



Neutron Star EOS Constraints from Pulsed X-ray Emission

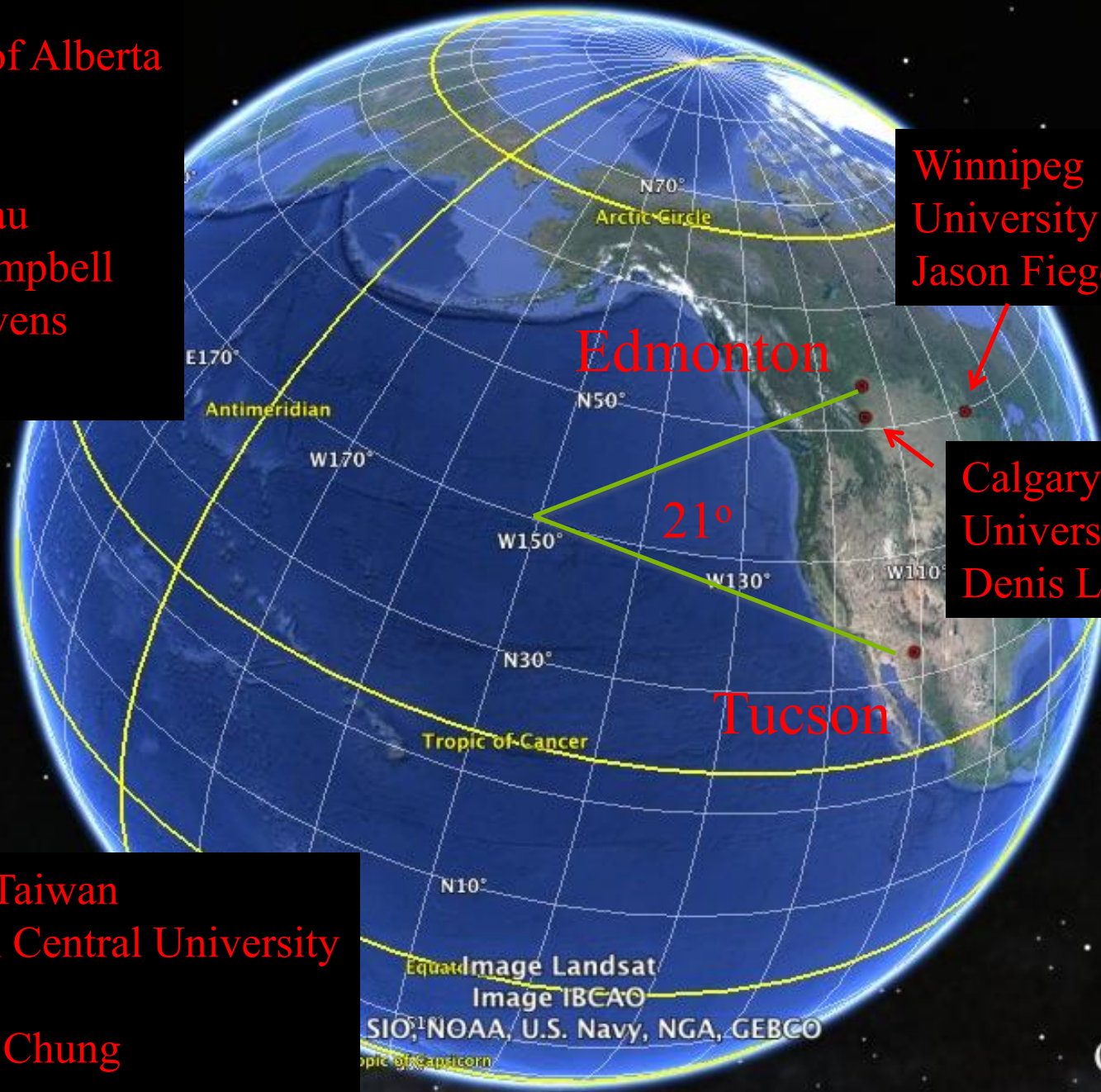
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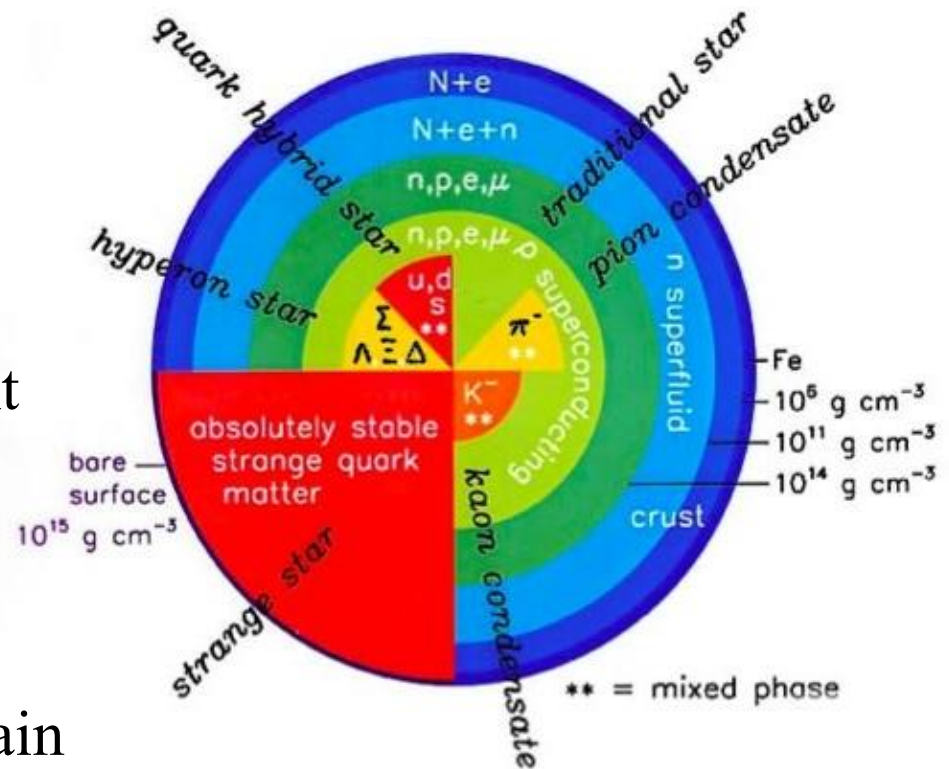
Edmonton

21°

Tucson

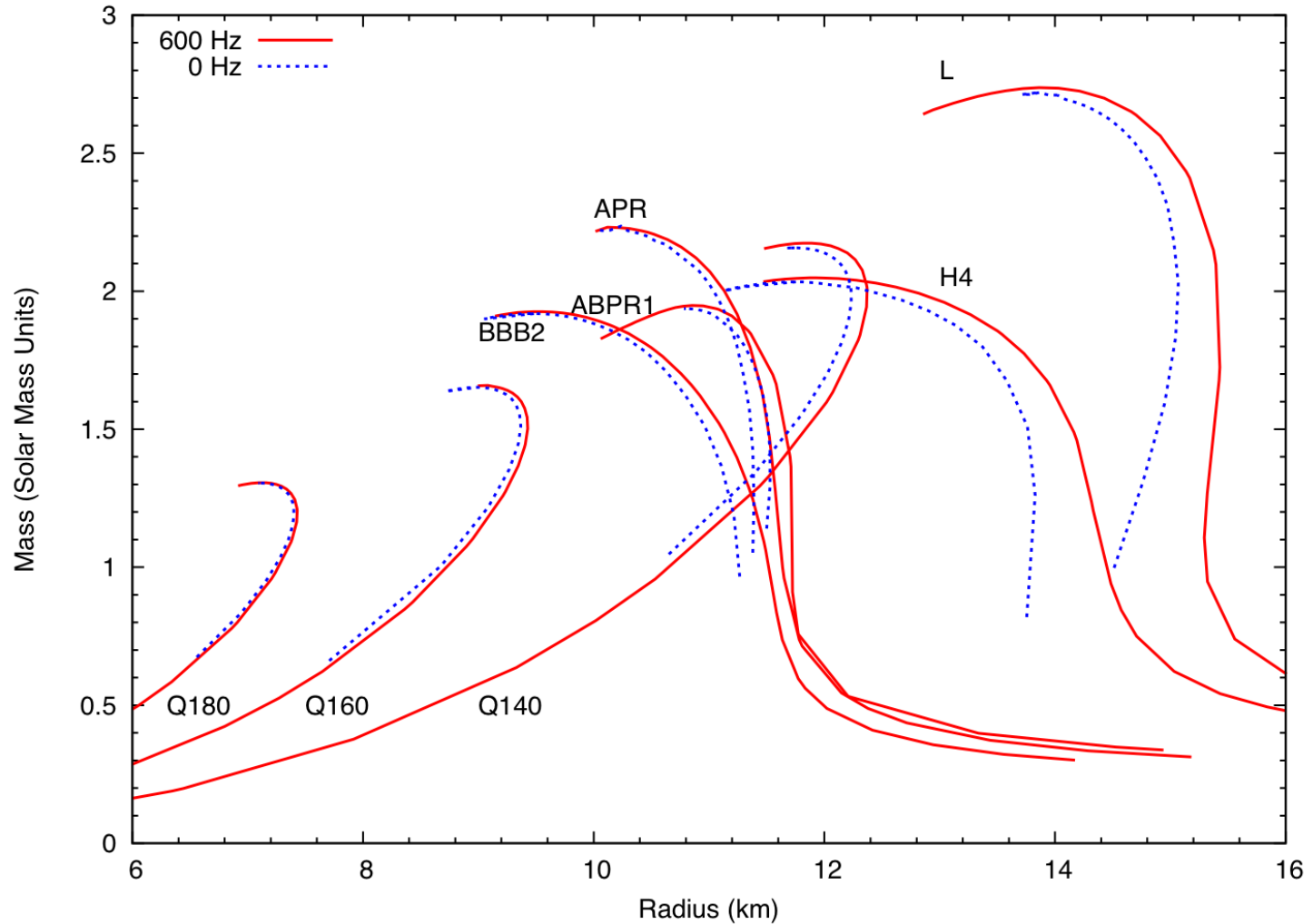
Neutron Stars -- More than just neutrons ...

- The behaviour of matter at densities above nuclear density but at low temperature is not well understood.
- Earth-based experiments like the Relativistic Heavy Ion Collider (RHIC) provide information only about the very high T phase
- Different hypotheses include different particle species and phases of matter in the core
- Each of the possible equations of state (EOS) provides different predictions about the possible masses and radii of NS.
- Major goal of studying NS is to make measurements that constrain the EOS of dense matter.

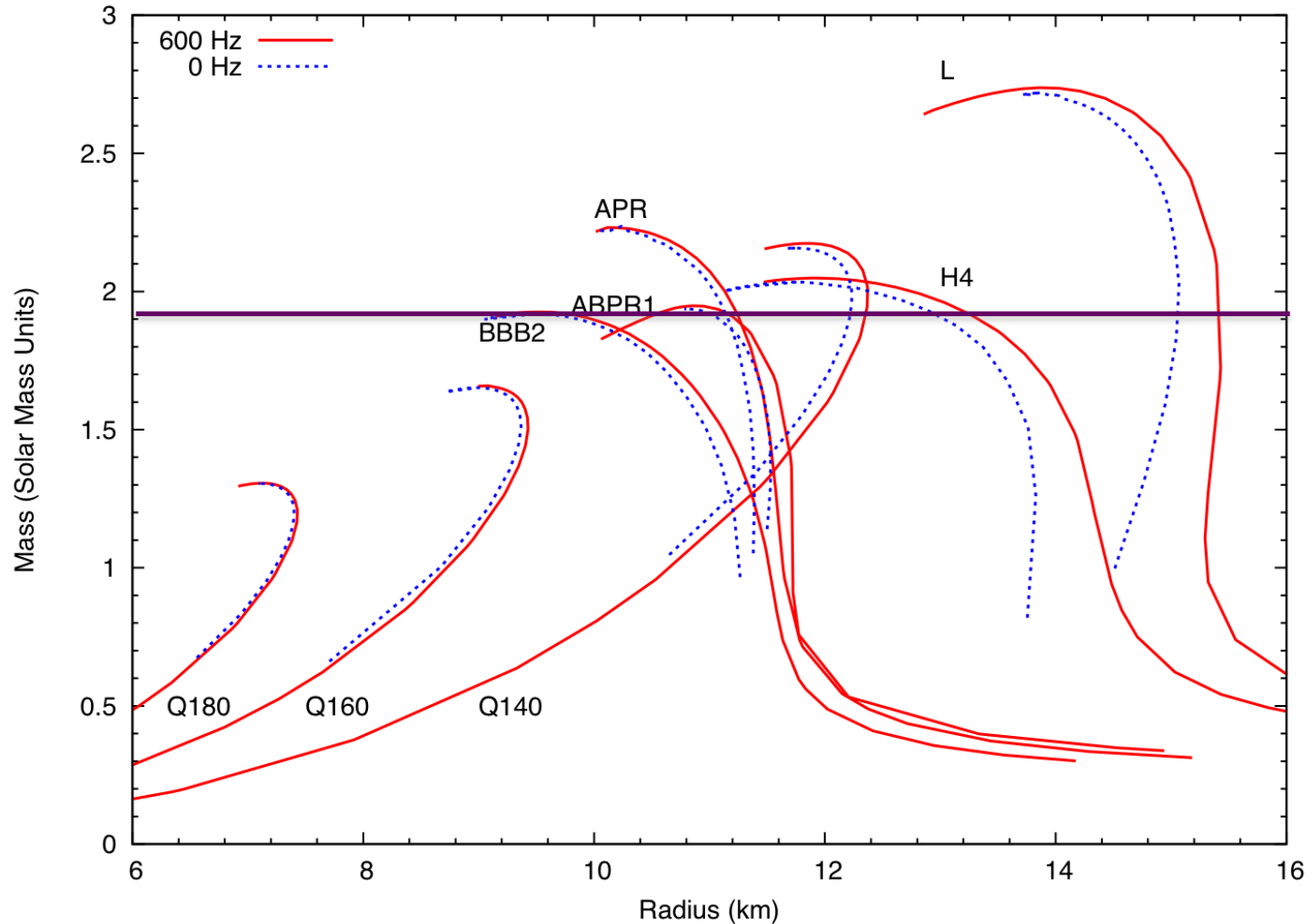


Drawing by James Lattimer

Mass - Radius Curves

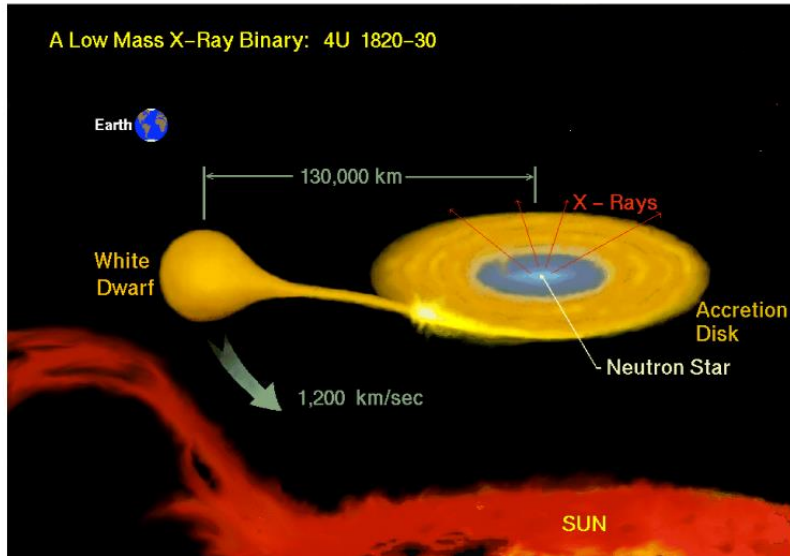


Mass - Radius Curves



Measurement of Shapiro Delay gives $M=1.93 M_{\odot}$ Demorest et al. Nature 2010

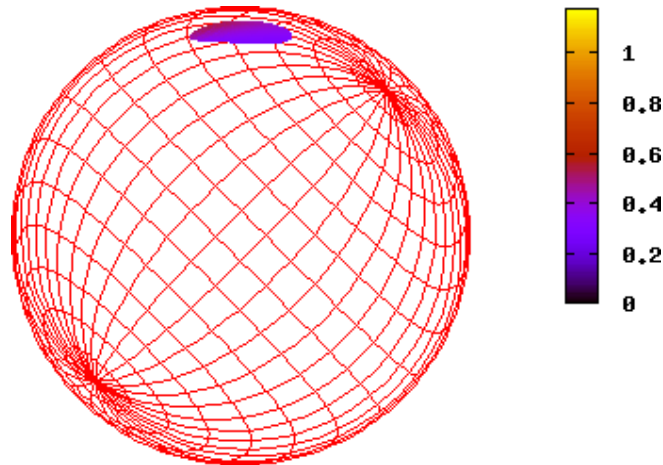
Neutron Stars in LMXB



- An accreting NS has different luminosity states: quiescence or outburst
- Quiescence – Little or no accretion, flux mainly from NS surface
- Outburst – heavy accretion
- Accretion powered pulsations sometimes seen
- X-ray Bursts sometimes seen
- Pulsations and X-ray Bursts are flux originating from the NS surface

Rotating Hot Spots

- Rotation Powered X-ray pulsars - no accretion, x-ray emission dominated by emission from the surface (not light cylinder). Eg: Bogdanov ApJ 2013
- Accretion Powered Pulsars – pulsations from hot spot
- X-ray Bursts – oscillations at the spin frequency observed
- A “hot spot” on the NS surface is most likely the source for the periodic flux from these sources



NS Constraints from Rotating Hot Spots

- Find neutron stars whose light is emitted from the star's surface
- Model the local microphysics of the emitting area
(spot size, shape, emission spectrum and beaming)
- Combine with relativistic raytracing to find which photons reach the telescope to construct light curve
- Light-deflection depends on the ratio GM/Rc^2
- Rotational “Doppler” effects depend on $R\Omega/c$

Forward Problem: Make assumptions about properties of star and emission and compute light curve.

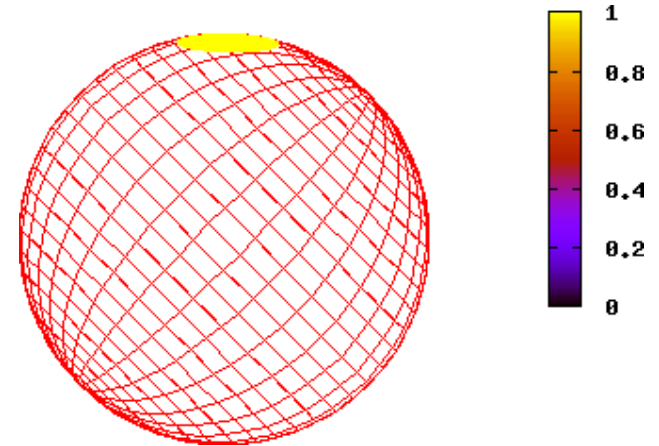
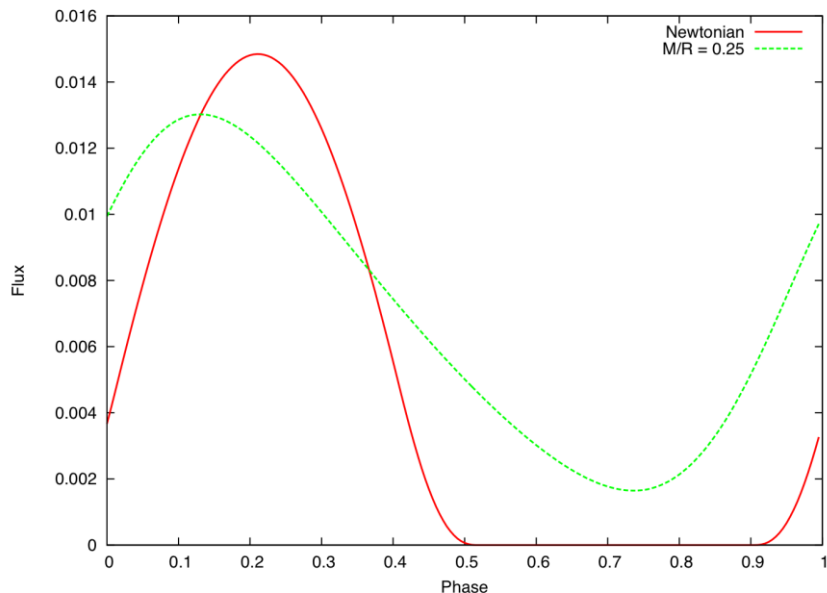
Inverse Problem: Measure light curve and find best fit set of parameters characterizing star and emission properties.

Dependence of Pulse Profiles on M/R

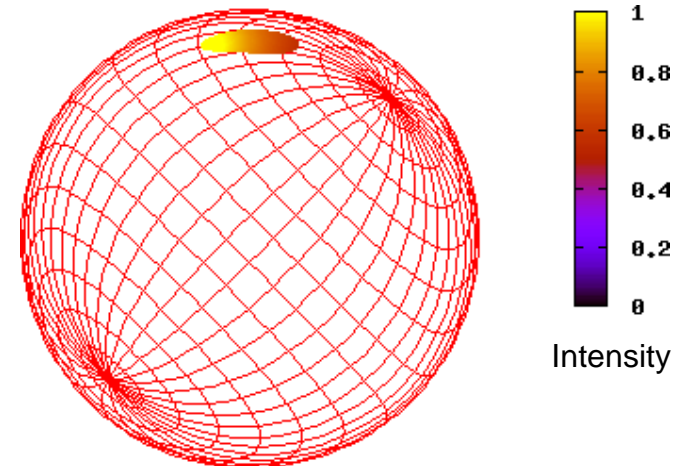
M/R = “compactness” affects how much of the star is visible due to light-bending

- larger M/R \rightarrow less modulation

These effects are independent of the photon's energy.



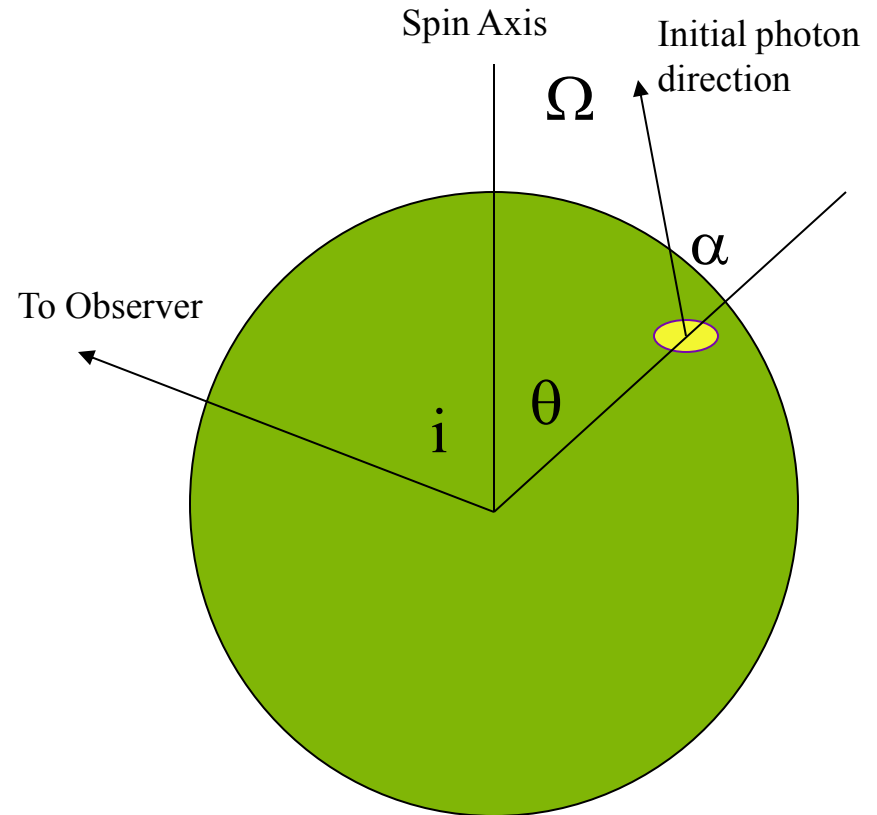
Newtonian Gravity



General Relativity M/R = 0.25

Inclination and emission angle

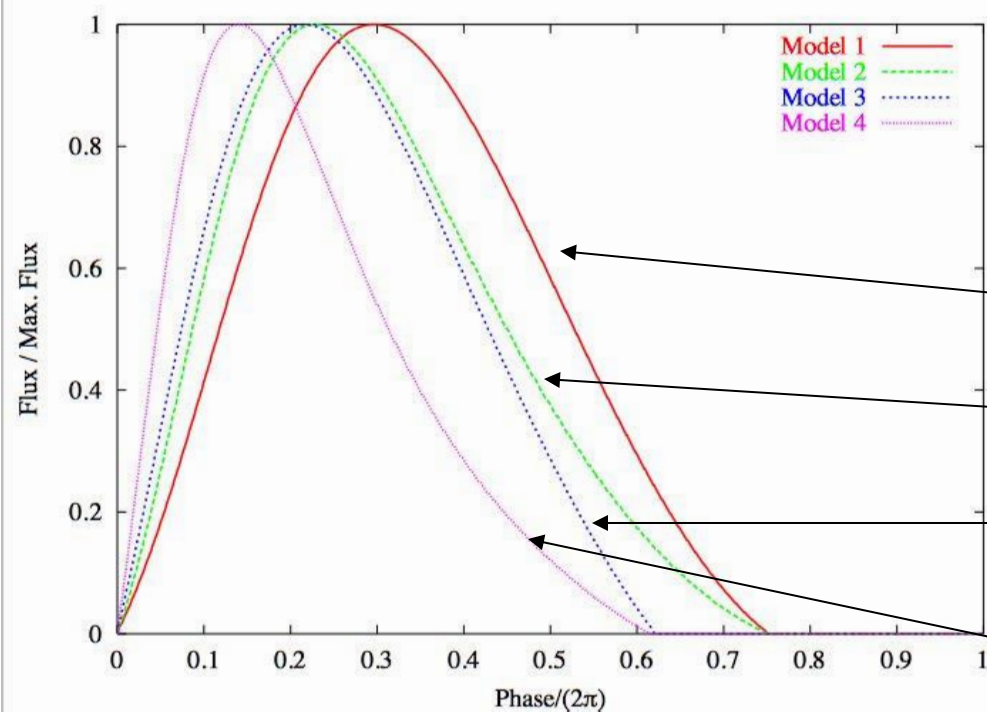
- θ = angle between the hotspot's centre and the spin axis
- i = angle between the observer and the spin axis (orbital and spin angular momenta aligned)
- α = angle between the photon's initial direction and the normal to the surface.
- Small $\sin(i)\sin(\theta)$ low modulation – degeneracy with M/R



Dependence of Pulse Profiles on Speed

$R \Omega \sin\theta \sin i (1-2M/R)^{-1/2} = \text{speed}$ affects asymmetries between rise and fall times

- larger speed \rightarrow larger time asymmetries
- Degeneracy between R and $\sin\theta \sin i$



Pulse Shapes for $1.4 M_{\odot}$ Stars
Isotropic + Equatorial Emission

$R=9.6 \text{ km}$ Spin=300 Hz $v=0.08 c$

$R=9.8 \text{ km}$ Spin=600 Hz $v=0.16 c$

$R=15.1 \text{ km}$ Spin=300 Hz $v=0.11c$

$R=16.4 \text{ km}$ Spin=600 Hz $v=0.24 c$

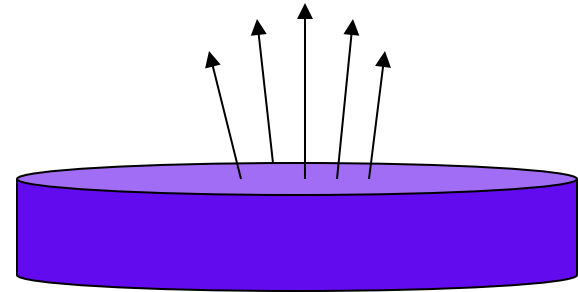
Anisotropic Emission

Beaming affects:

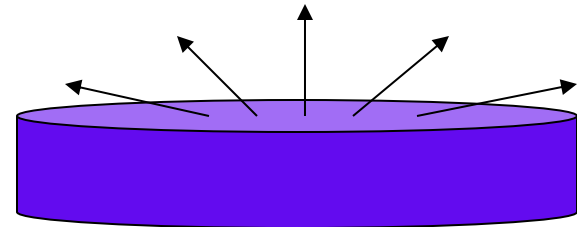
- modulation: anti-beaming, (case C) allows the spot to be seen more easily than normal beaming (case A)
- timing asymmetries: peak emission occurs earlier for C than for A
- Pulse shape: double-peaks or flattened peaks possible with C

Accretion Powered Pulsations – Case C
with an unconstrained amount

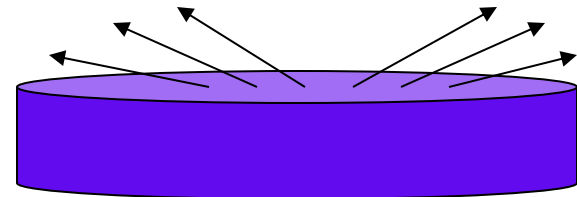
X-ray Burst Oscillations – Case A, fairly
well known limb-darkening



A = Beamed towards the normal



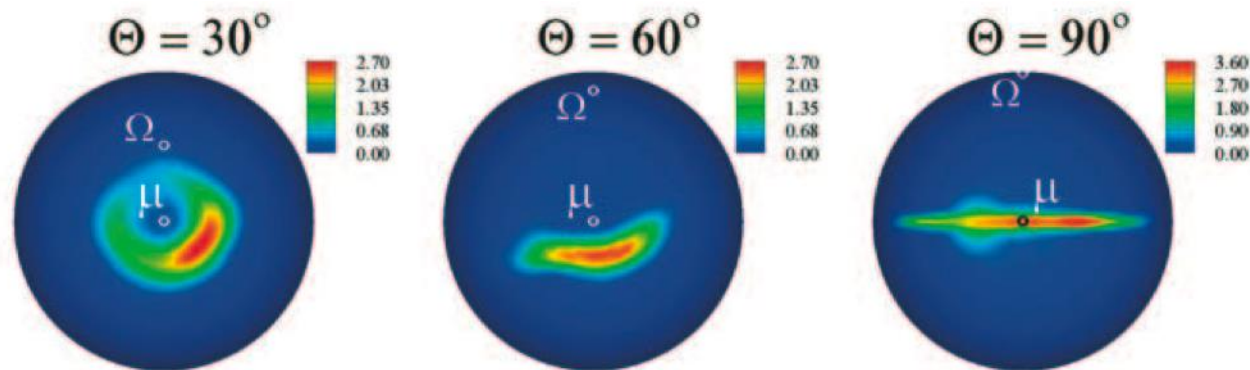
B = Isotropic emission



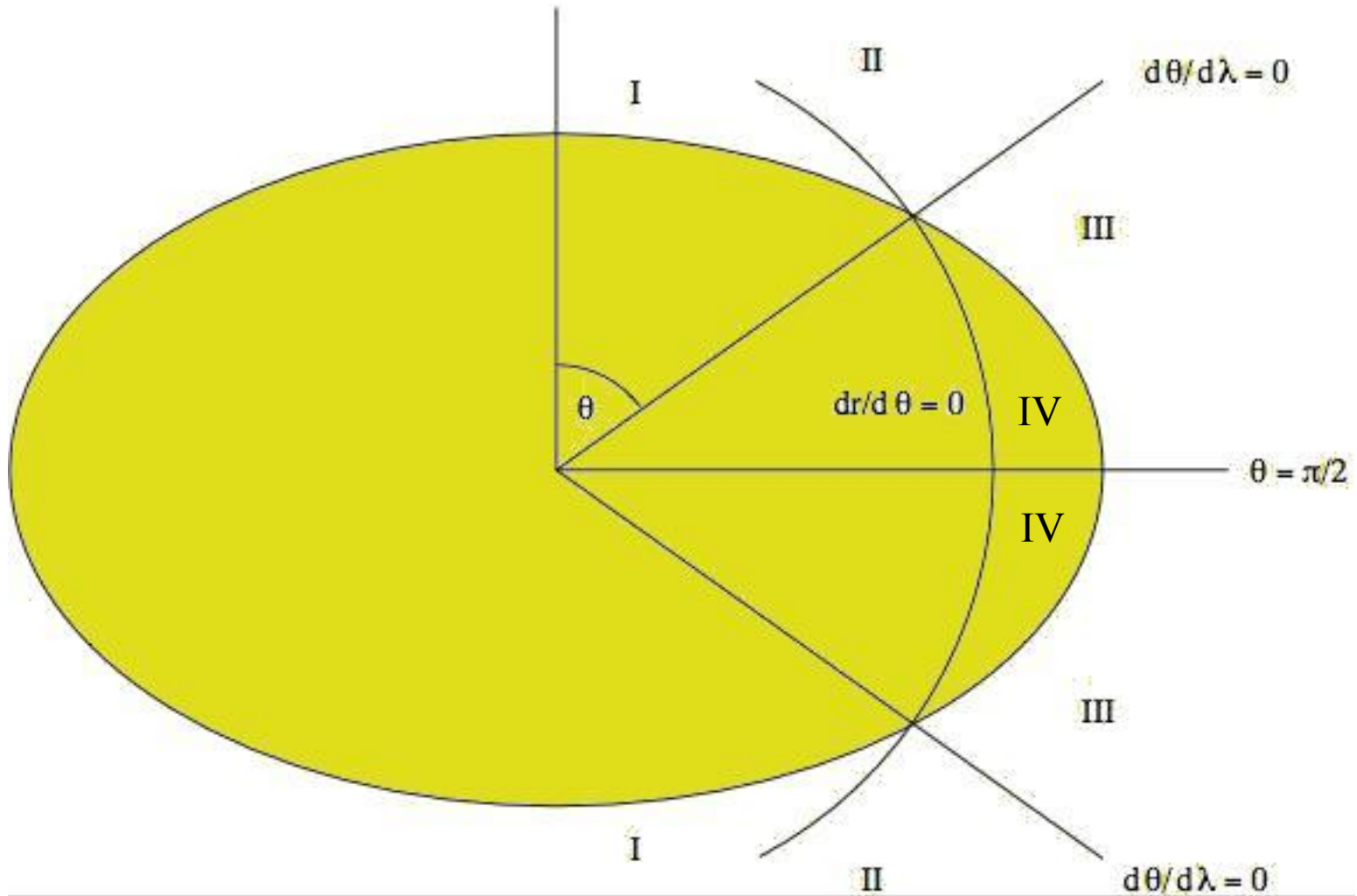
C = Beamed towards the surface

Other complications

- Oblate shape of star
- Scattering by optically thin plasma near star
- Multiple spots may be visible (Ibragimov and Poutanen 2009)
- Spots are not necessarily circles (Kajava et al 2011)
- MHD simulations by Kulkarni, Romanova & Lovelace
- Accretion onto a rapidly rotating magnetic NS
- Complicated spot shapes result



Stellar Oblateness



Cadeau, Morsink, Leahy & Campbell 2007 ApJ

Morsink, Leahy, Cadeau & Braga 2007 ApJ

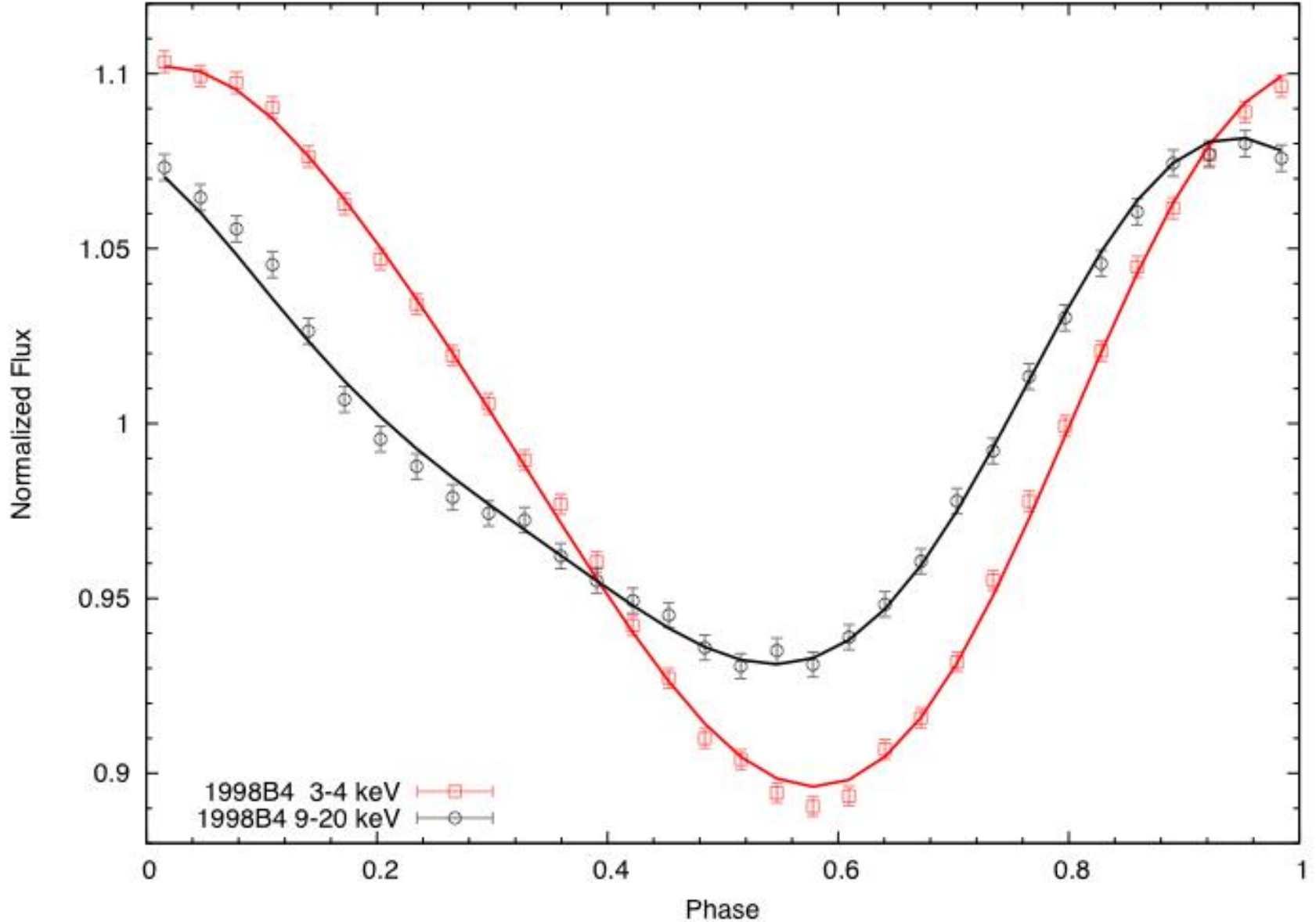
X-ray Telescopes

- RXTE (1996 – 2012) X-ray timing
- Chandra and XMM – mainly spectroscopy and imaging, some timing capabilities
- NICER = Neutron Star Interior Composition Explorer, new instrument on ISS, approved for launch in 2016
- ATHENA: spectroscopy, imaging and timing; if approved launch 2028 (ESA)
- Proposed Missions (ESA)
 - LOFT: Large Observatory For X-ray Timing; if approved launch 2024

Constraints from Accreting ms-Period Pulsars

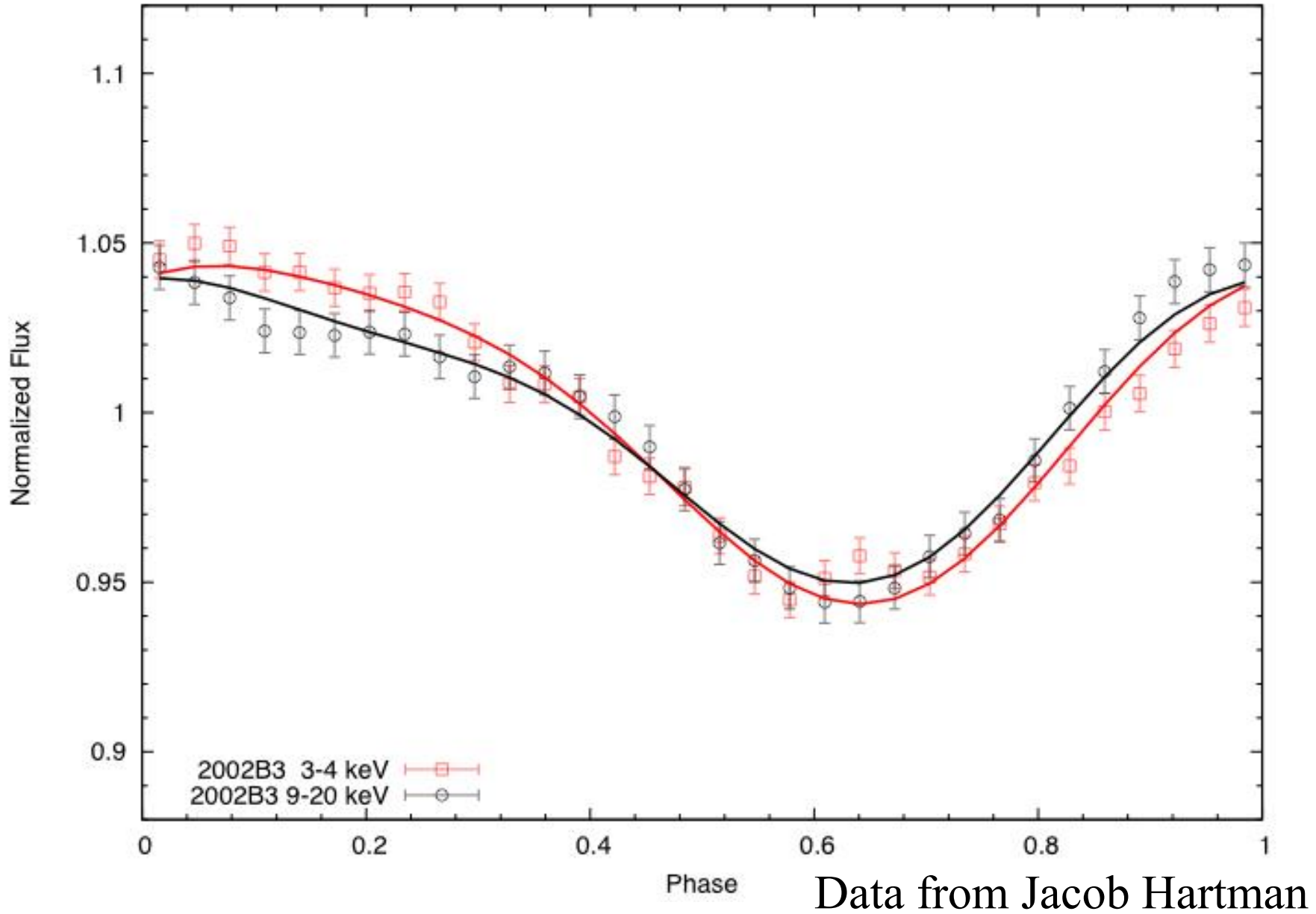
- Models include oblate shape, time delays
- Unknown inclination angle, mass, radius
- Different pulse shapes in different time periods: allow for changes in spot location and spectrum, keep i , M , R fixed
- Free parameter describing anisotropy and freedom in choosing spectral model dominate precision
- Leahy, Morsink & Chou, ApJ 2011
- Morsink & Leahy, ApJ 2011
- Leahy, Morsink, Chung, & Chou, ApJ 2009

SAX J1808 1998 Outburst (Box 4)



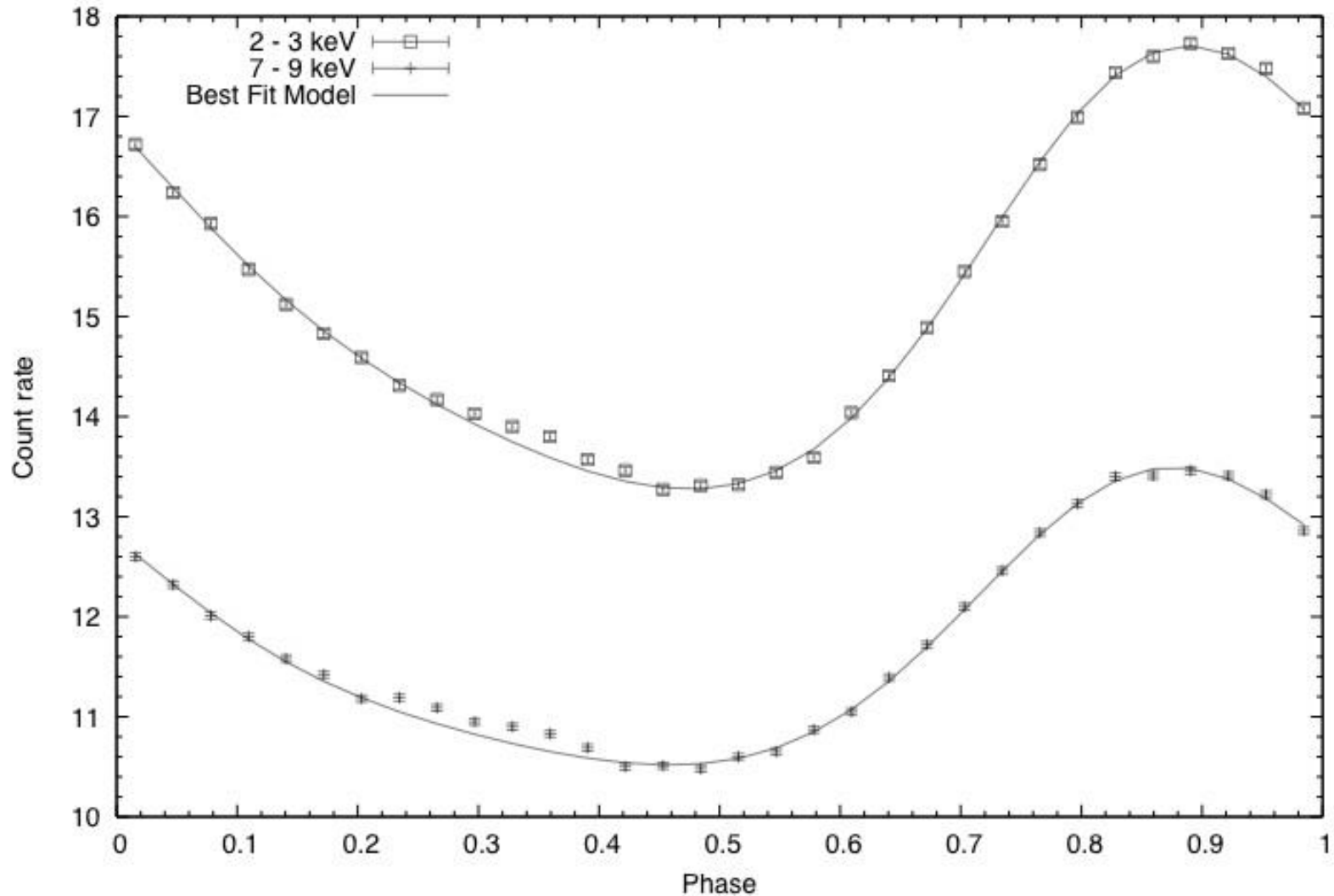
RXTE Data from Jacob Hartman

SAX J1808 2002 Outburst (Box 3)



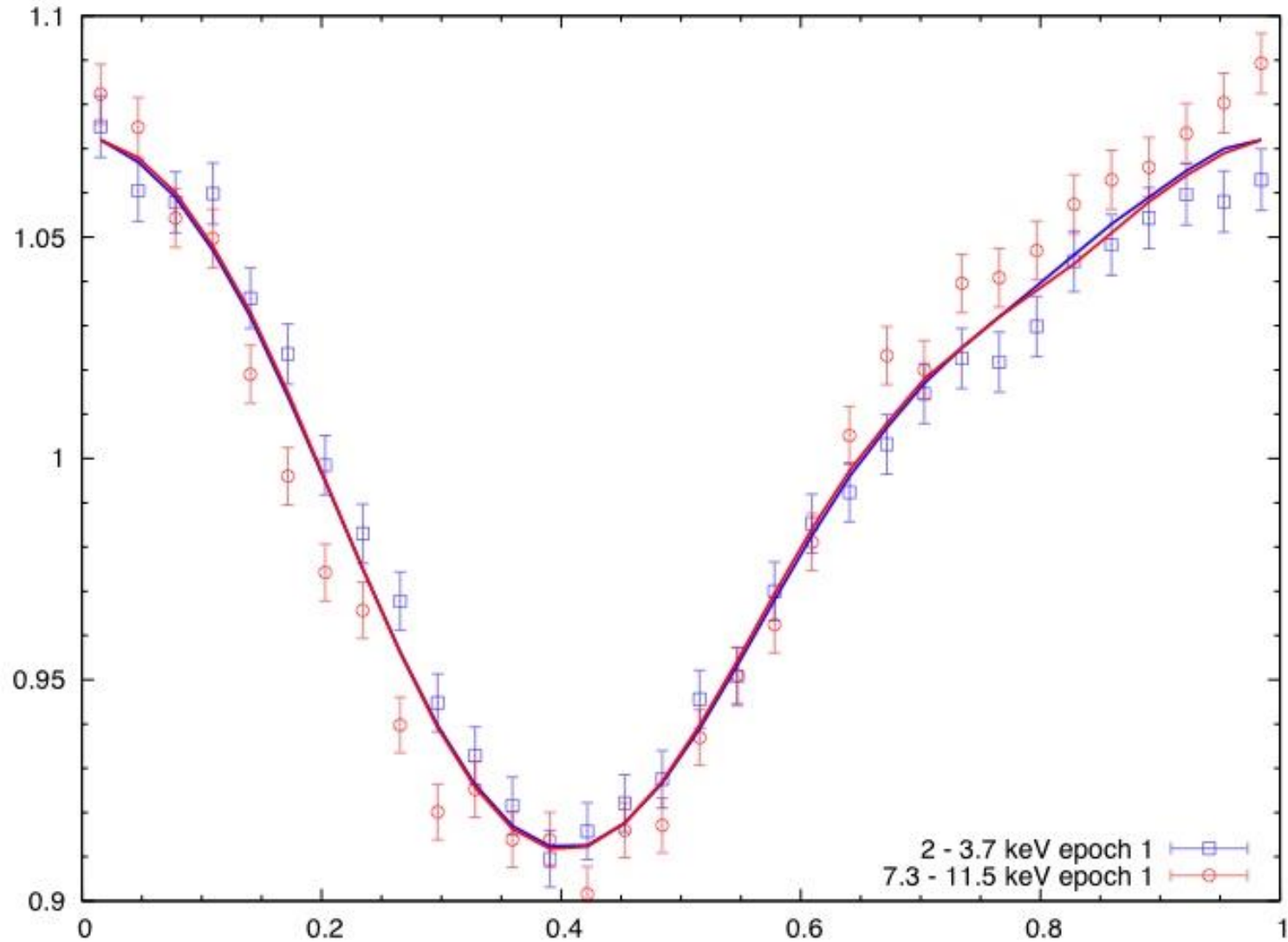
XTE J1814

Combined Data from All Days - 2 Energy Bands

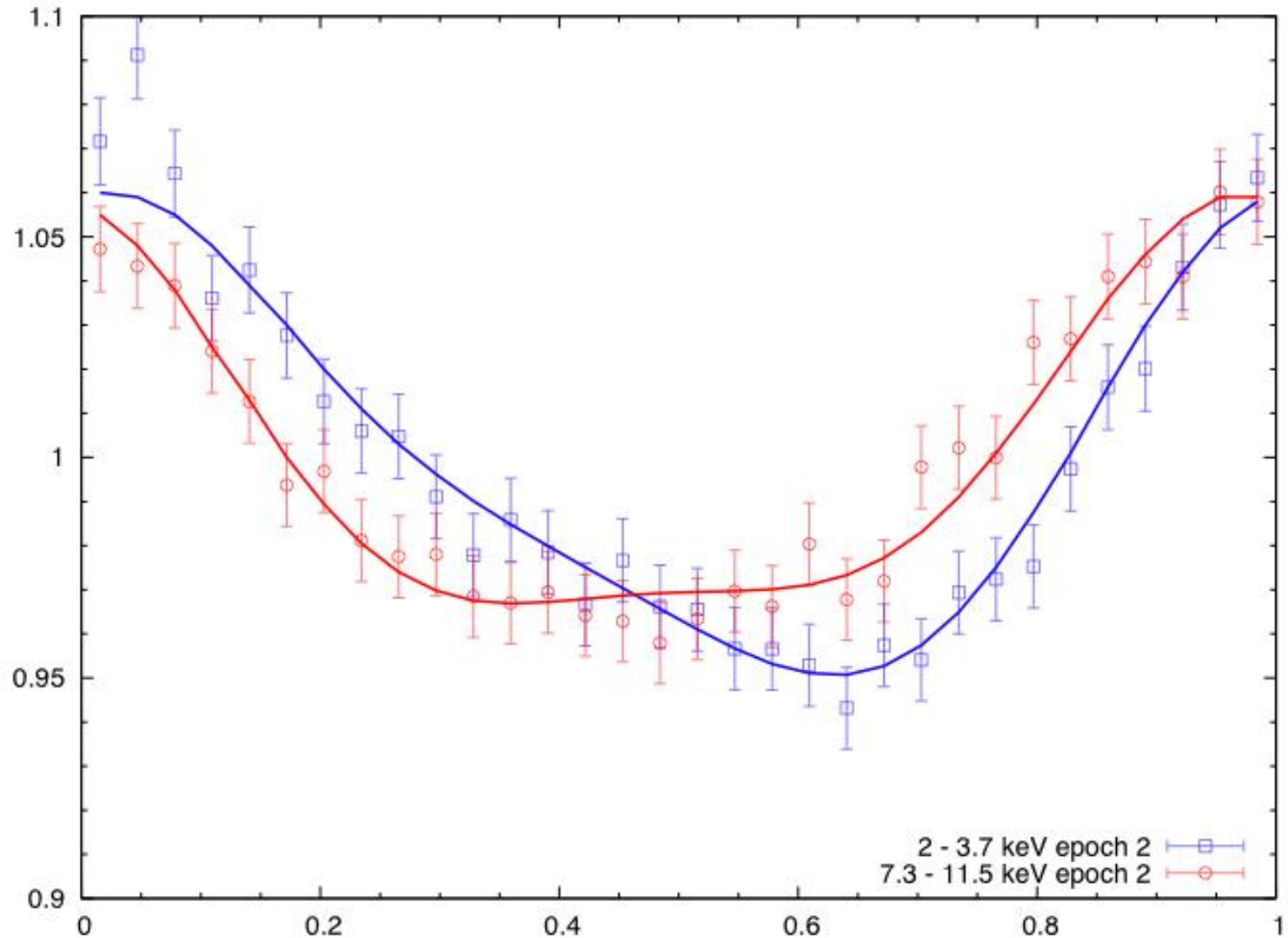


Evidence for an antipodal spot visible part of the time.

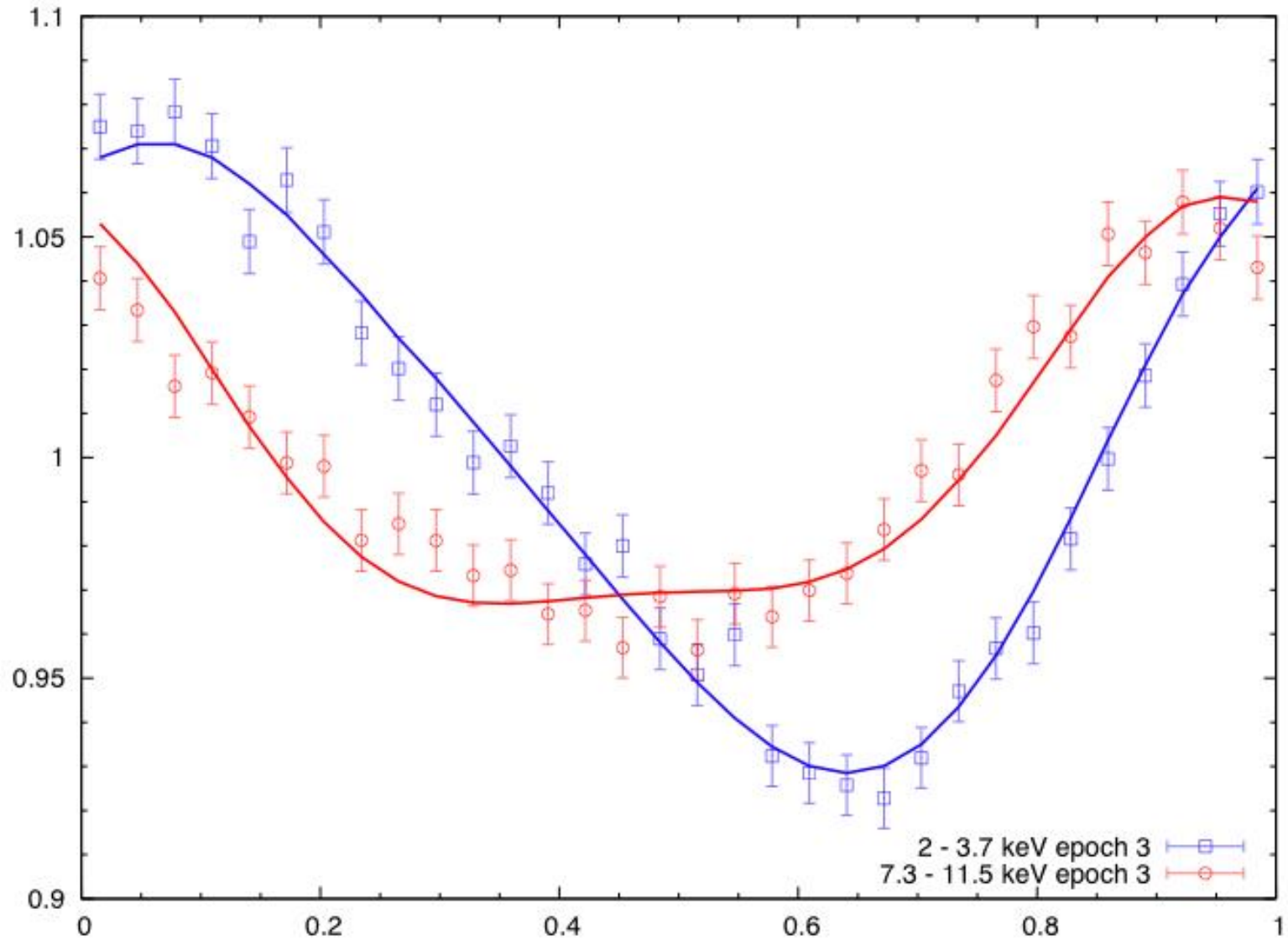
XTE J1807 Epoch 1



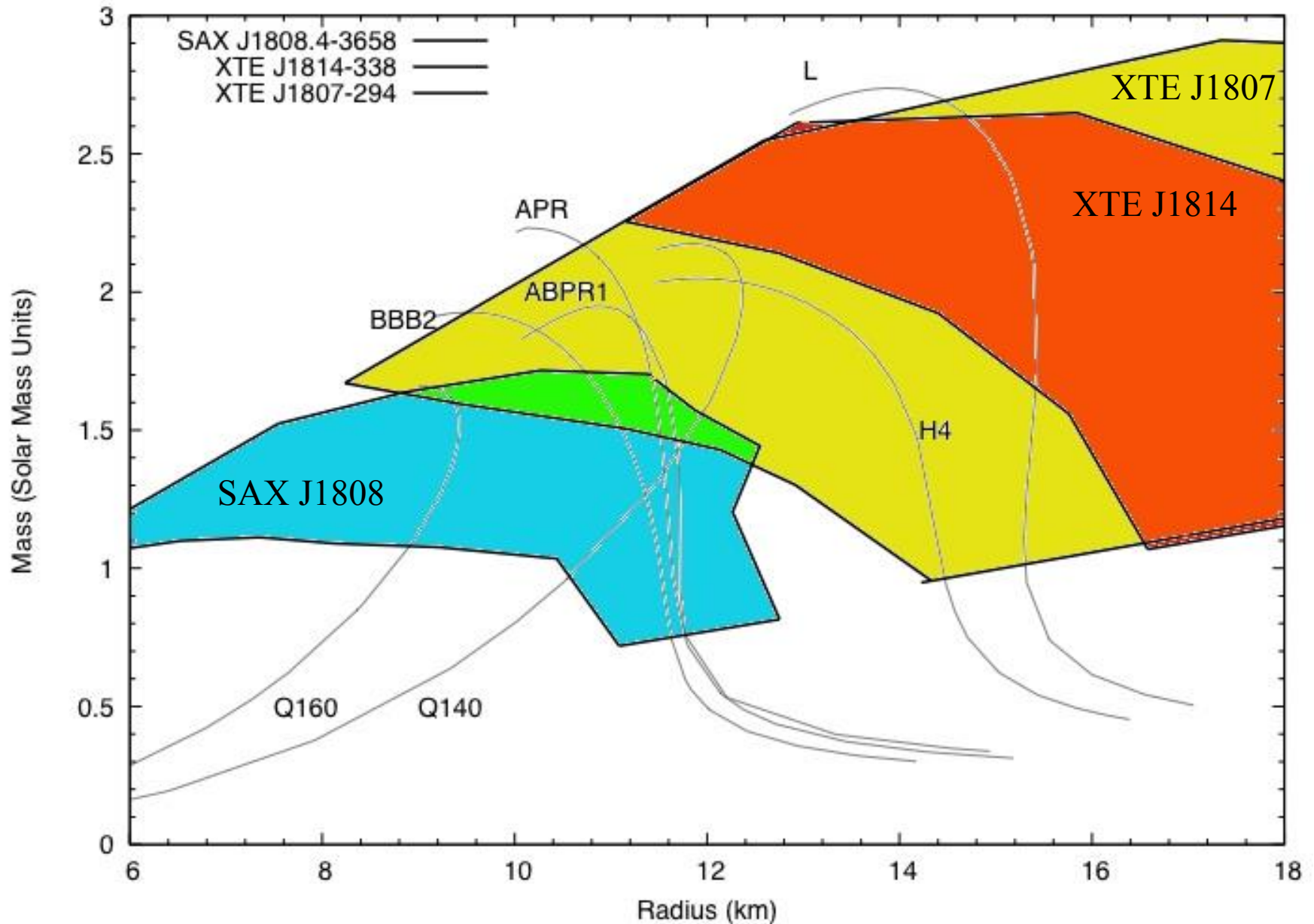
XTE J1807 Epoch 2



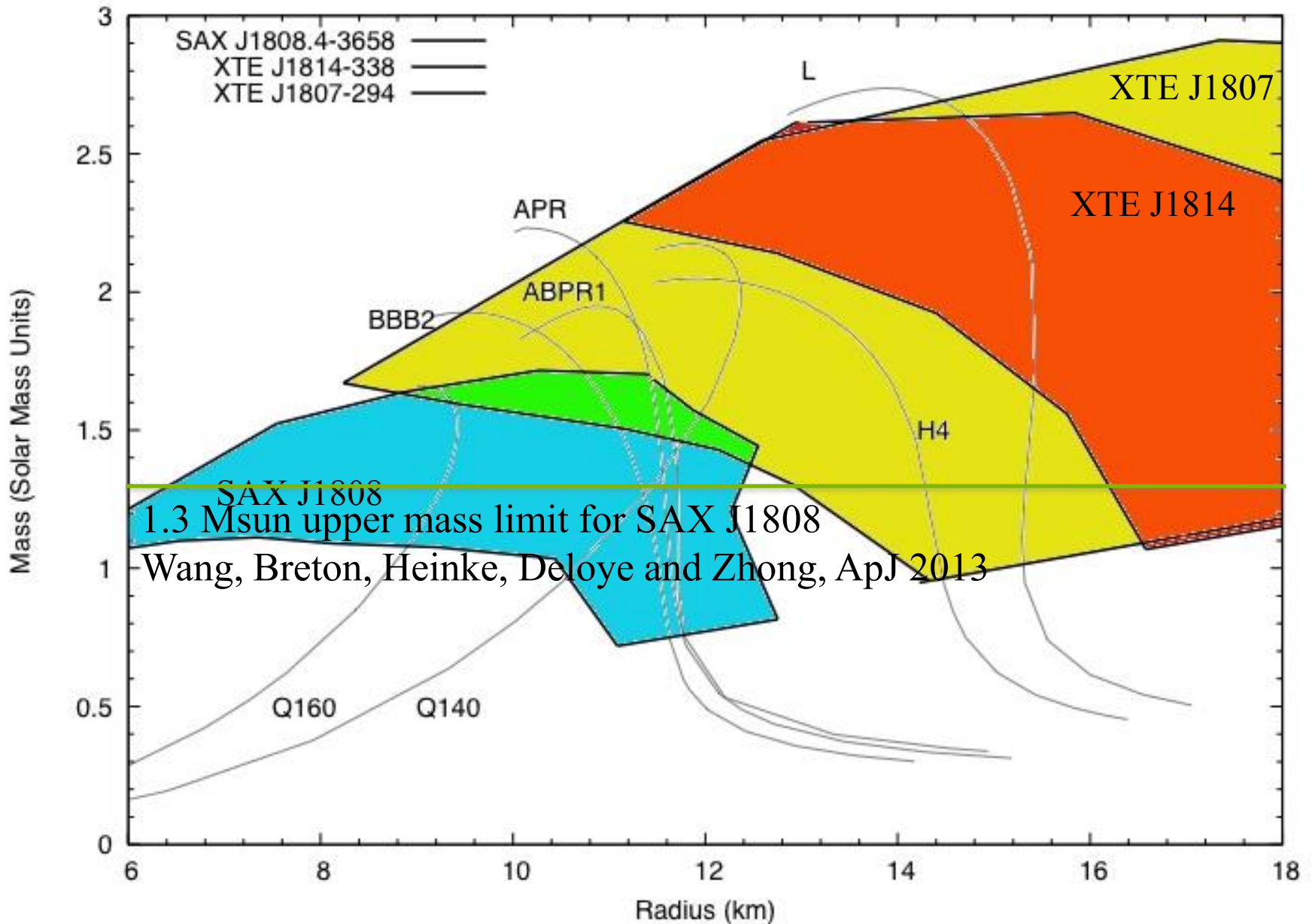
XTE J1807 Epoch 3



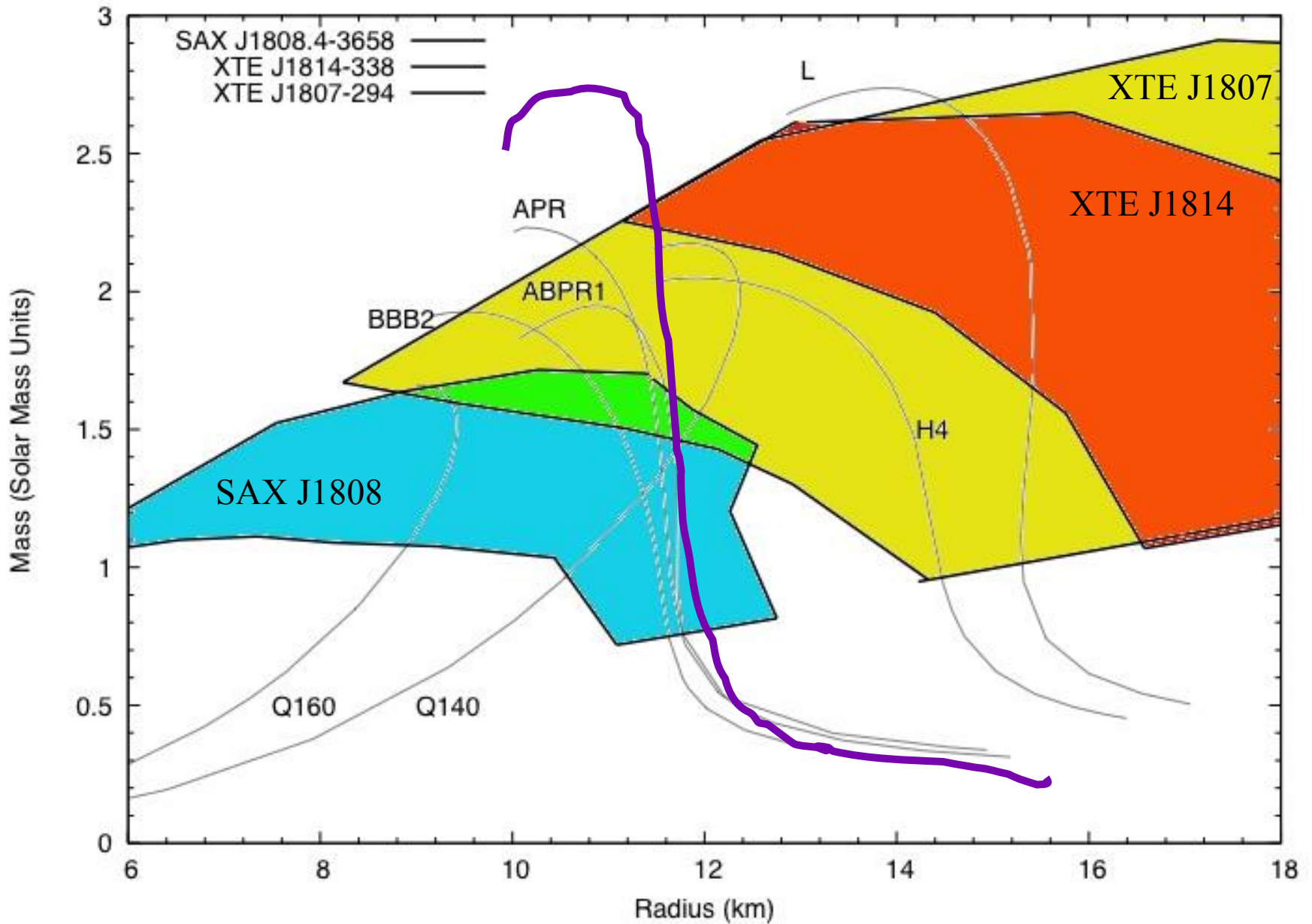
Constraints from 3 stars (3 sigma)



Constraints from 3 stars (3 sigma)



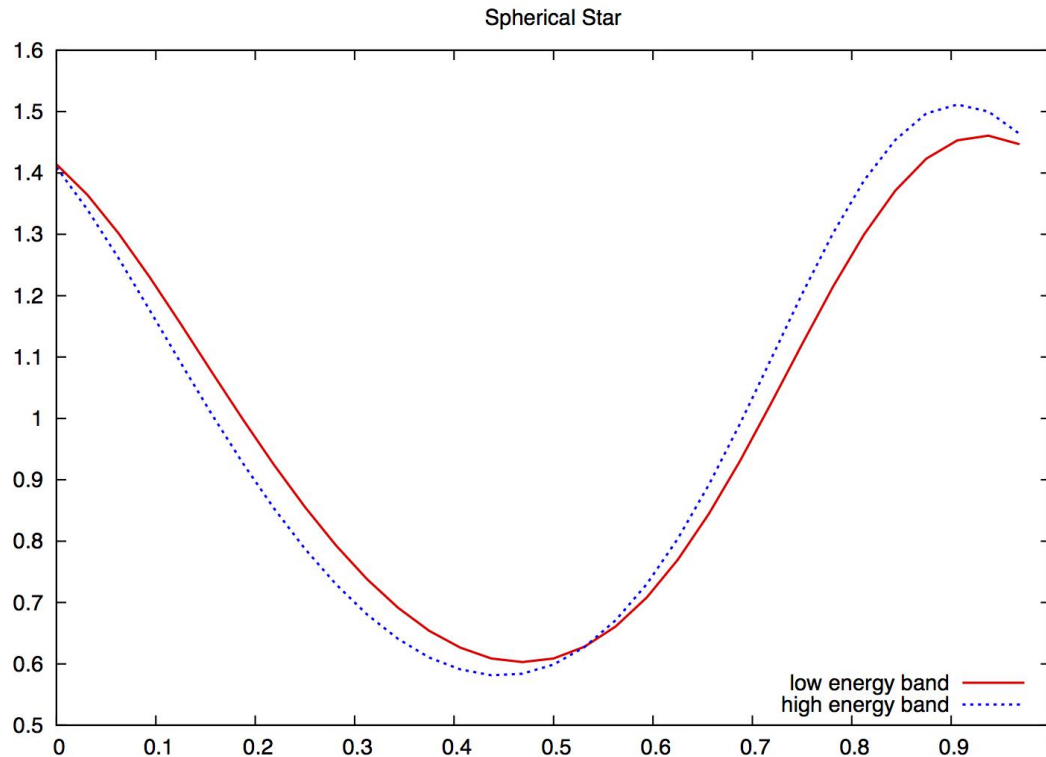
An Allowed EOS?



X-ray Bursts

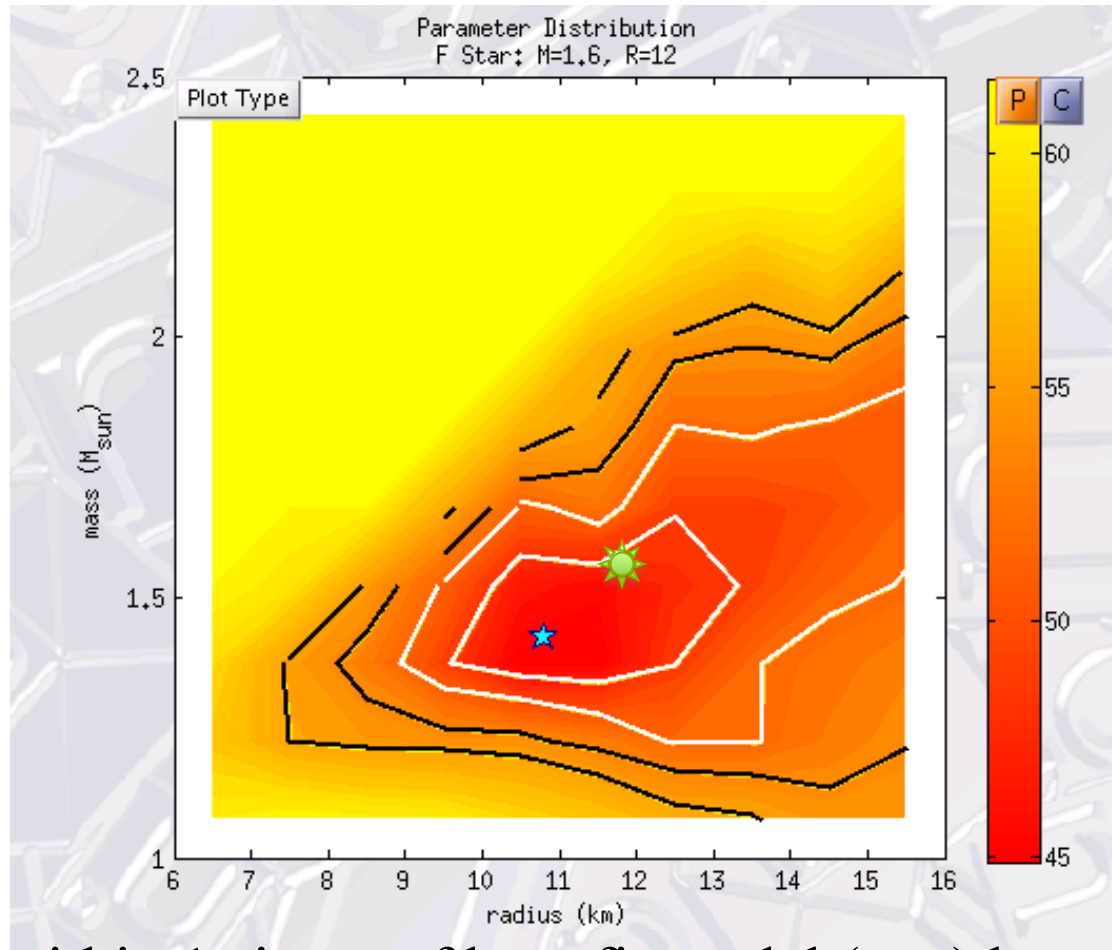
- X-ray burst spectrum is well modeled by a limb-darkened blackbody
- Fewer free parameters may allow for better constraints
- Small subset of LMXB NS have both accretion powered pulsations, and pulsations during X-ray bursts!
- Current collaboration with Jason Fiege (U of Manitoba) making use of genetic algorithms for fitting, Abigail Stevens (MSc U of A) and Denis Leahy (U of Calgary). (See also Lo, Miller, Bhattacharyya & Lamb 2013, Psaltis, Ozel & Chakrabarty 2013)
- How precise and accurate can we determine M and R?

Theoretical curves for $M=1.6$, $R=12\text{km}$,
spin=600 Hz, $i=60$, $\theta=20$
 $v \sim 0.05 c$



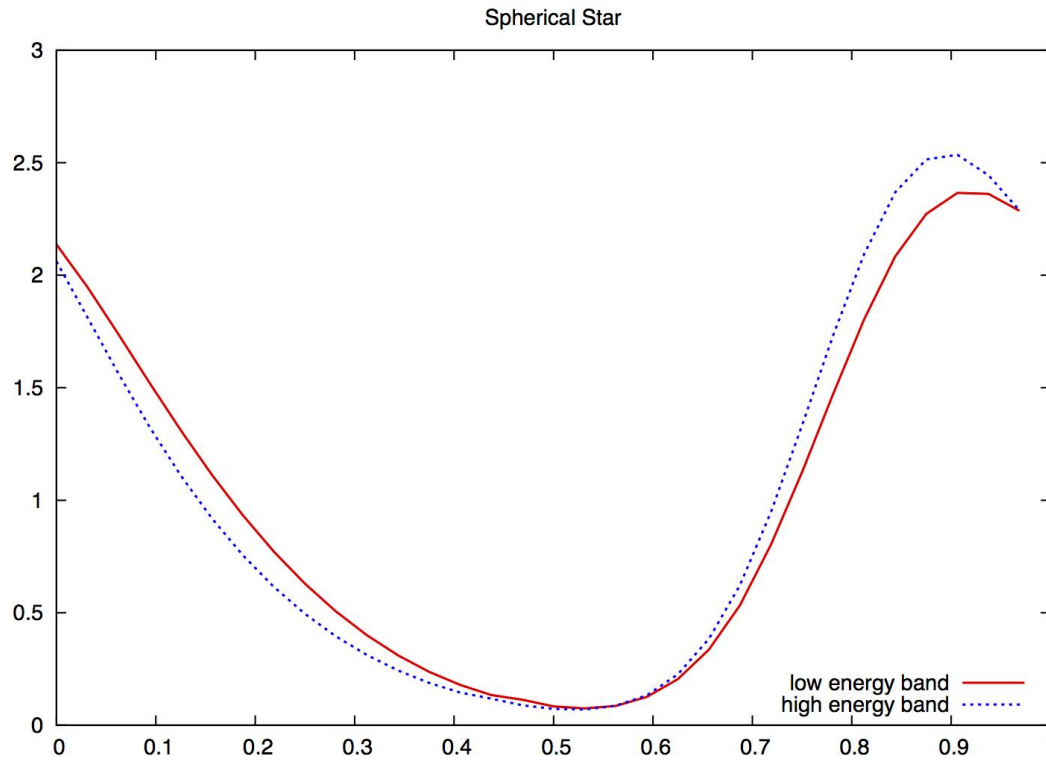
Curves are almost sinusoidal – almost anything will fit!

Genetic Algorithm Best fit contours (after adding Poisson Noise)



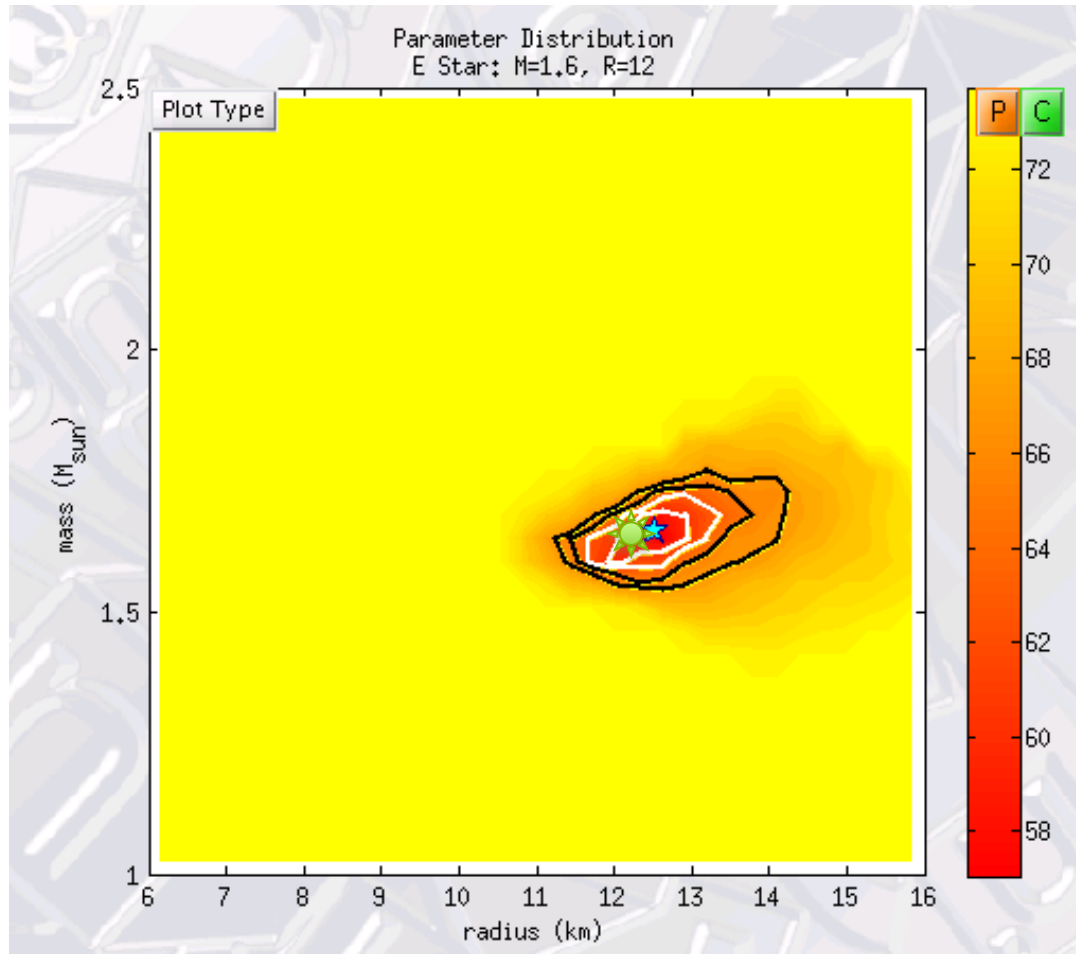
True value within 1 sigma of best-fit model (star) but poor accuracy and precision

Theoretical curves for $M=1.6$, $R=12\text{km}$,
spin=600 Hz, $i=60$, $\theta=60$
 $v \sim 0.15 c$



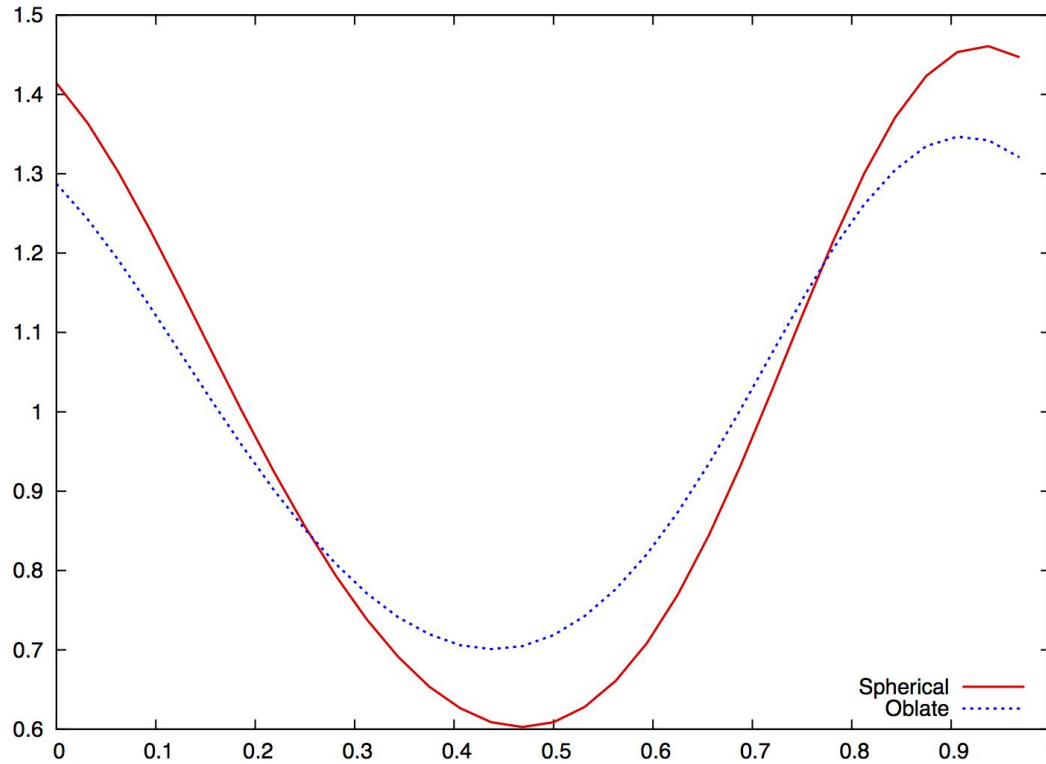
Curves are asymmetric – “features” help fitting

Genetic Algorithm Best fit contours (after adding Poisson Noise)



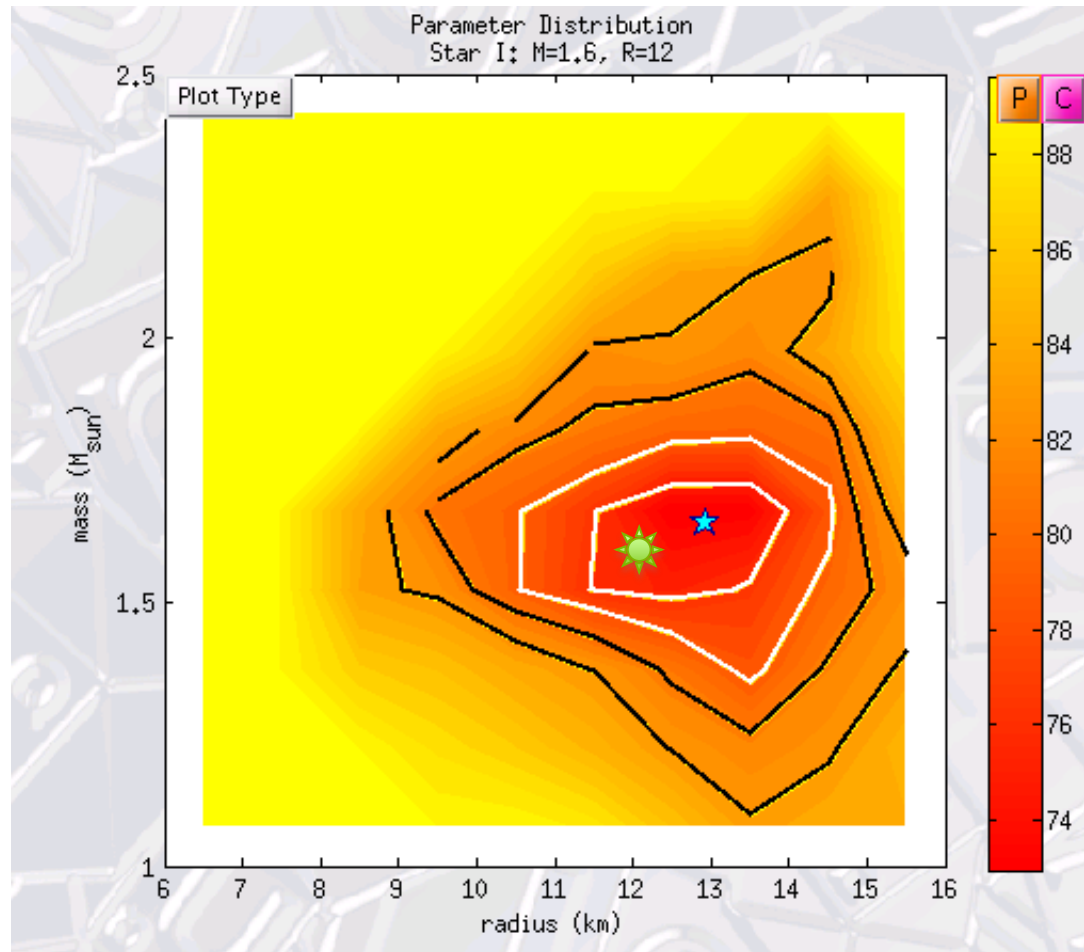
Good accuracy and precision

Theoretical curves for $M=1.6$, $R=12\text{km}$,
spin=600 Hz, $i=60$, $\theta=20$ and oblate
 $v \sim 0.05 c$



Curves are less modulated than those produced by spherical star

Genetic Algorithm Best fit contours (after adding Poisson Noise)



Better accuracy and precision compared to spherical star; oblate shape “breaks” degeneracy between angles and radius

Conclusions

- All methods for constraining Mass and Radius for neutron stars are model dependent and may suffer from unknown systematics
- Important to explore many independent methods to determine EOS!
- X-ray burst observations have potential to provide better constraints, with LOFT's better statistics