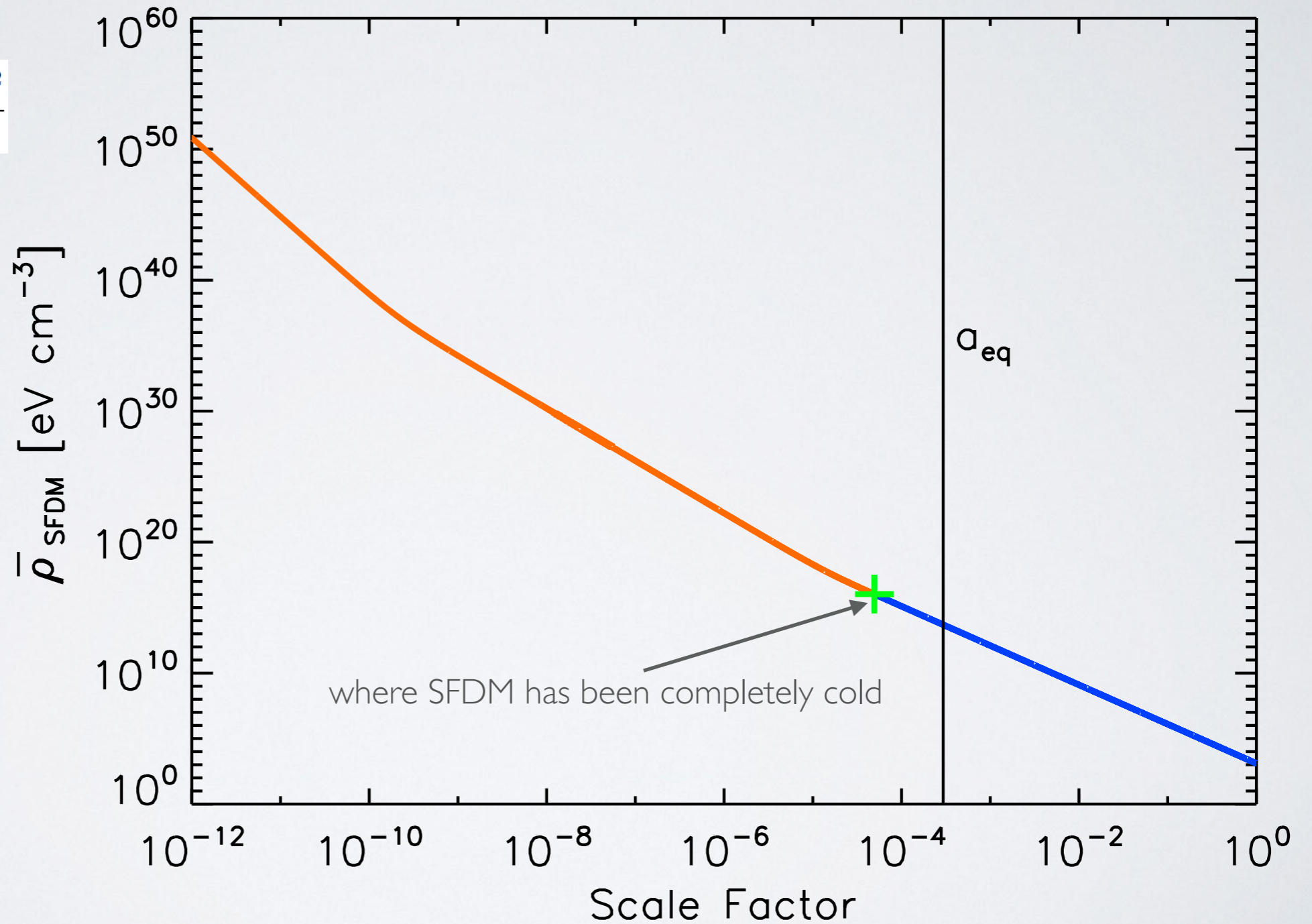
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CONSTRAINTS

- From z_{eq}

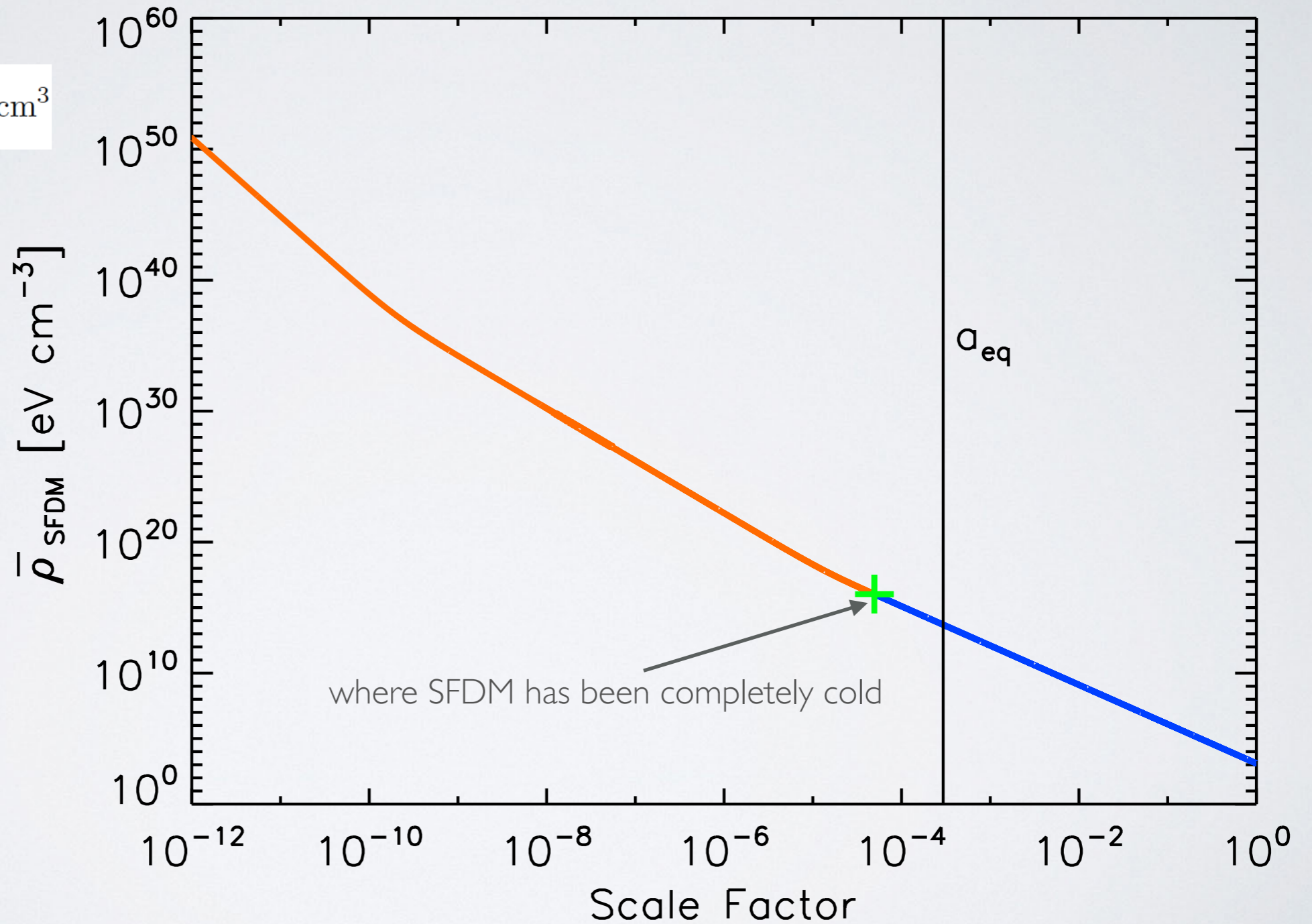
$$1 + z_{\text{eq}} \equiv \frac{1}{a_{\text{eq}}} = \frac{\Omega_b h^2 + \Omega_c h^2}{\Omega_r h^2}$$



CONSTRAINTS

- From Z_{eq}

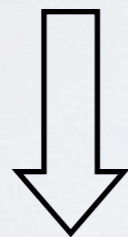
$$\frac{\lambda}{(mc^2)^2} \leq 4 \times 10^{-17} \text{ eV}^{-1} \text{ cm}^3$$



CONSTRAINTS

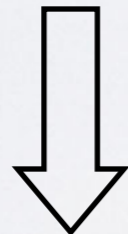
- From N_{eff} : the effective number of neutrino species

Relativistic SFDM



$$\frac{\Delta N_{\text{eff}}}{N_{\text{eff,standard}}} = \frac{\bar{\rho}_{\text{SFDM}}}{\bar{\rho}_{\nu}},$$

Expansion rate (N_{eff})



Primordial light element abundances ($[\text{He}]$, $[\text{D}]$, ...)

$$N_{\text{eff,standard}} = 3.046$$

accounts for 3 SM neutrinos

$$\Delta N_{\text{eff}} \equiv N_{\text{eff}} - N_{\text{eff,standard}}$$

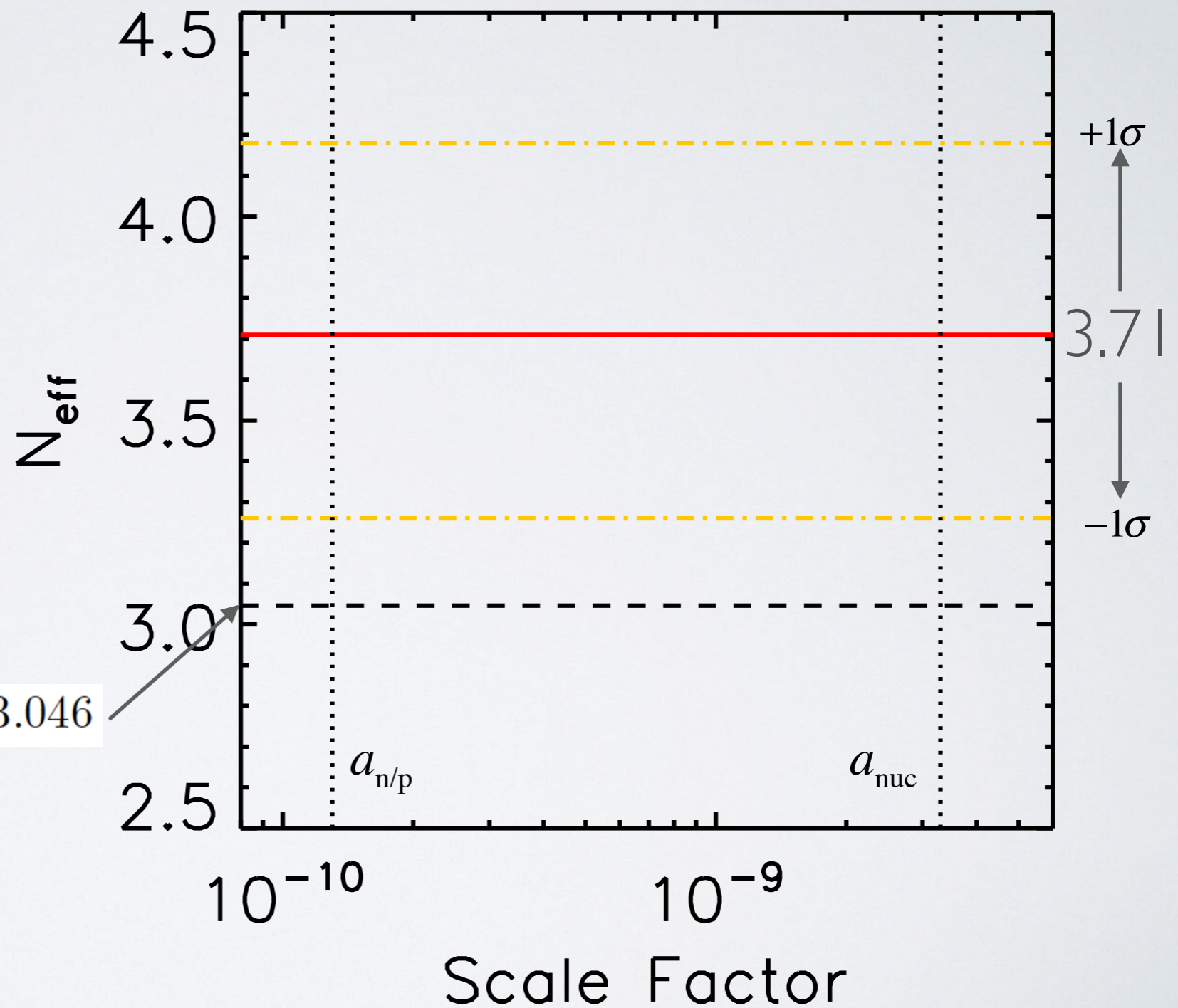
CONSTRAINTS

- From N_{eff}

$$N_{\text{eff}} = 3.71^{+0.47}_{-0.45}$$

Steigman (2012), arXiv:1208.0032

$$N_{\text{eff,standard}} = 3.046$$



CONSTRAINTS

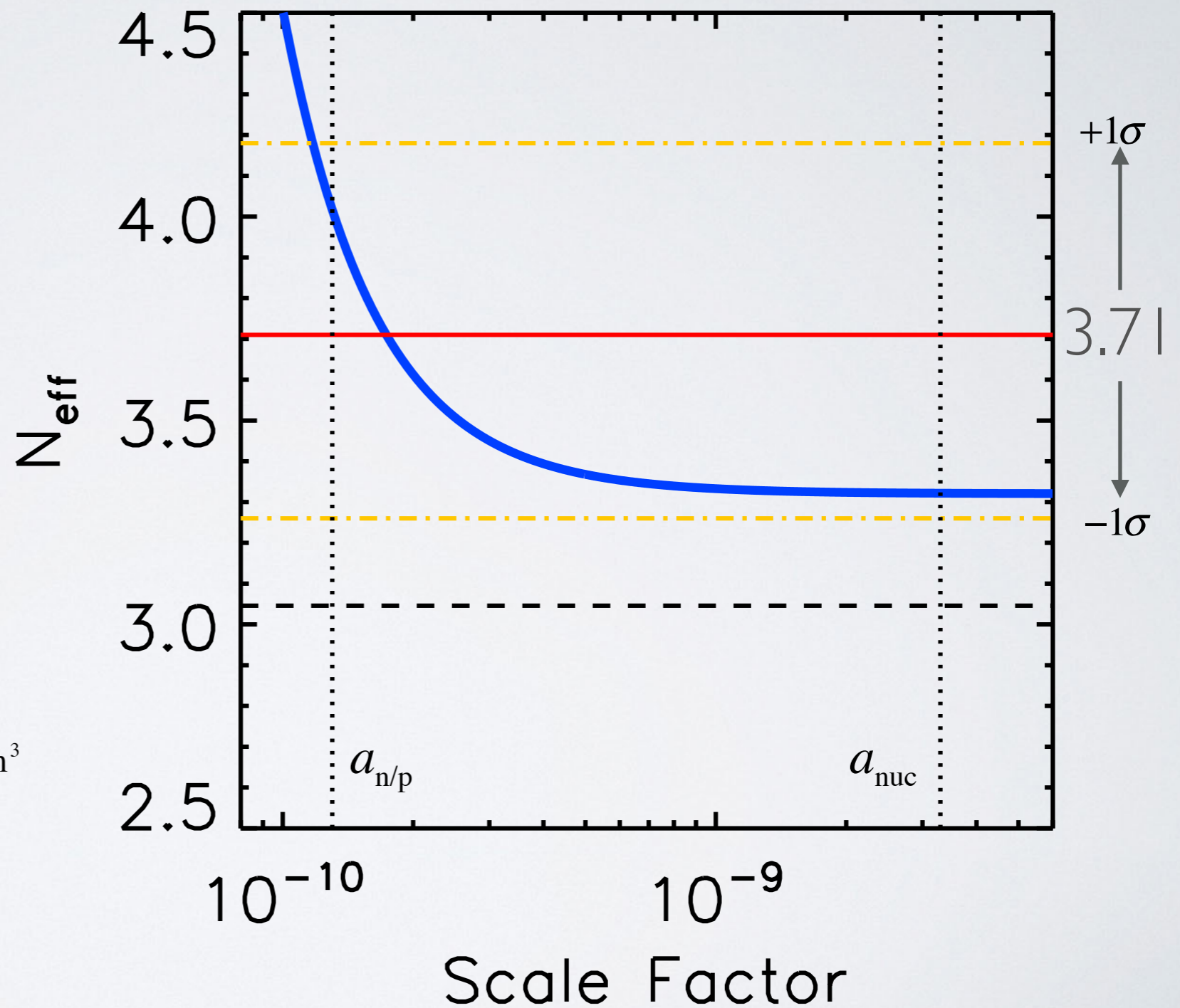
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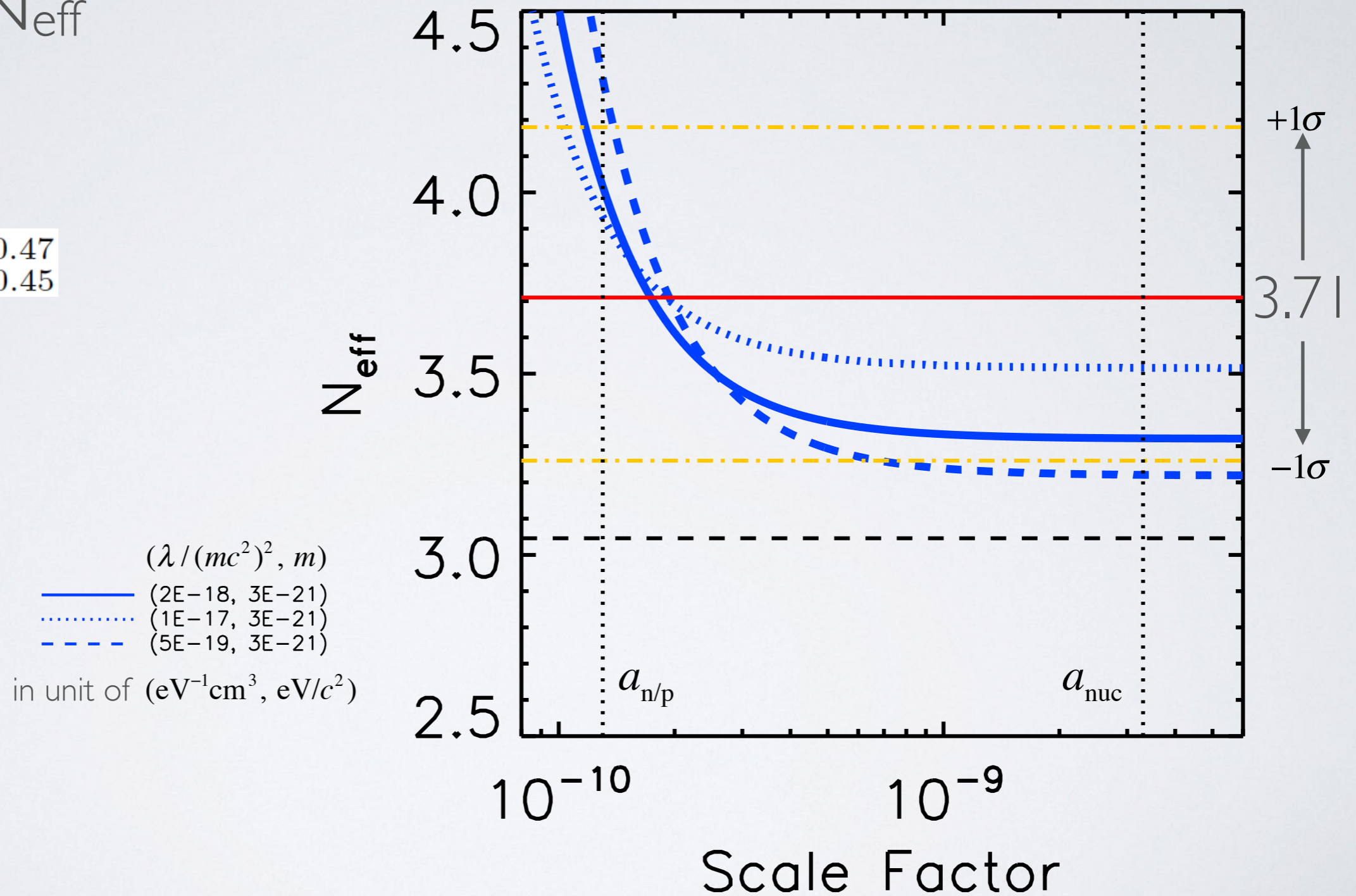
$$m = 3 \times 10^{-21} \text{ eV} / c^2$$



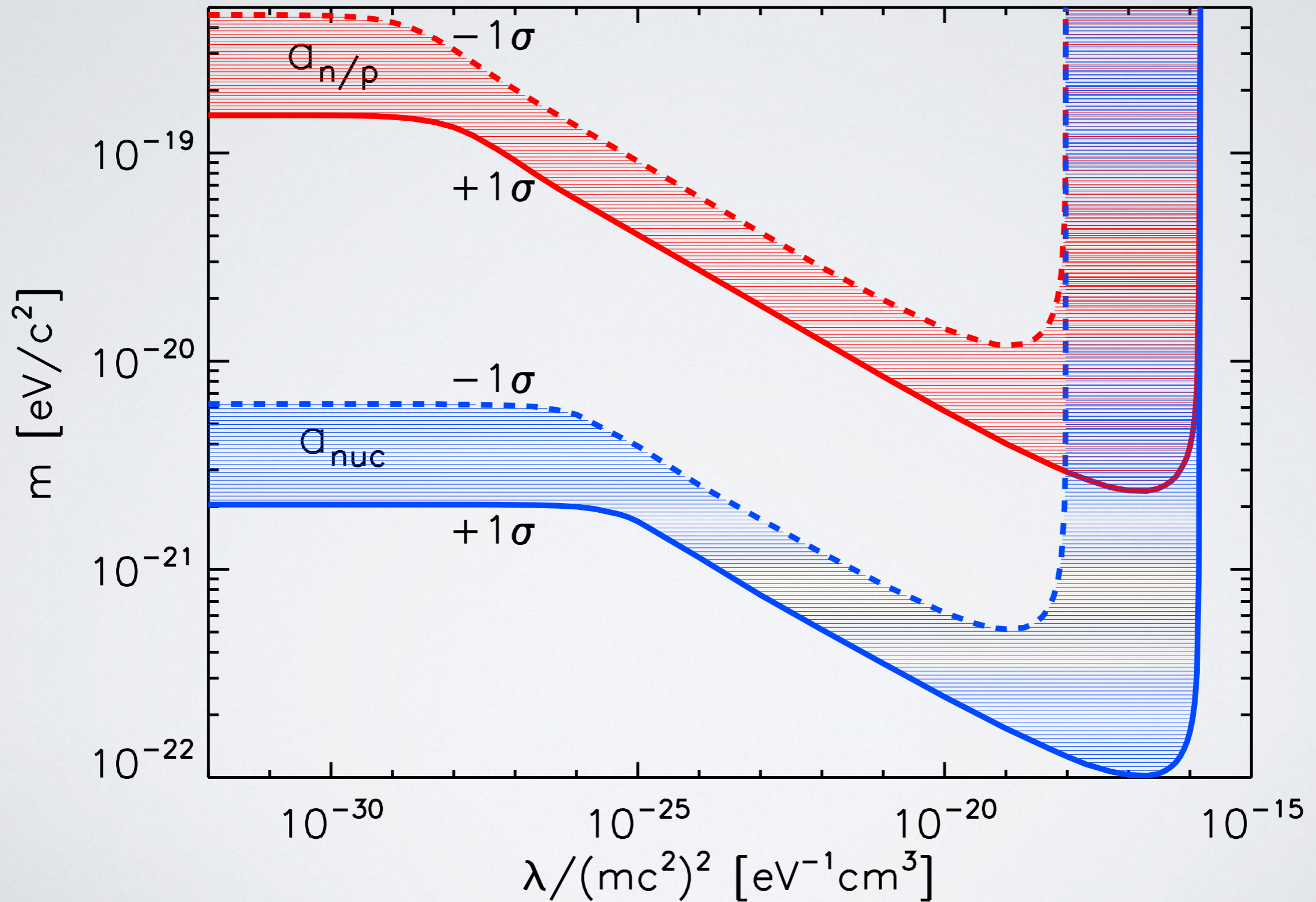
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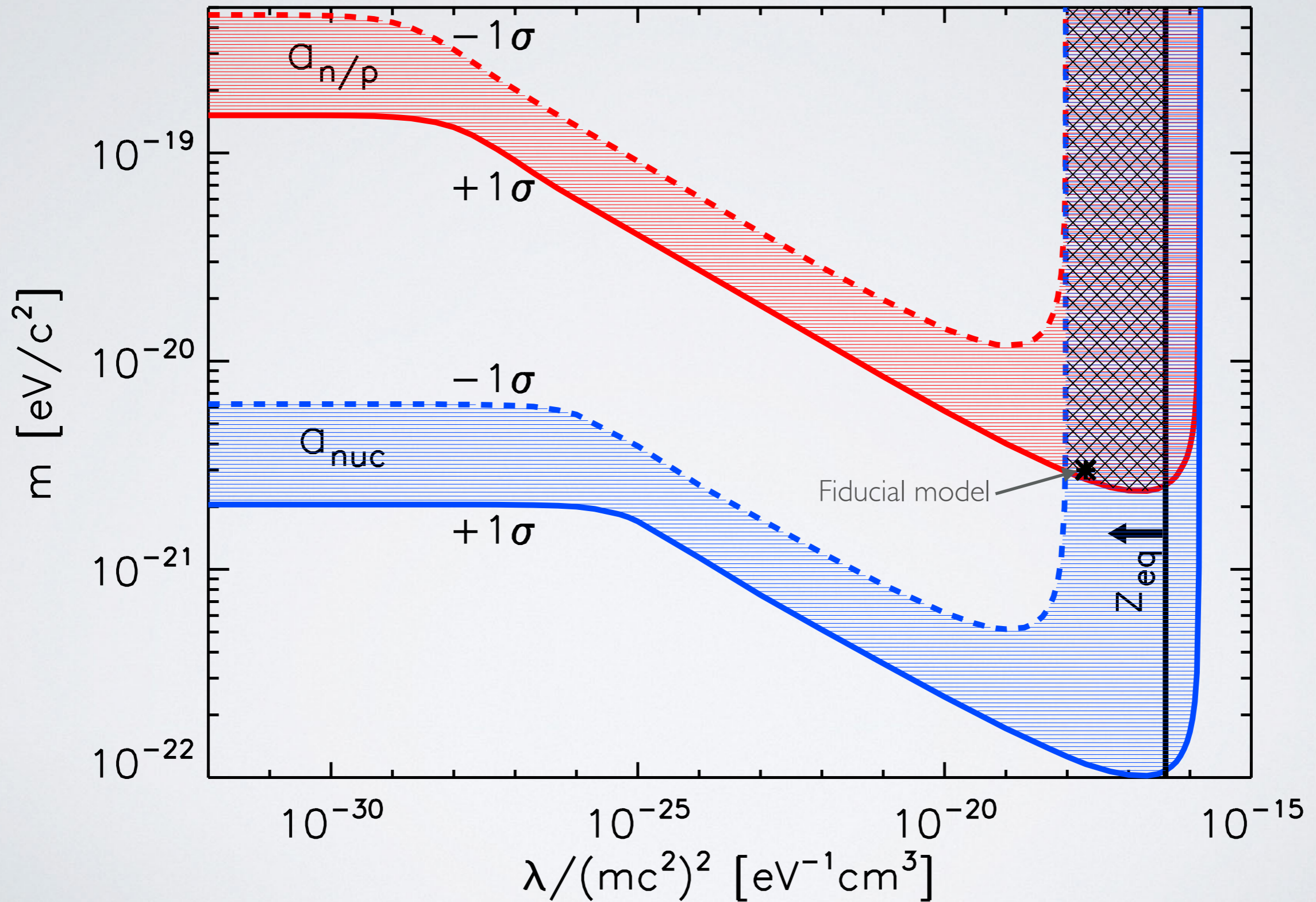
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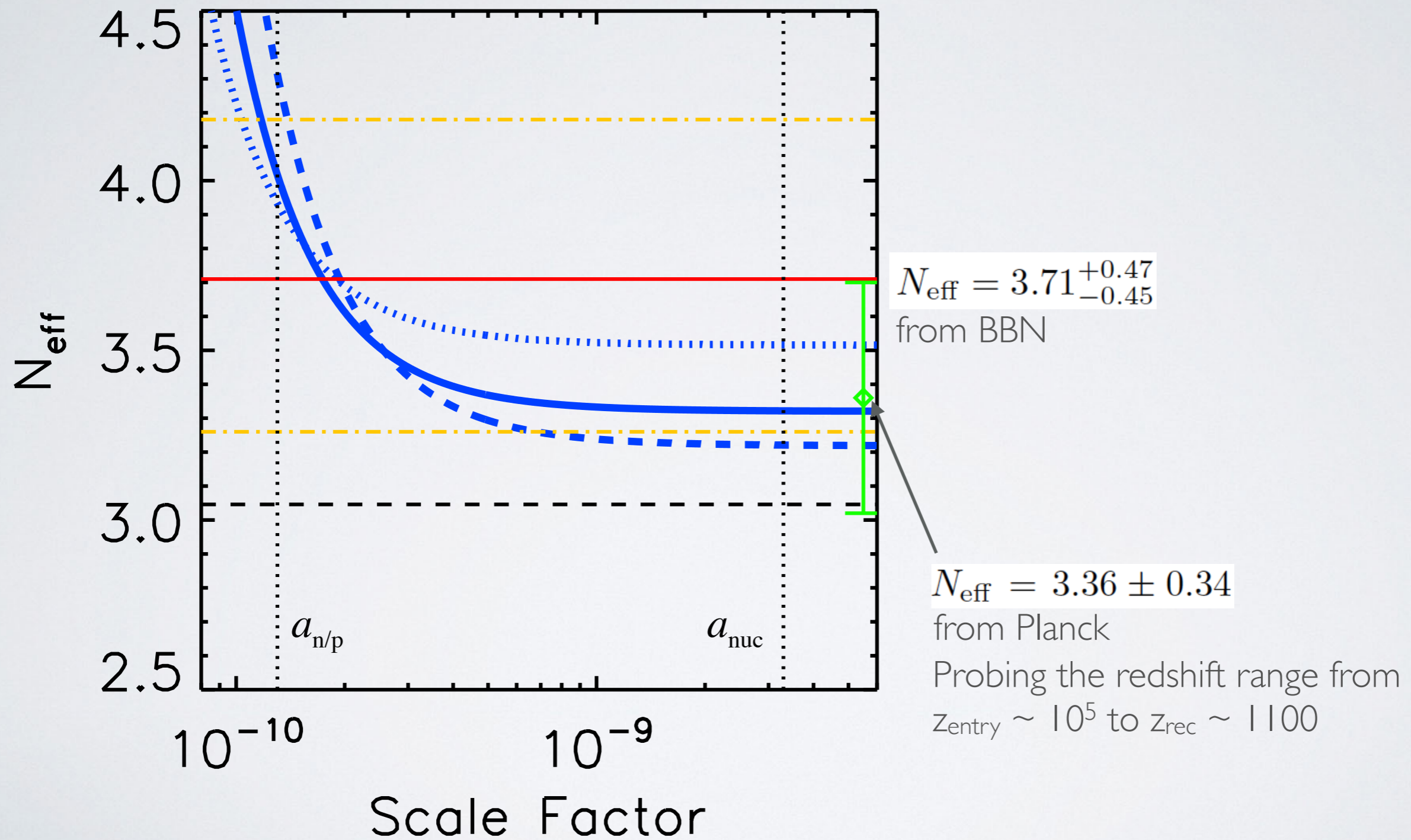
RESULT: PARTICLE PARAMETER SPACE



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N_{eff} FROM BBN VS. N_{eff} FROM CMB



FUTURE WORK

- Find the exact constraint on the SFDM particle parameters from N_{eff} during BBN, by calculating primordial abundances of the light elements using a BBN code
- Calculate the growth of structures with SFDM
 - Linear: mass function, power spectrum, CMB
 - Non-linear: halo formation