

# The Neutron Star Radius and the dense matter equation of state

Sebastien Guillot  
Robert Rutledge



**Results from Guillot et al. 2013, ApJ 772**

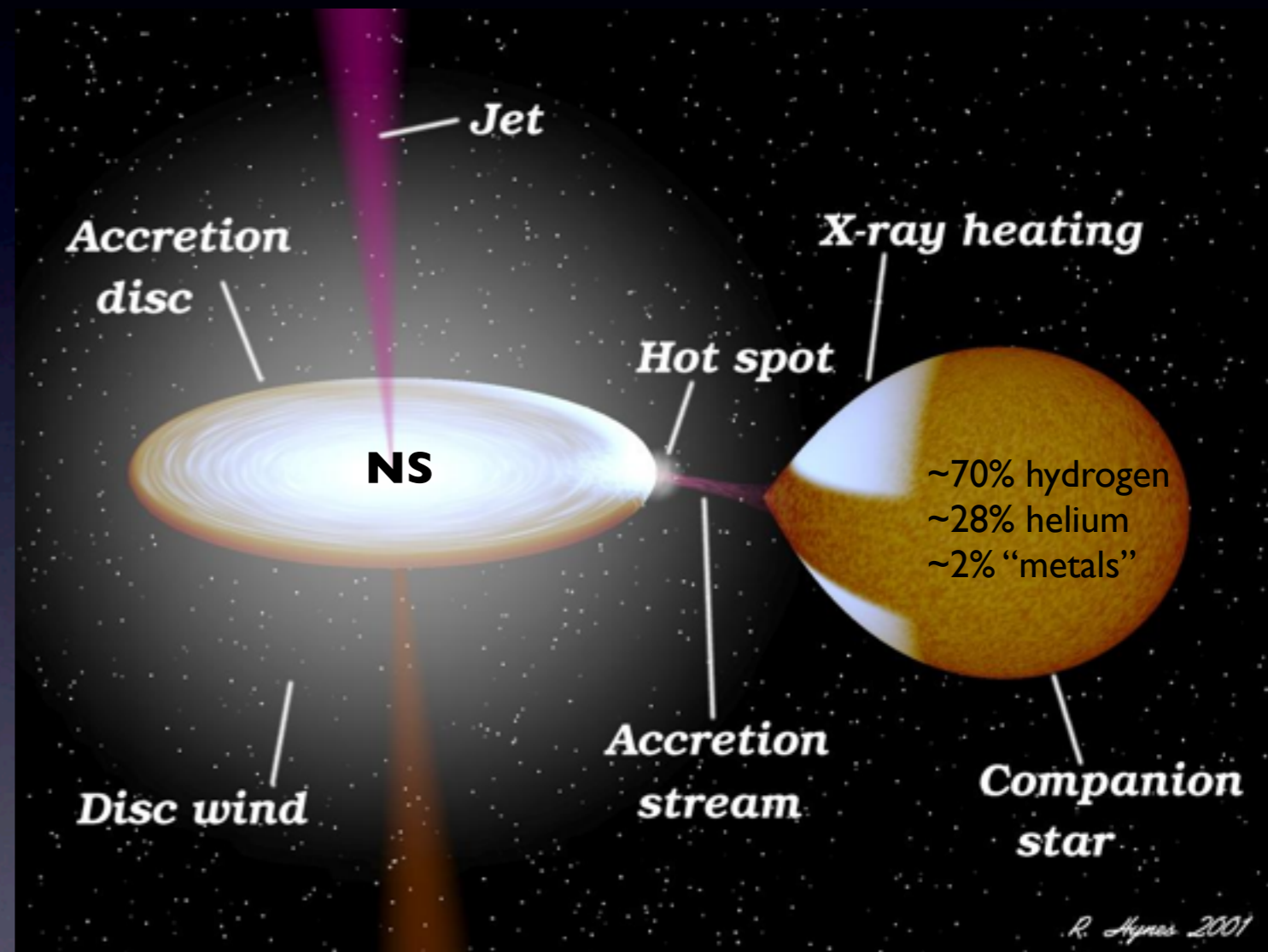
## Collaborators

Natalie Webb, IRAP (Toulouse, France)  
Mathieu Servillat, Harvard-CfA & CEA Saclay

*27th Texas Symposium - Dallas, TX  
Dec. 2013*

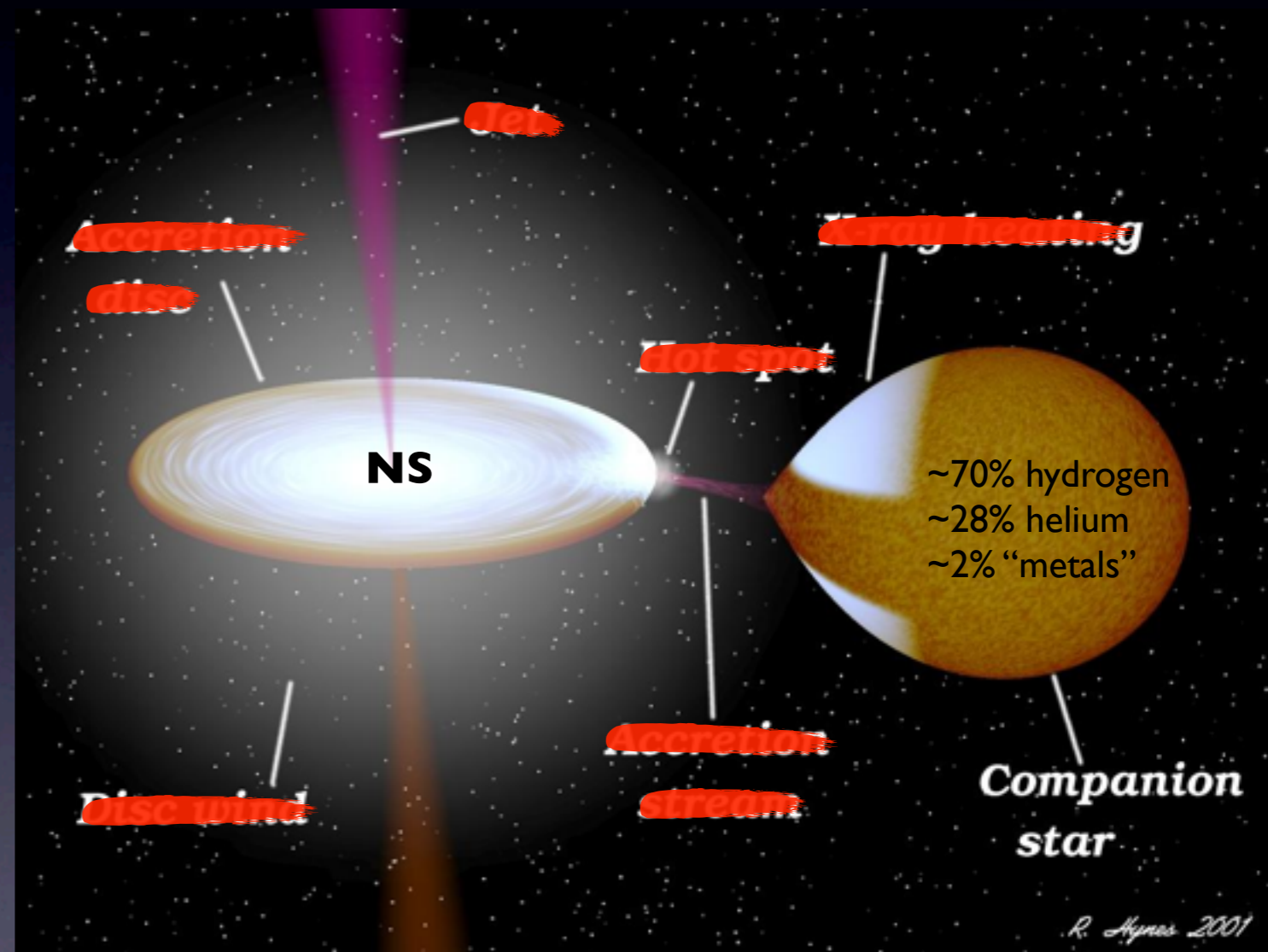
# Quiescent low-mass X-ray binaries are ideal systems for Mass-Radius measurements.

- In quiescence, LMXBs have low mass accretion rate
- Thermal emission powered by deep crustal heating
- Surface thermal emission comes from a pure hydrogen atmosphere with  $L_x = 10^{32-33}$  erg/sec
- Neutron star has a weak magnetic field



# Quiescent low-mass X-ray binaries are ideal systems for Mass-Radius measurements.

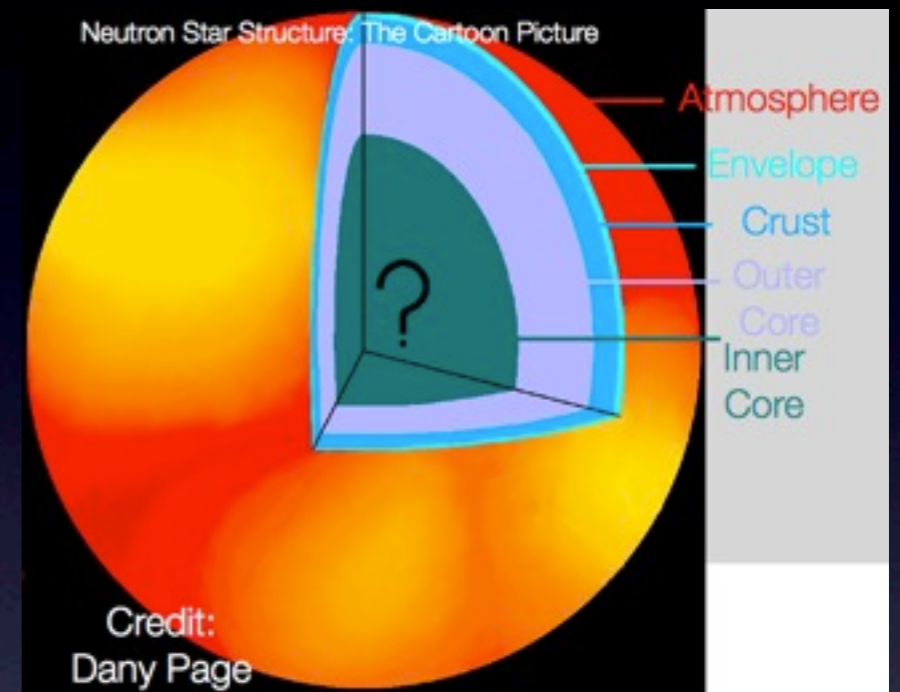
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# The atmosphere of the neutron star in a qLMXB is composed of pure hydrogen.

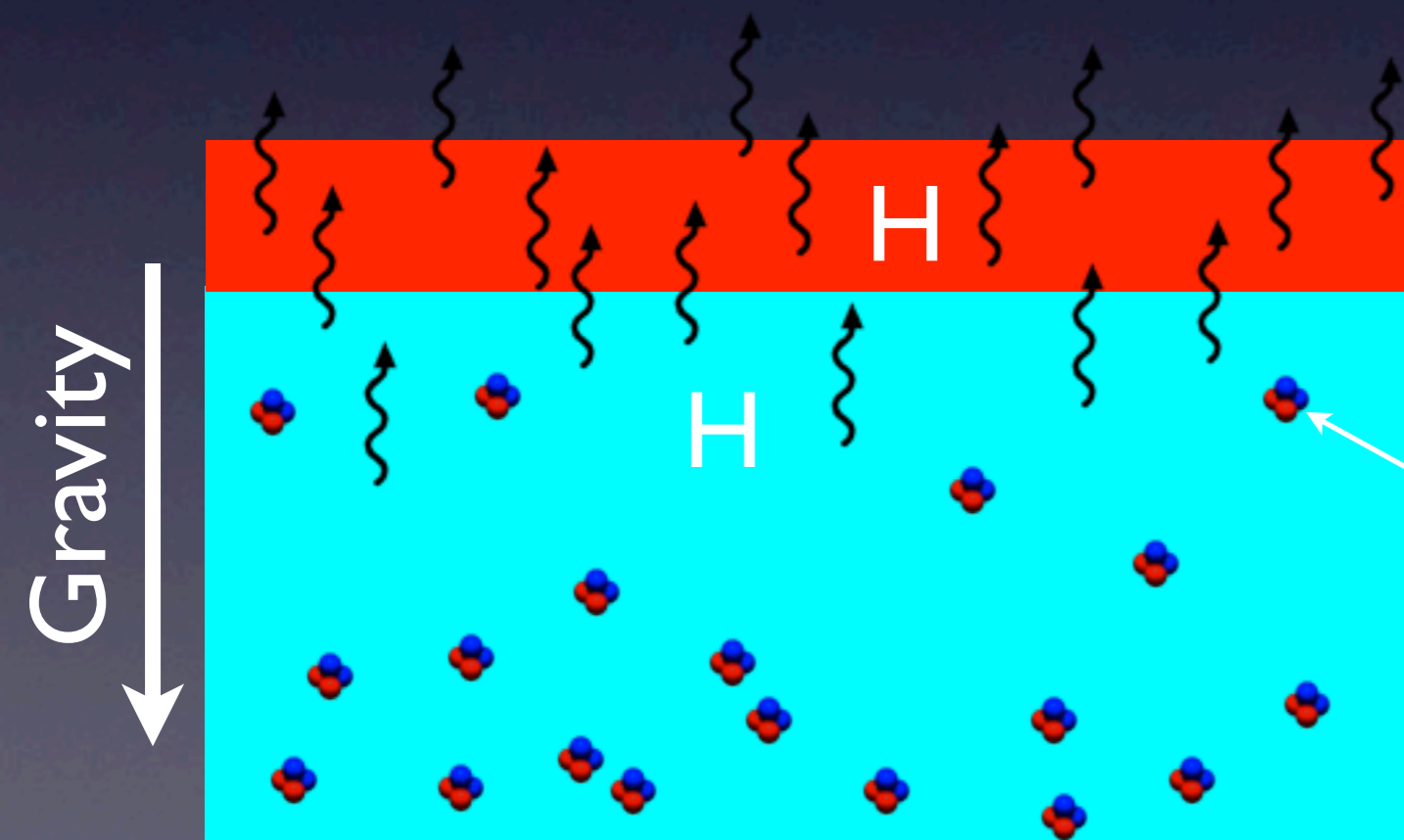


H-atmosphere  
thermal spectrum  
seen by observer



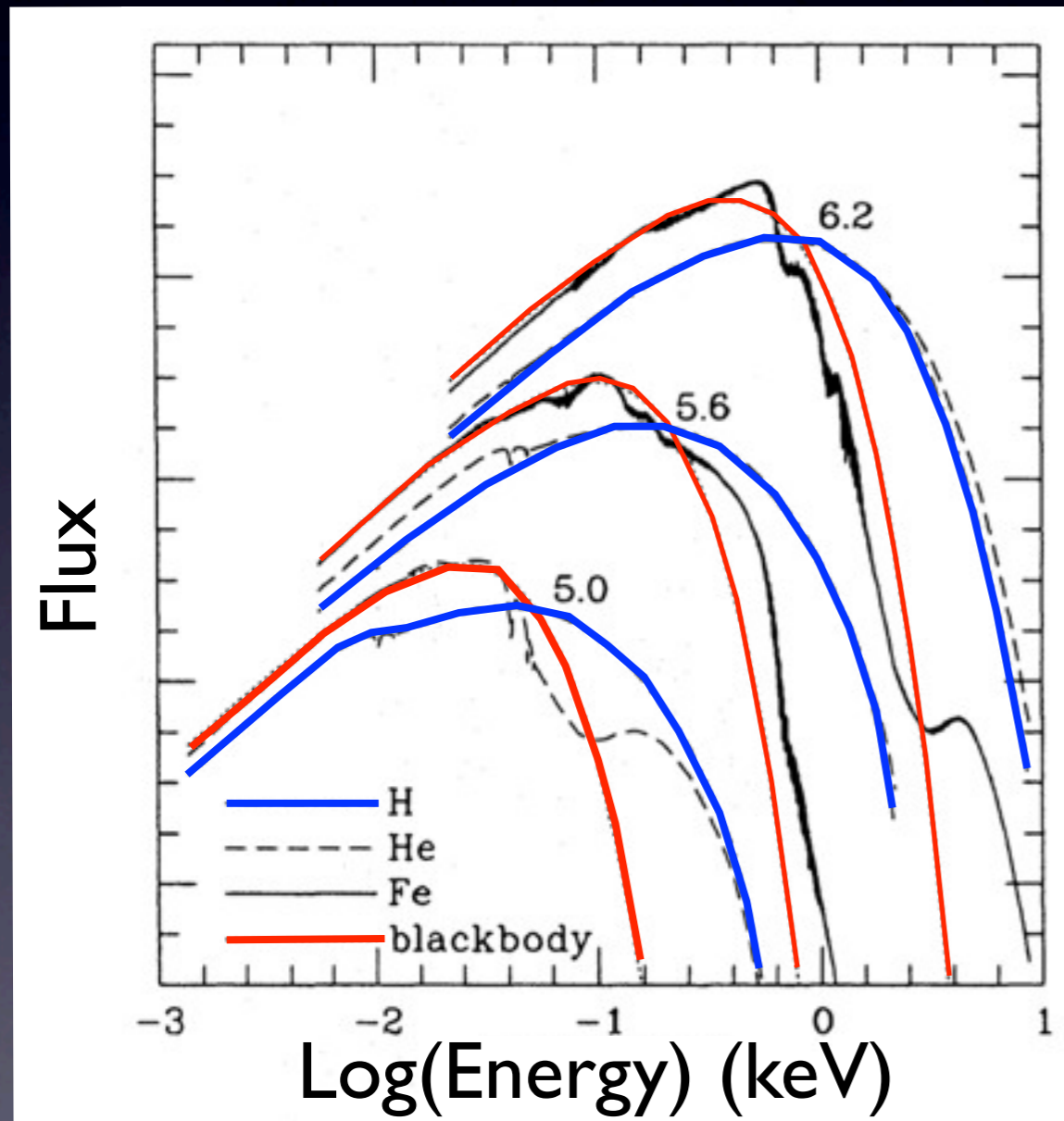
Photosphere  $\sim 10$  cm

Helium



# The thermal emission from a NS surface is modelled with NS atmosphere models.

Models by Zavlin et al. (1996), Heinke et al. (2006), Haakonsen et al. (2012)



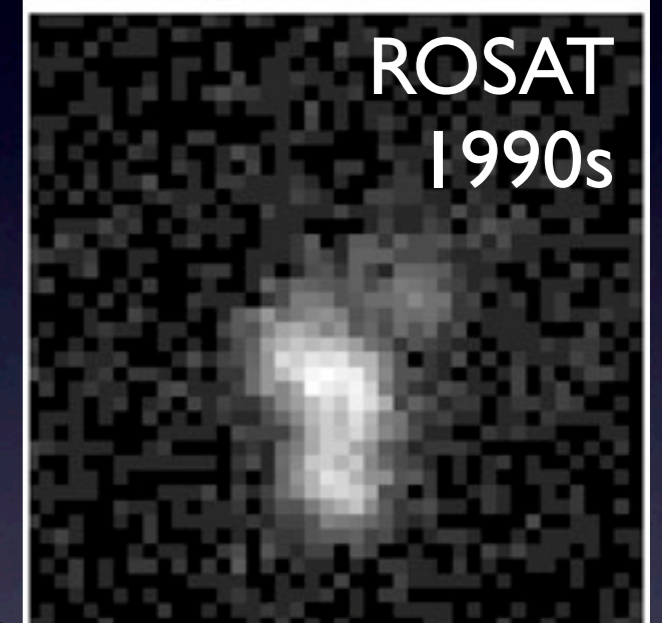
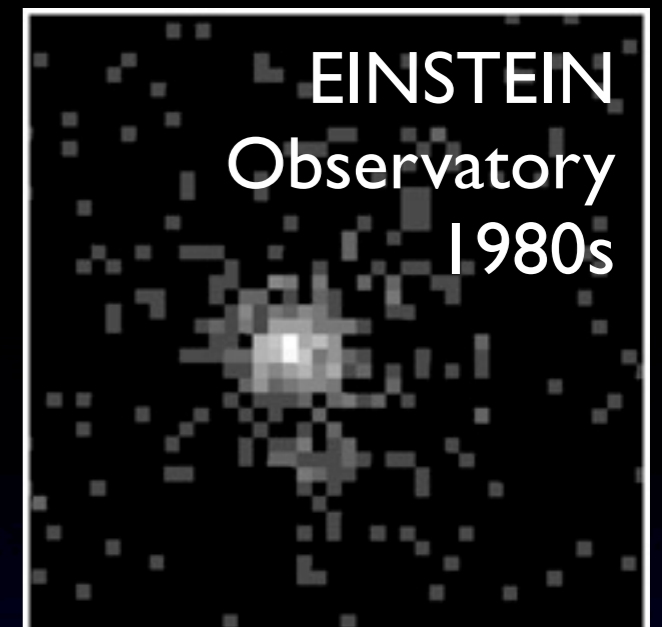
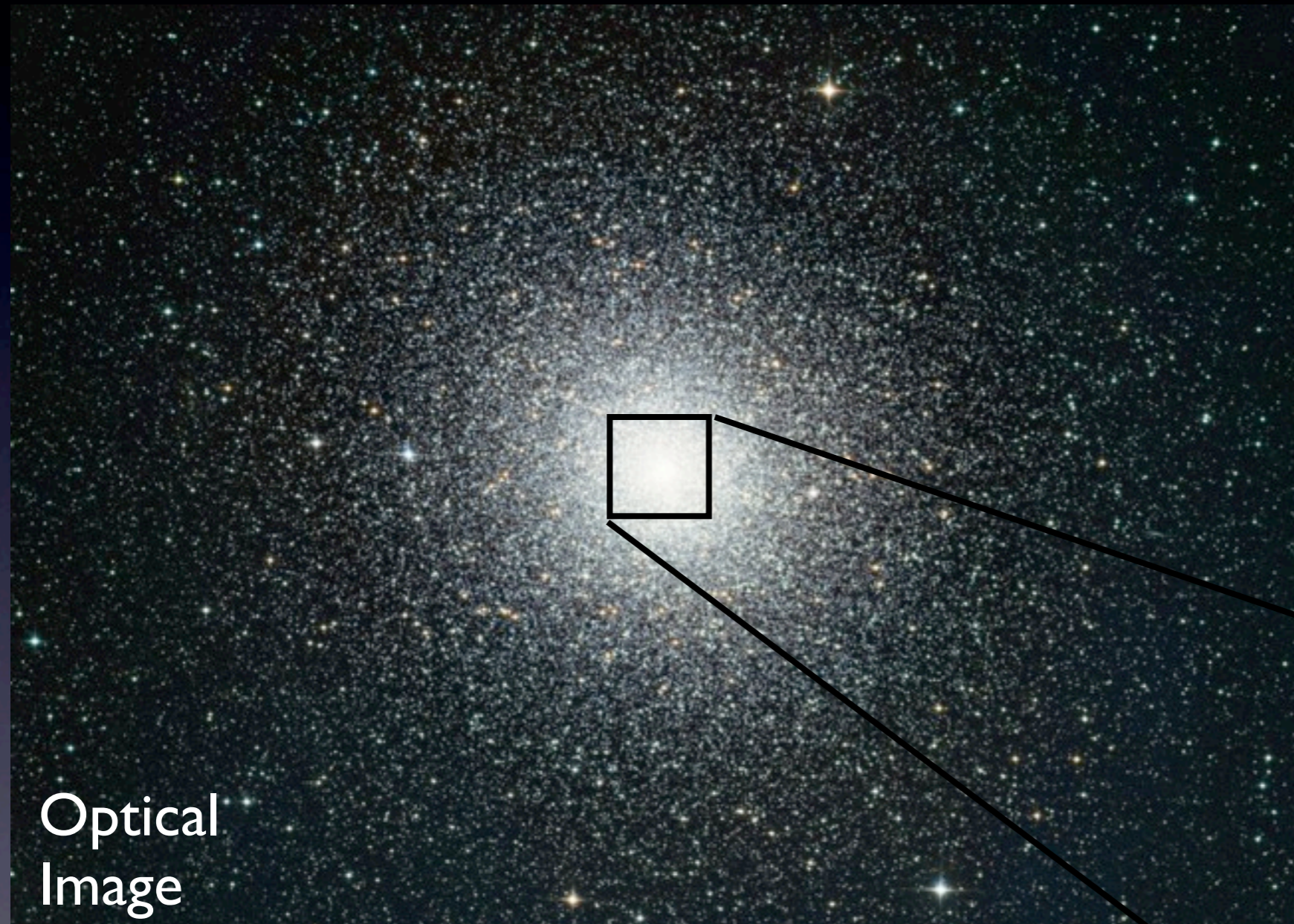
Spectral fitting of the thermal emission gives us  $T_{\text{eff}}$  and  $(R_{\infty}/D)^2$

$$R_{\infty} = R_{\text{NS}} \left( 1 - \frac{2GM_{\text{NS}}}{R_{\text{NS}} c^2} \right)^{-1/2}$$

NS H-atmosphere model parameters are:

- Effective temperature  $kT_{\text{eff}}$
- Mass  $M_{\text{NS}}$  ( $M_{\odot}$ )
- Radius  $R_{\text{NS}}$  (km)
- Distance  $D$  (kpc)

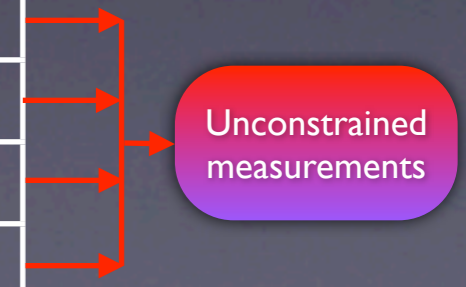
# Globular clusters host an overabundance of LMXB systems...



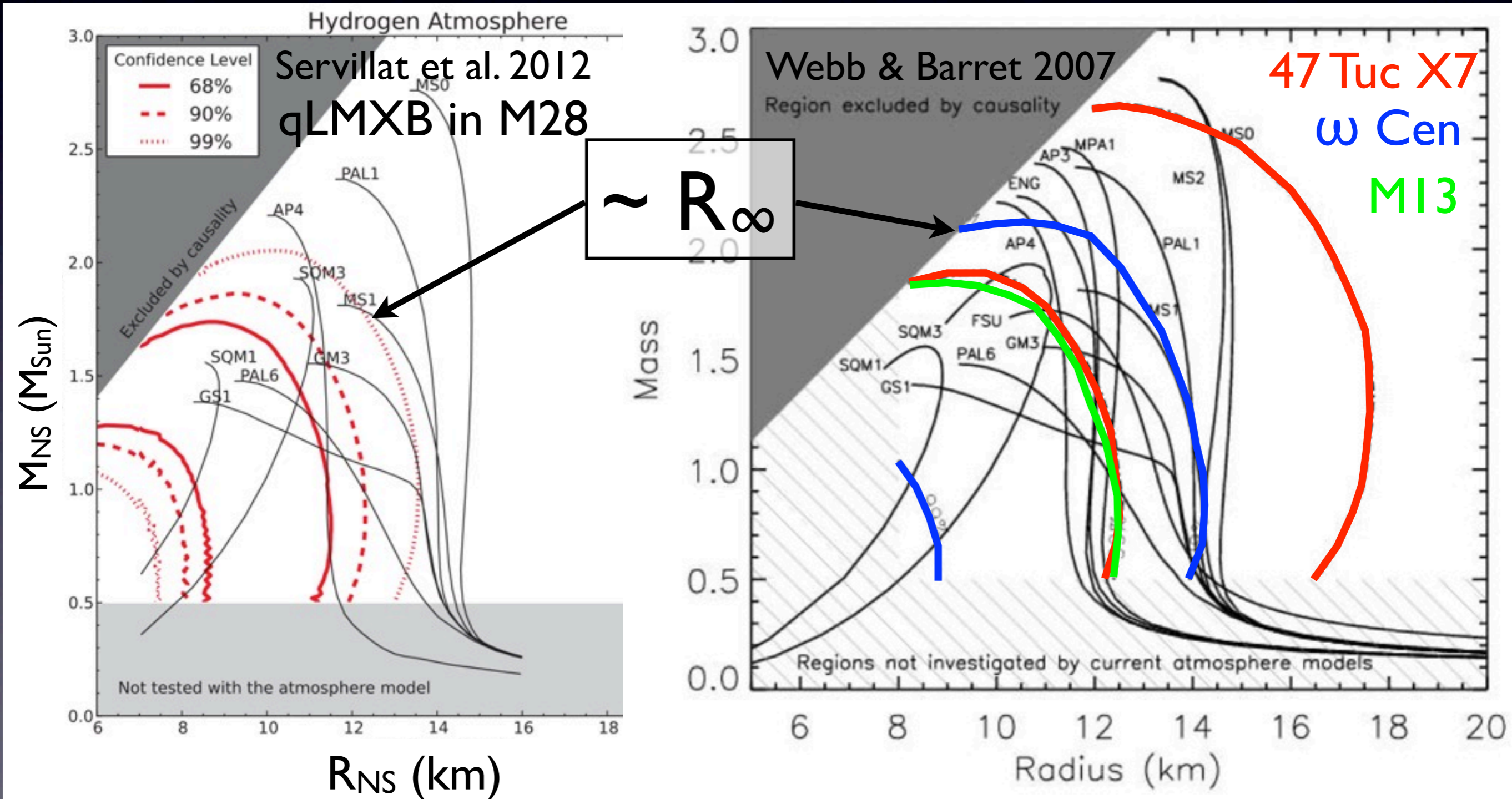
...and they have well-measured distances.

# 29 quiescent LMXBs are known within globular clusters of the Milky Way.

Globular Cluster	Distance (kpc)	$N_H$ ( $10^{22} \text{ cm}^{-2}$ )	qLMXB	“Useful”	Difficulties	Need Chandra
$\omega$ Cen	5.3	0.09	1	Green		NO
M13	7.7	0.01	1	Green		NO
M28	5.5	0.26	1	Green	Moderate pile-up	YES
NGC 6304	6.0	0.27	1	Green		YES
NGC 6397	2.5	0.14	1	Green		YES
NGC 6553	6.0	0.35	1	Green	<i>NEEDS TO BE CONFIRMED</i>	YES
47 Tuc	4.5	0.03	2 (+3?)	Orange	Important pile-up	YES
M30	9.0	0.03	1	Orange	Large distance	YES
M80	10.3	0.09	2	Orange	Large distance	YES
NGC 362	8.6	0.03	1	Orange	Large distance	YES
NGC 2808	9.6	0.82	1	Red	Large distance and $N_H$	YES
NGC 3201	5.0	1.17	1	Red	Very Large $N_H$	NO
NGC 6440	8.5	0.70	8	Red	Large distance and $N_H$	YES
Terzan 5	8.7	1.20	4	Red	Large distance and $N_H$	YES



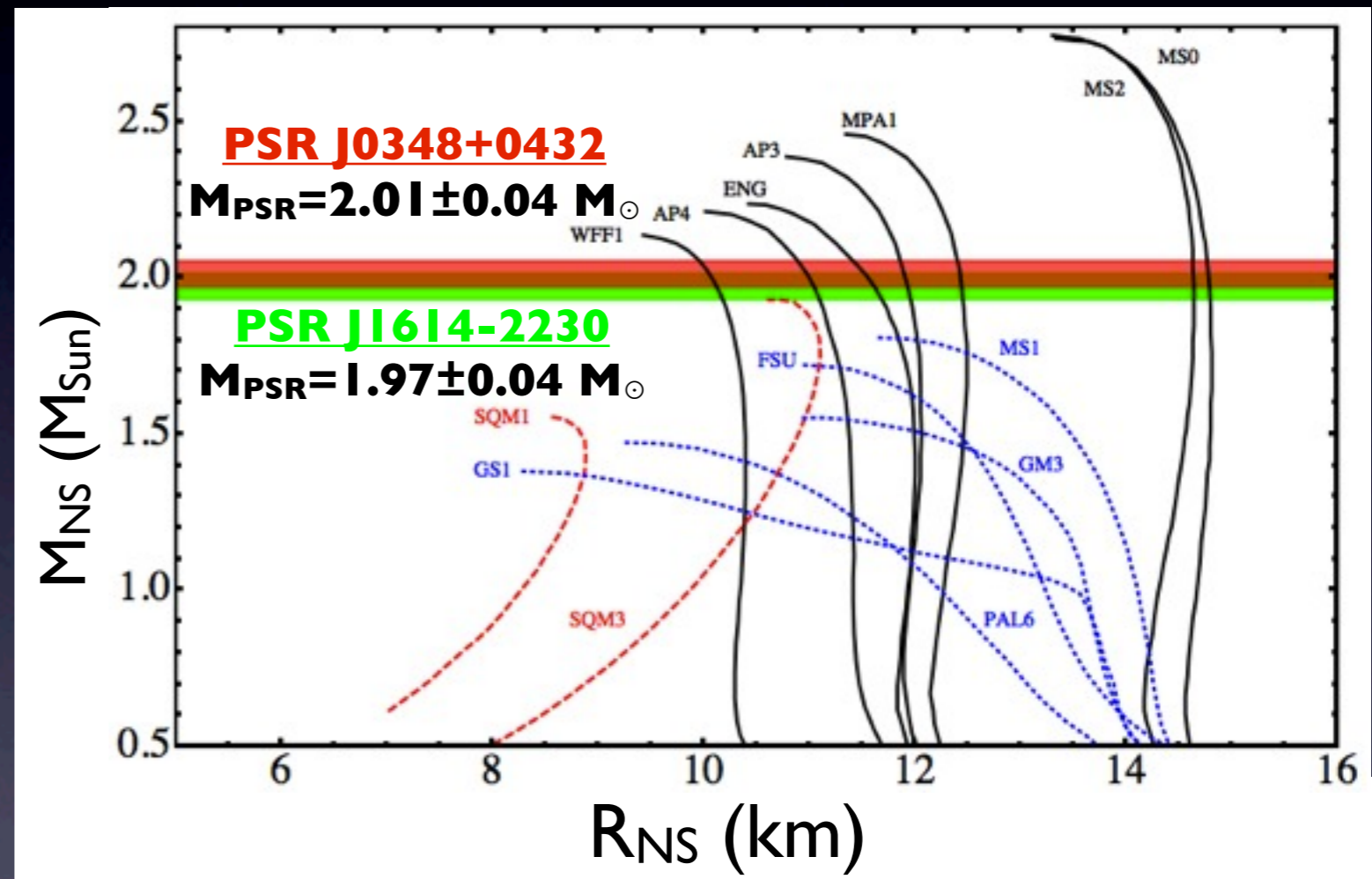
Quiescent LMXBs are routinely used for  $M_{\text{NS}}-R_{\text{NS}}$  measurements, but only place weak constraints on the dense matter EoS.





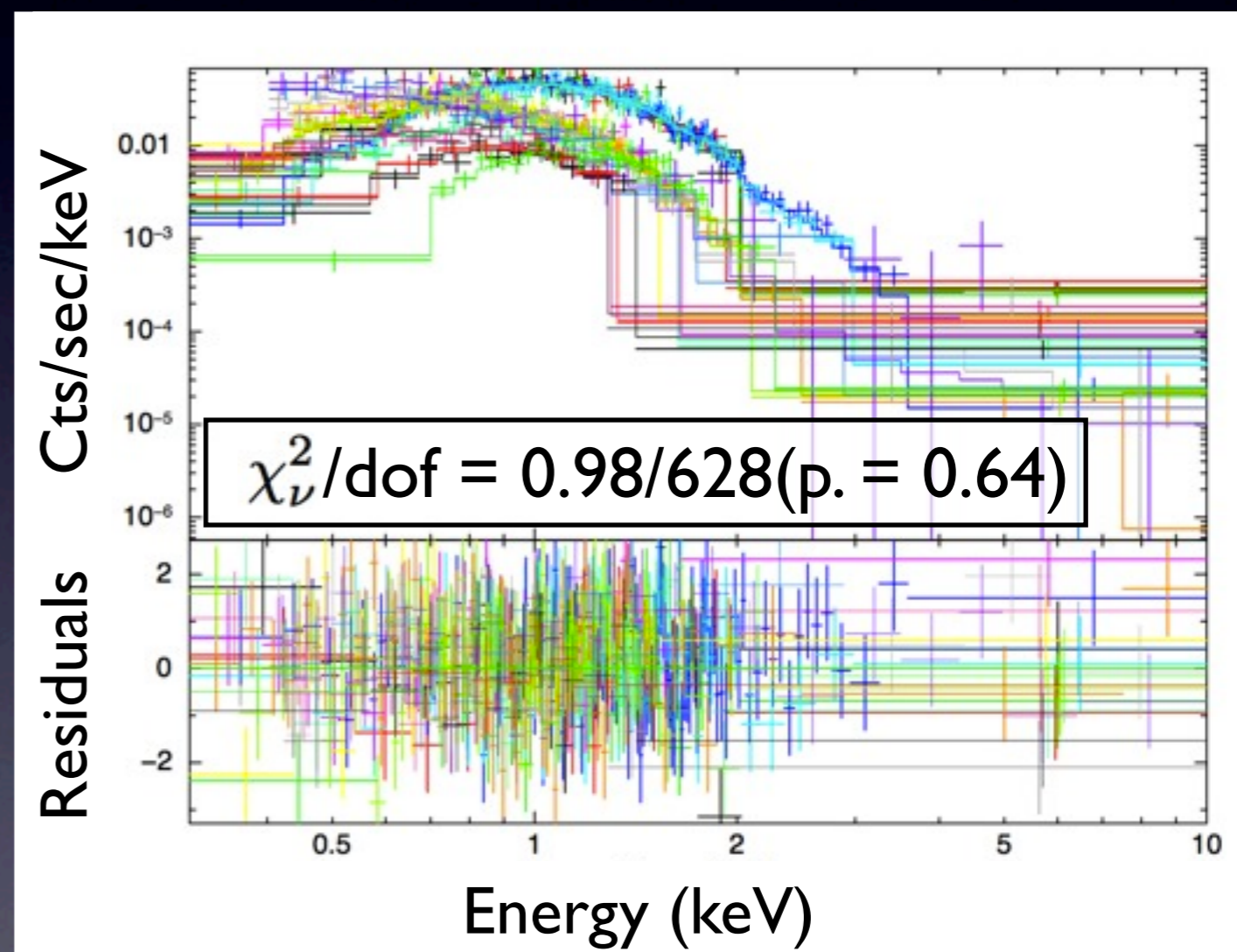
In Guillot et al (2013), we follow a simplified parametrization for the EoS.

Equations of state consistent with  $\sim 2M_{\text{sun}}$  are those described by a constant radius for a wide range of masses.



We assume that  
all neutron stars have the same radius

# We simultaneously fit the spectra of 5 qLMXBs with H-atmosphere model



**One radius to fit them all!**

Five parameters per target:

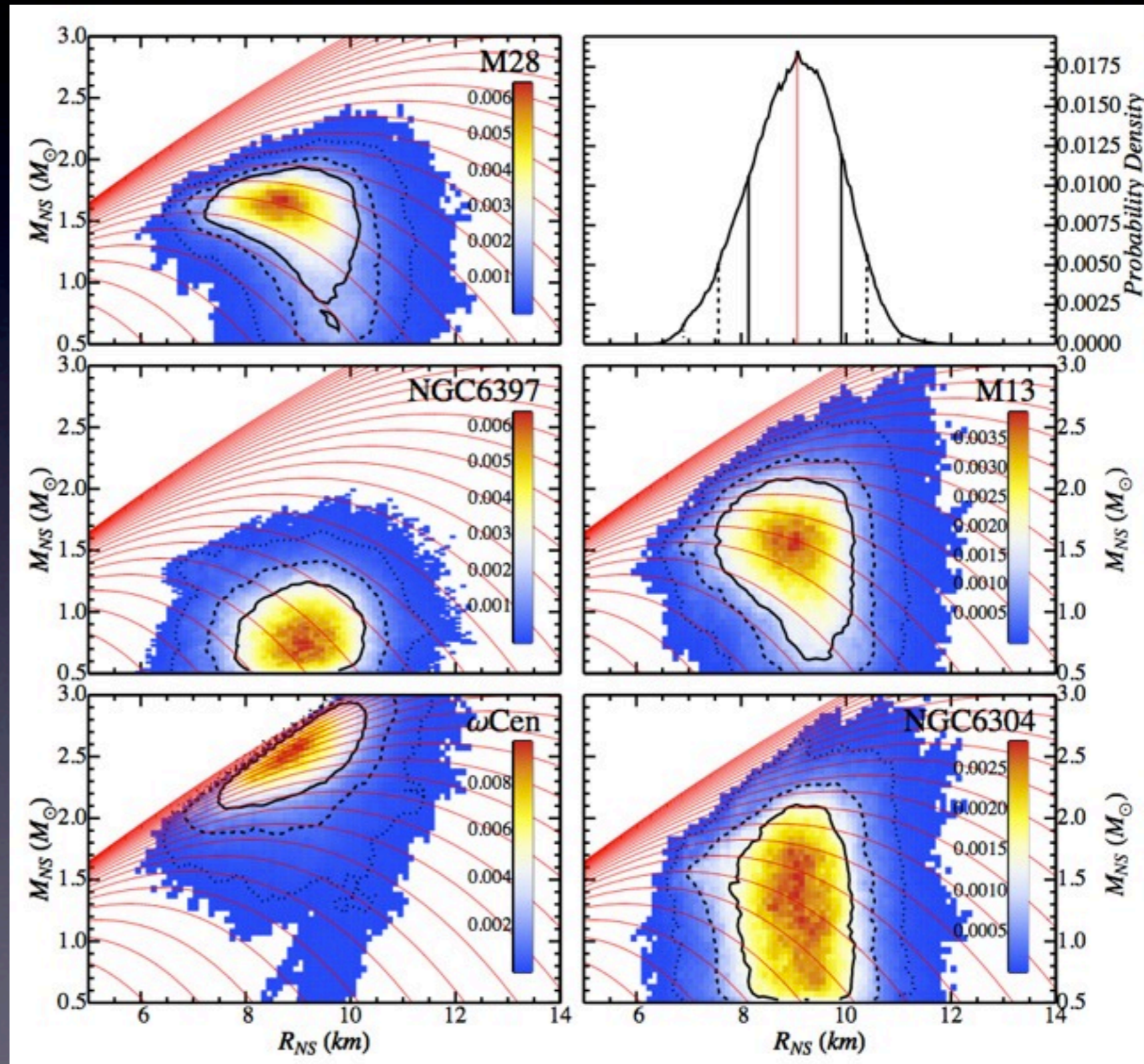
$T_{\text{eff}}$ ,  $M_{\text{NS}}$ ,  $N_{\text{H}}$ , distance,  
power-law component

Our most conservative radius measurement relies on the least number of assumptions.

Most conservative  
NS radius  
measurement is

$$R_{\text{NS}} = 9.1^{+1.3}_{-1.5} \text{ km}$$

90% conf. level



# Our most conservative $R_{NS}$ measurement includes most sources of uncertainty

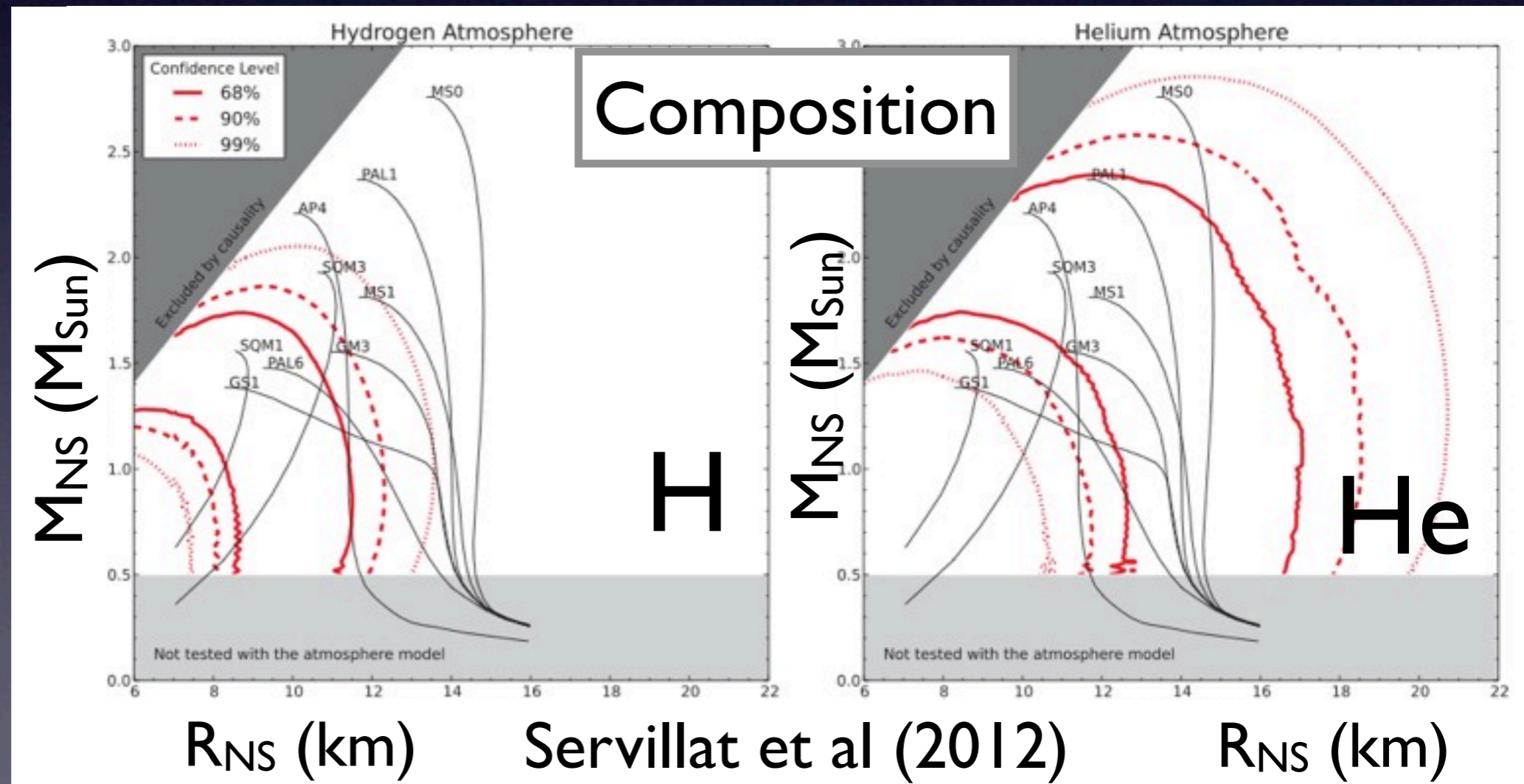
We included the uncertainties linked to:

- Galactic absorption
- Distances of the host clusters
- Possible power-law component
- Calibration of x-ray detectors

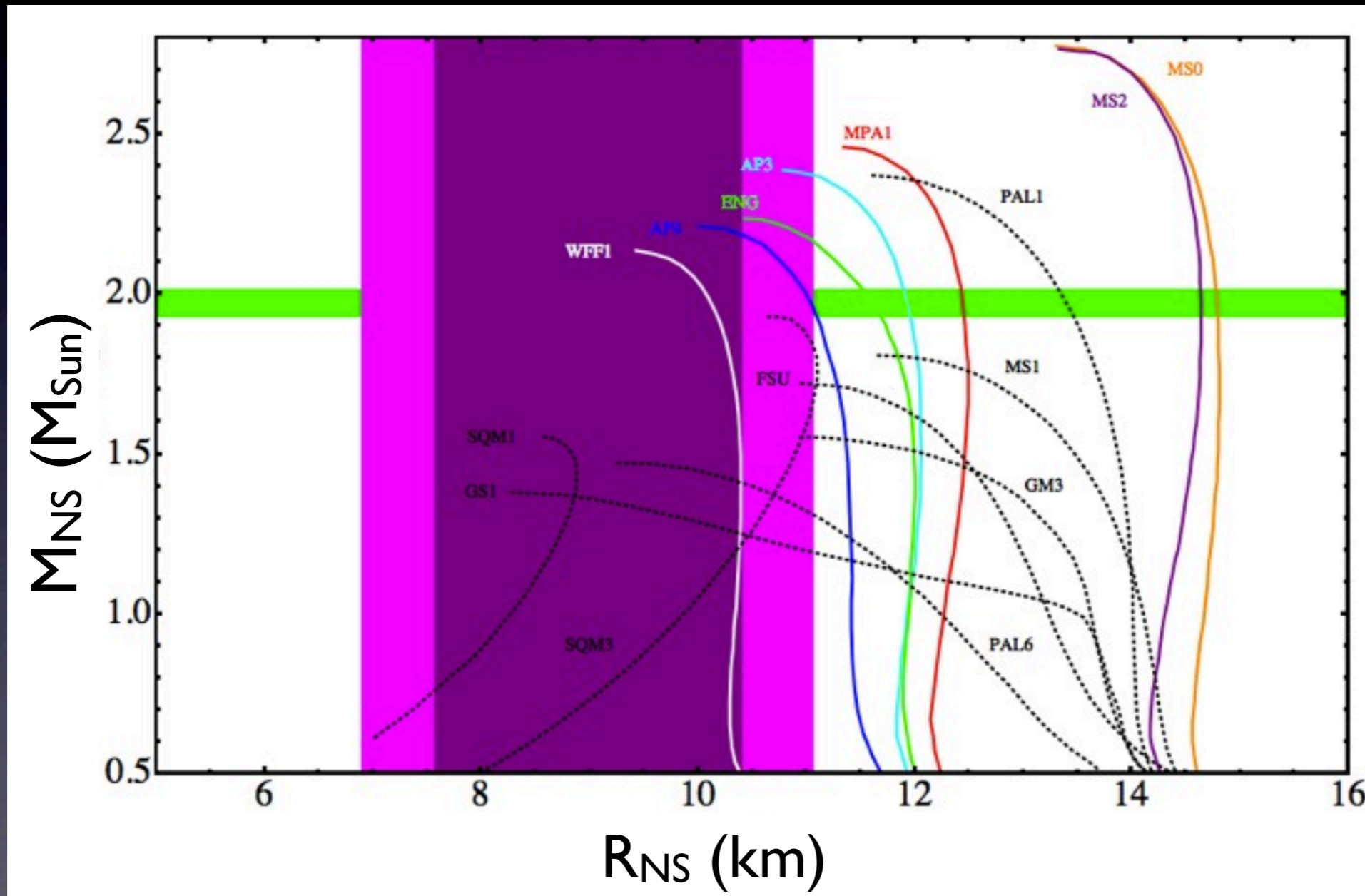
# There are analysis assumptions

NS surface emits isotropically

Negligible magnetic field



Our most conservative radius measurement places important constraints on the dense matter equation of state.



$R_{NS}$  in the 7-11 km range at the 99%-confidence level

# Conclusions

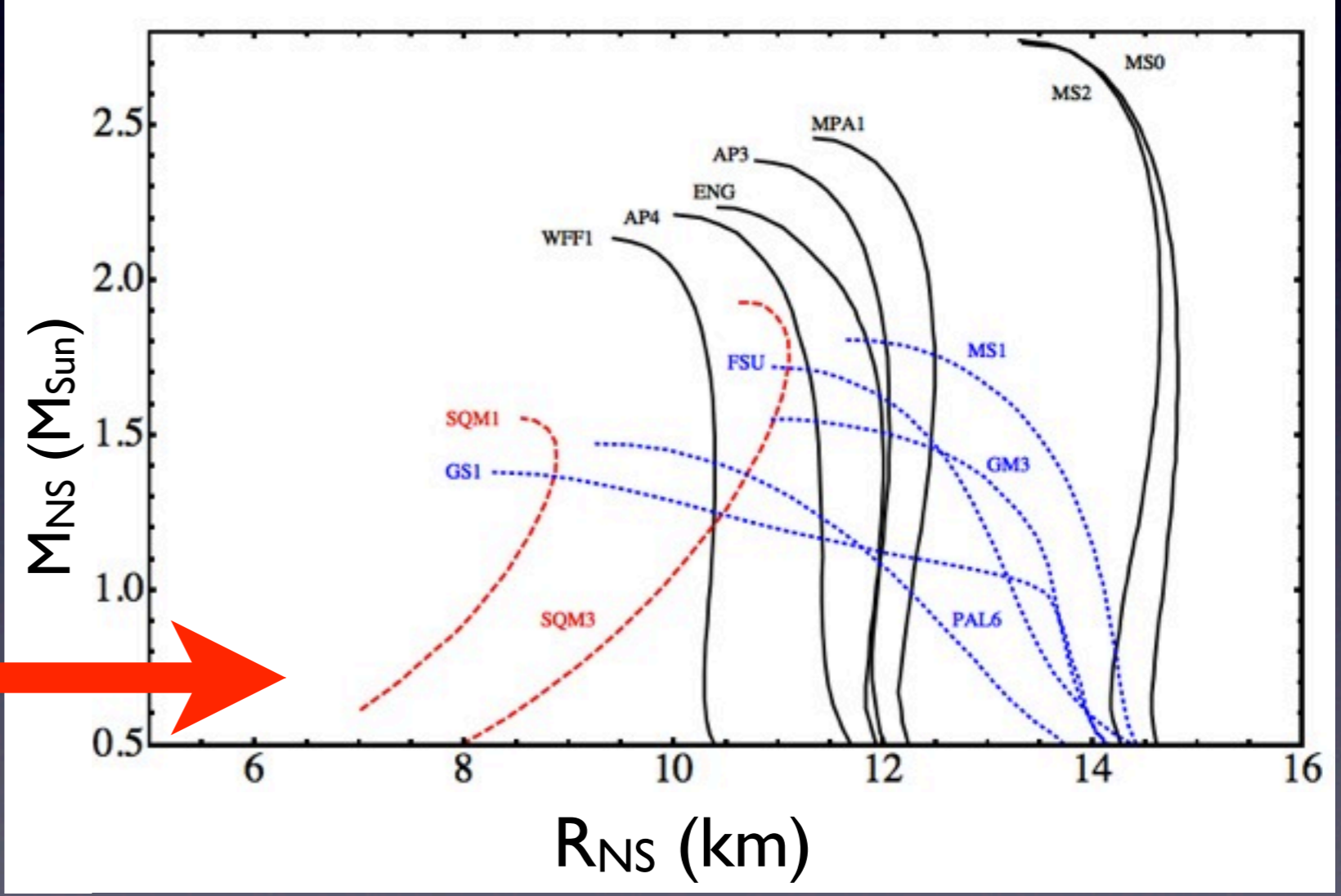
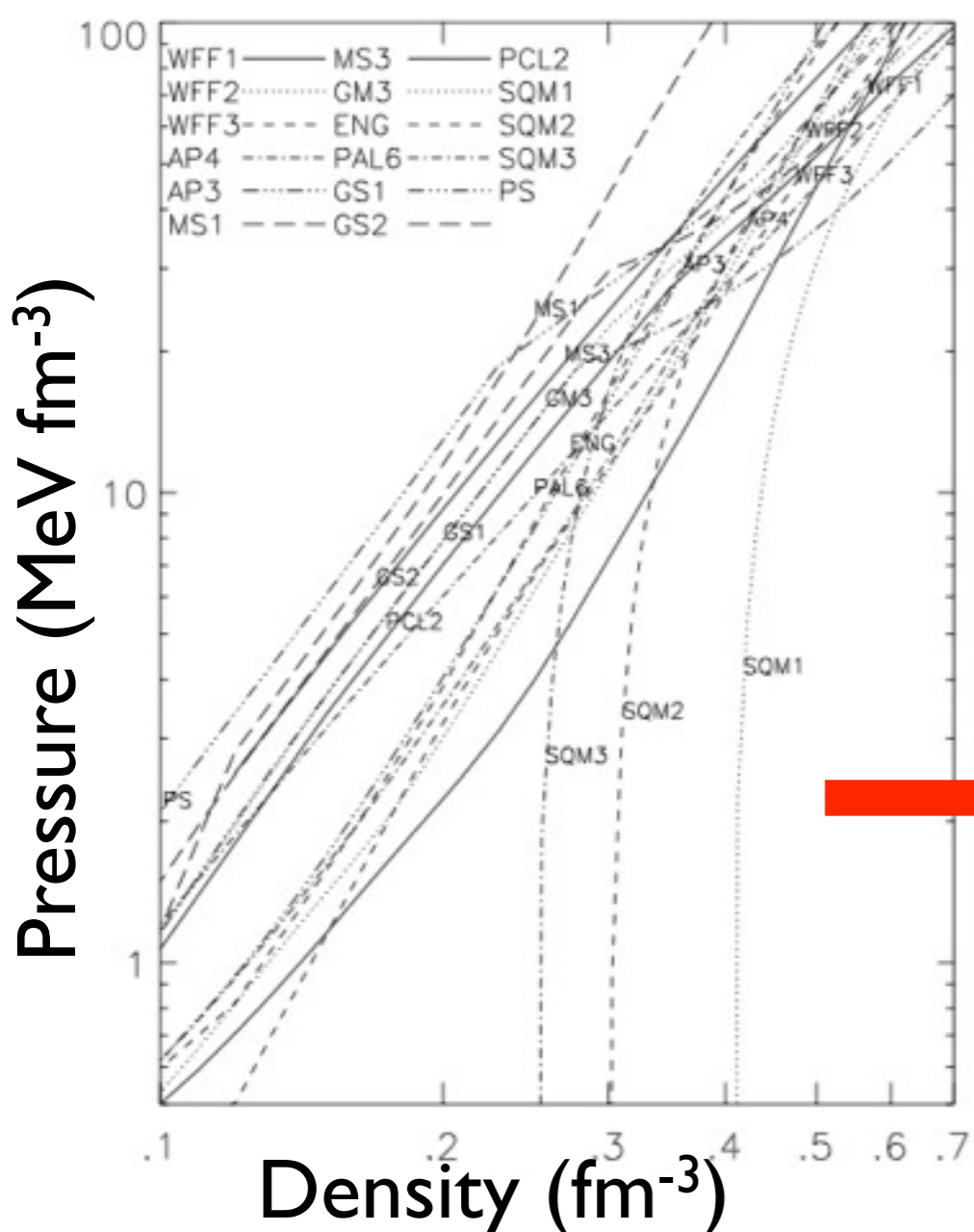
- Evidence that  $R_{\text{NS}}$  is constant for a wide range of masses
- Use this assumption to measure  $R_{\text{NS}}$  from five quiescent low-mass X-ray binaries located inside globular clusters
- Spectral fit with neutron star H atmosphere model using an MCMC simulation
- Measurement of  $R_{\text{NS}} = 9.1_{-2.2}^{+2.0}$  km (99% c.l.) with the least number of assumptions, and a particular effort to control systematic uncertainties.
- Only some EoSs are consistent with these results, for example, WFFI (Wiringa et al 1988)





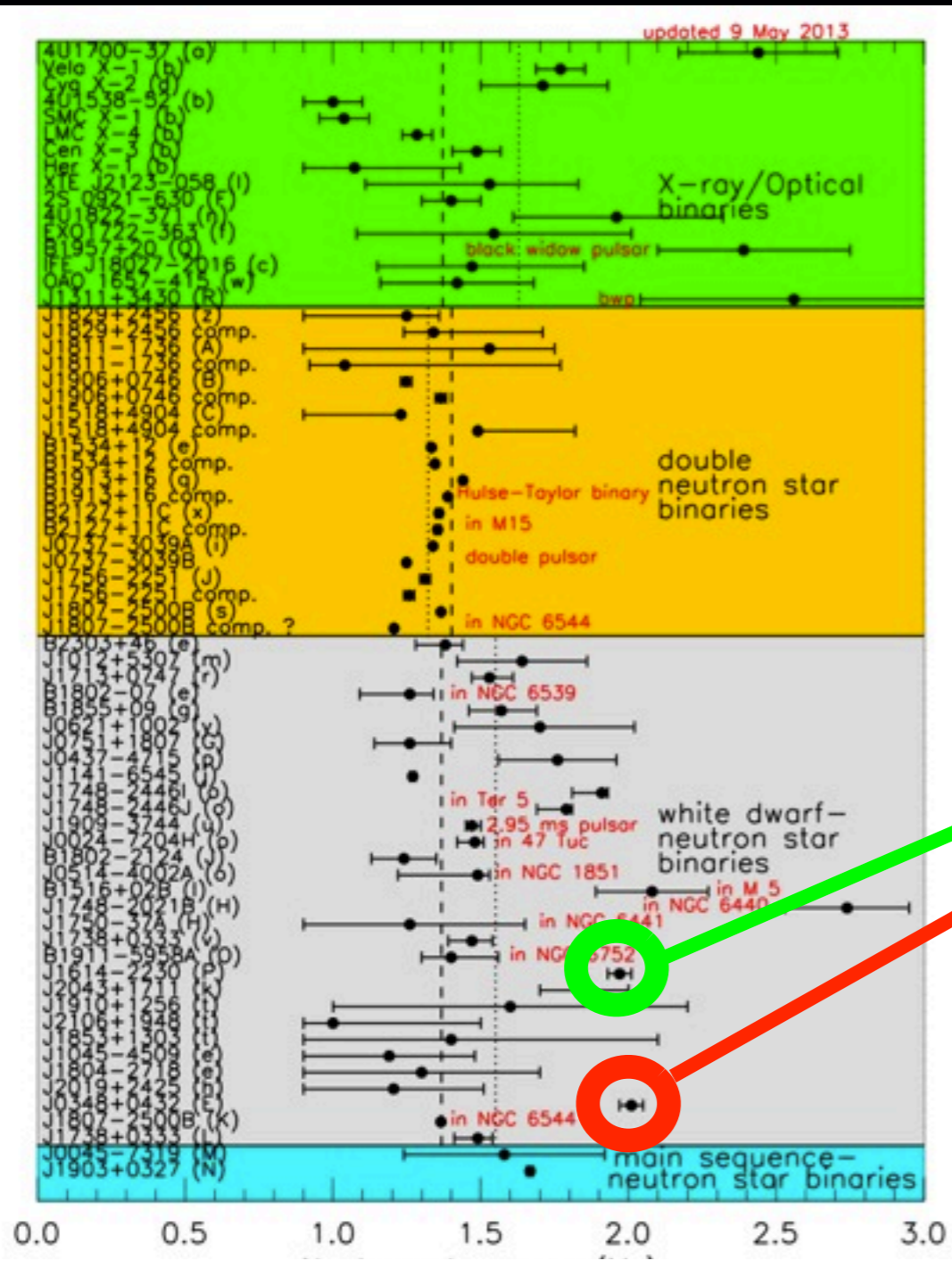
# The nuclear matter equation of state is still unknown and many proposed theories exist.

Density at and above nuclear saturation density  $\rho_{\text{nuc}} = 2.8 \times 10^{14} \text{ g/cm}^3$



Lattimer and Prakash 2001

# Only new $M_{\text{NS}}$ measurements larger than previous ones improve constraints on the dense matter EoS



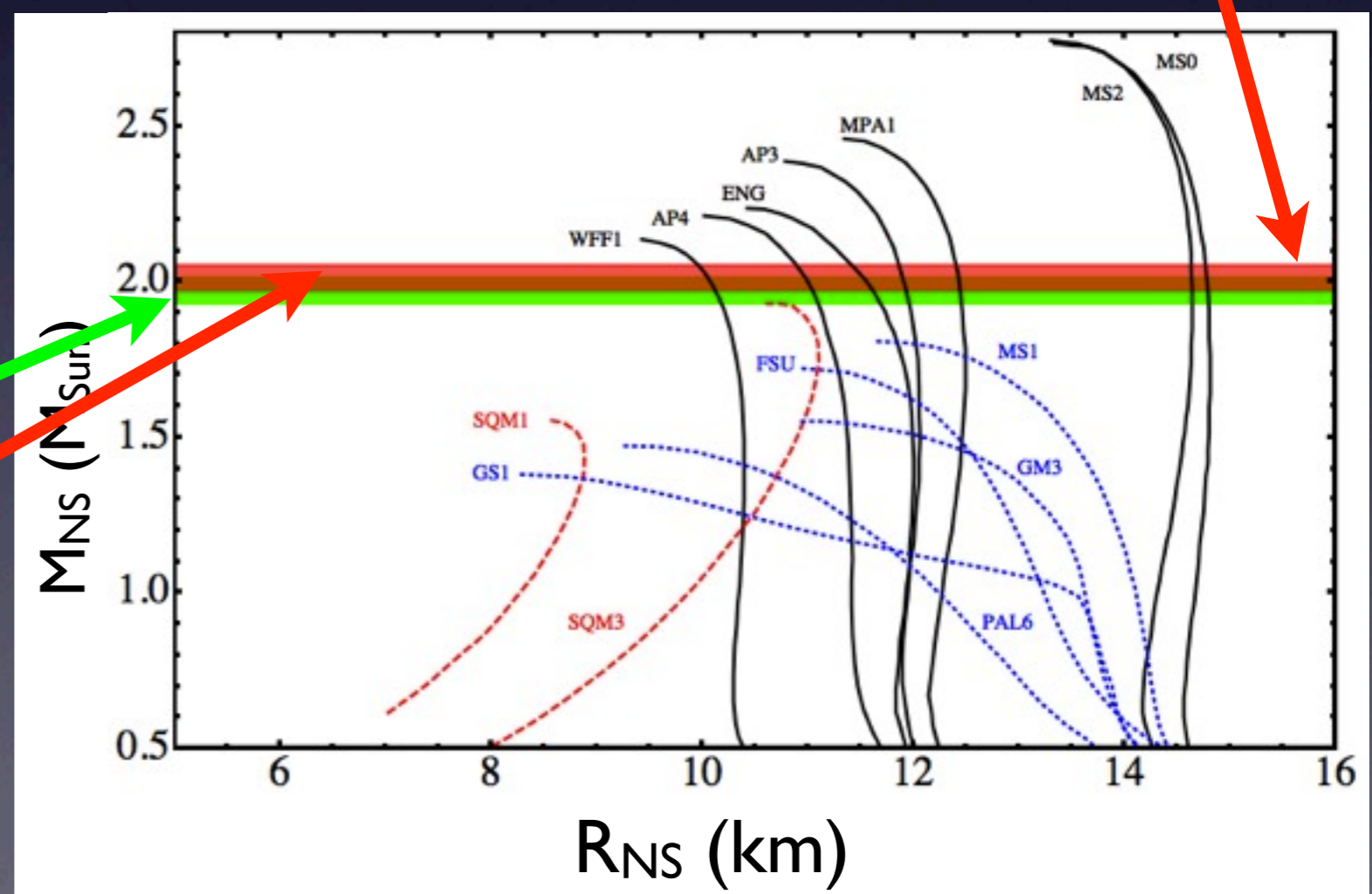
Mass ( $M_{\odot}$ ) Lattimer 2011

PSR J1614-2230

$M_{\text{PSR}} = 1.97 \pm 0.04 M_{\odot}$   
(Demorest et al. 2010)

PSR J0348+0432

$M_{\text{PSR}} = 2.01 \pm 0.04 M_{\odot}$   
(Antoniadis et al. 2013)

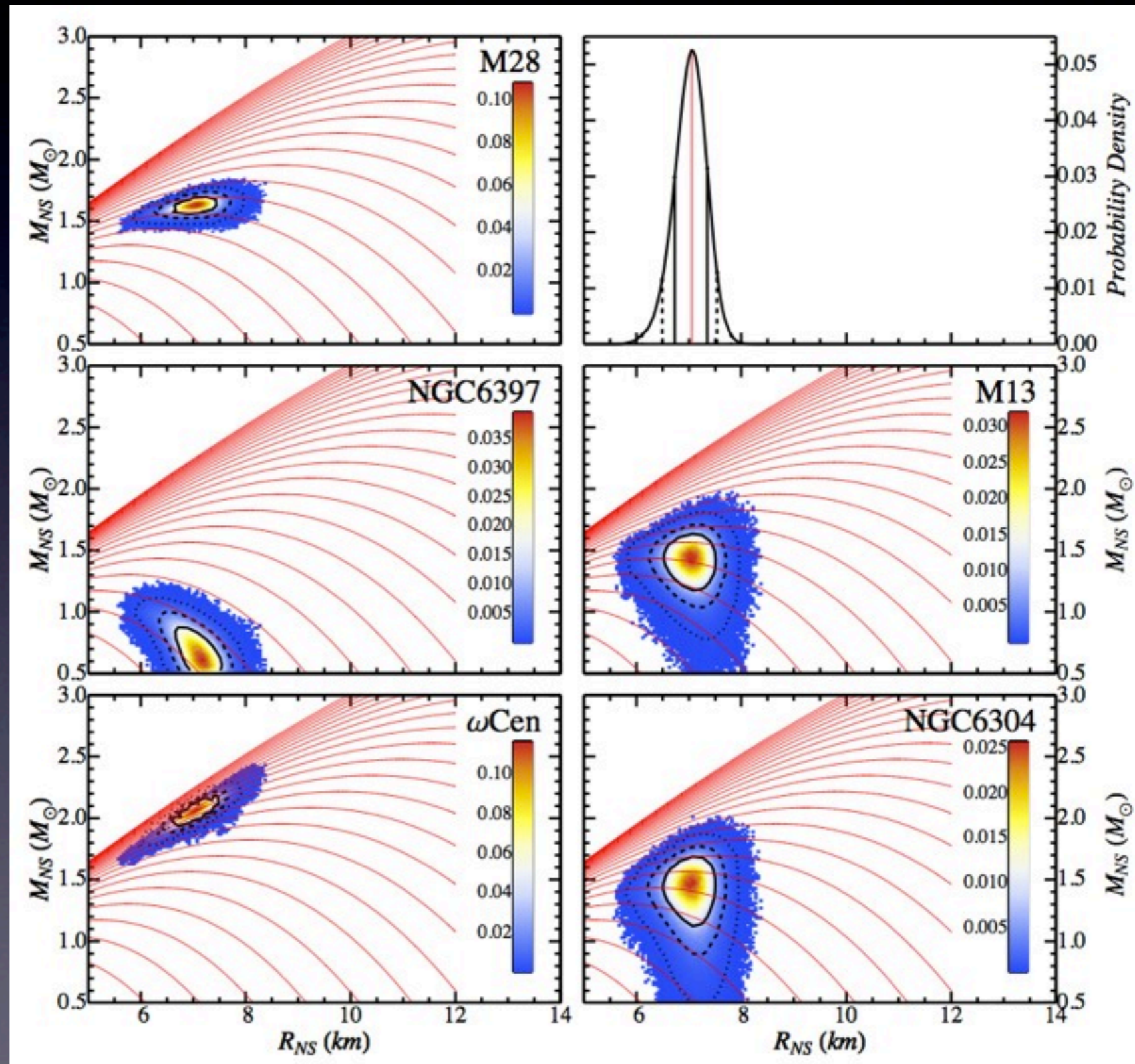


# Our MCMC results with the strongest assumption dependence are the most constraining

We start with an MCMC run with the following assumptions:

- fixed Galactic absorption  $N_H$
- fixed distances to clusters
- no power-law component

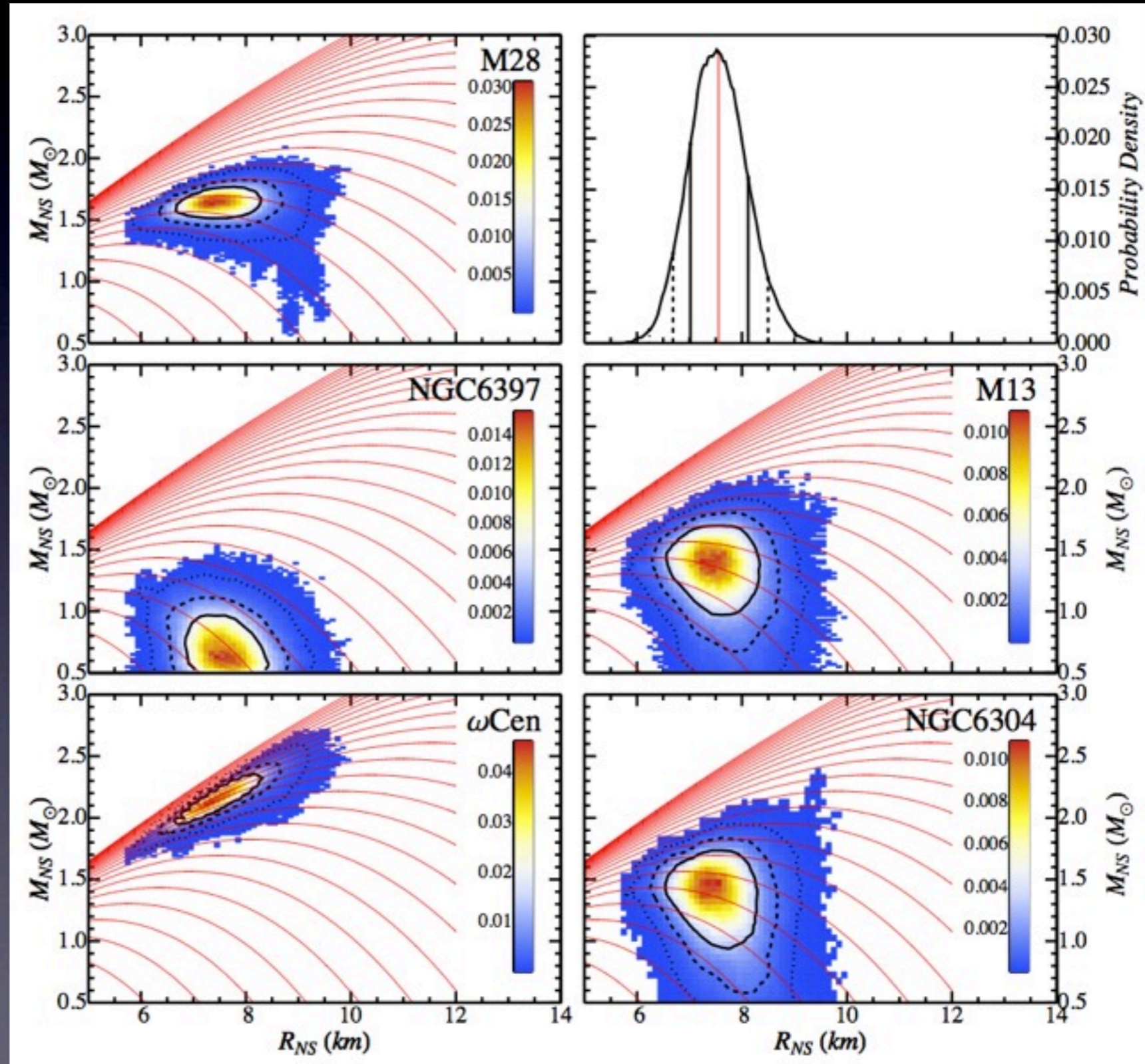
Afterwards, we progressively relax the assumptions.



As assumptions are relaxed,  
uncertainties increase in the  $R_\infty$  direction.

Relaxing assumptions  
contributes to total  
uncertainty

For example here, the  
distance contributes to  
uncertainties in the  $R_\infty$   
direction



# Constraints on the nuclear matter EoS can be derived from neutron star observations.

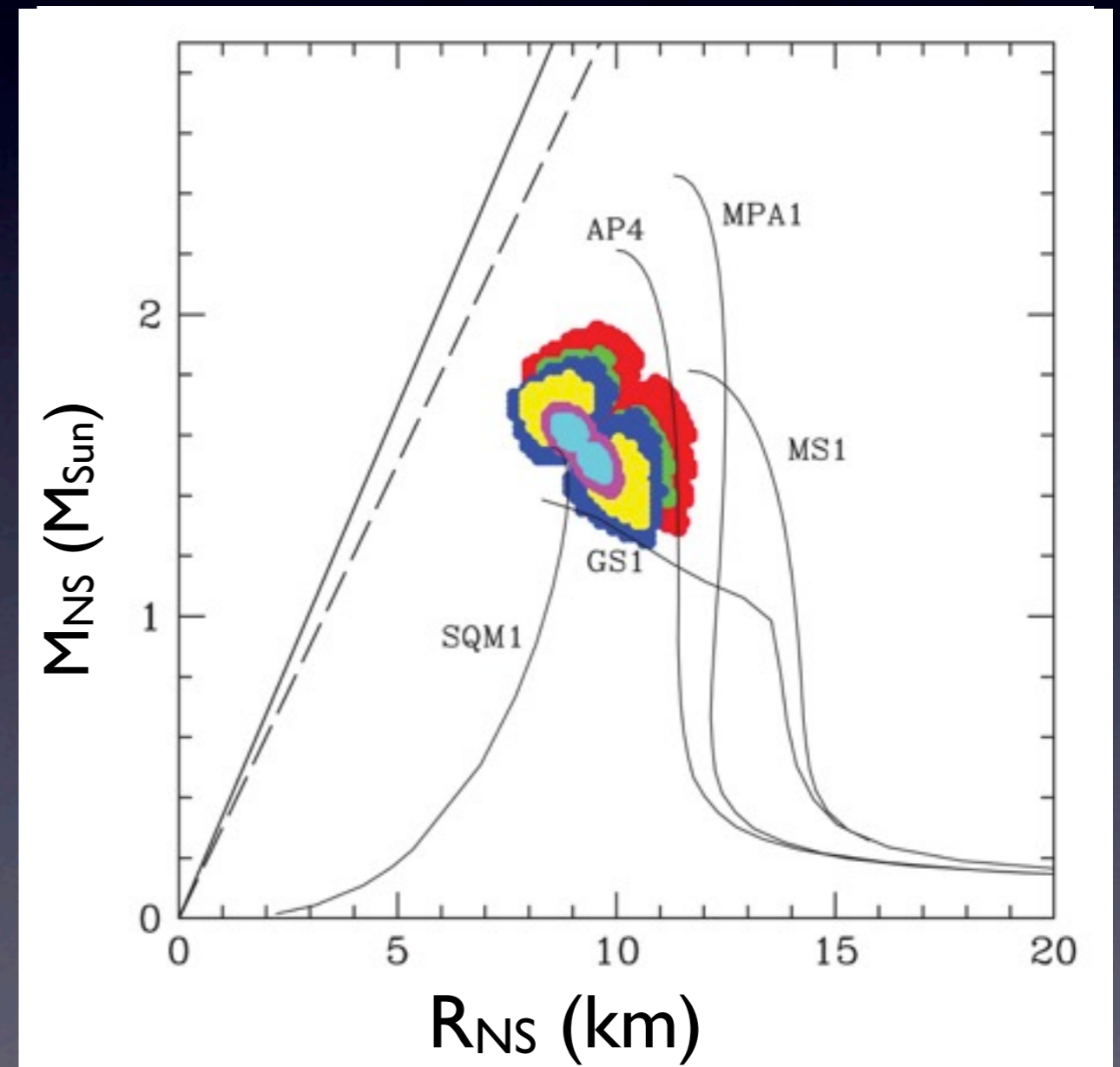
Thermonuclear X-ray burst from accreting low-mass X-ray binaries

(Özel 2006, Suleimanov et al. 2011)

2 observables

$$A = \frac{R^2}{D^2 f_c^4} \left(1 - \frac{2GM}{Rc^2}\right)^{-1}$$

$$F_{\text{Edd}} = \frac{GMc}{k_{\text{es}} D^2} \left(1 - \frac{2GM}{Rc^2}\right)^{1/2}$$



Özel et al. 2010

# Constraints on the nuclear matter EoS can be derived from neutron star observations.

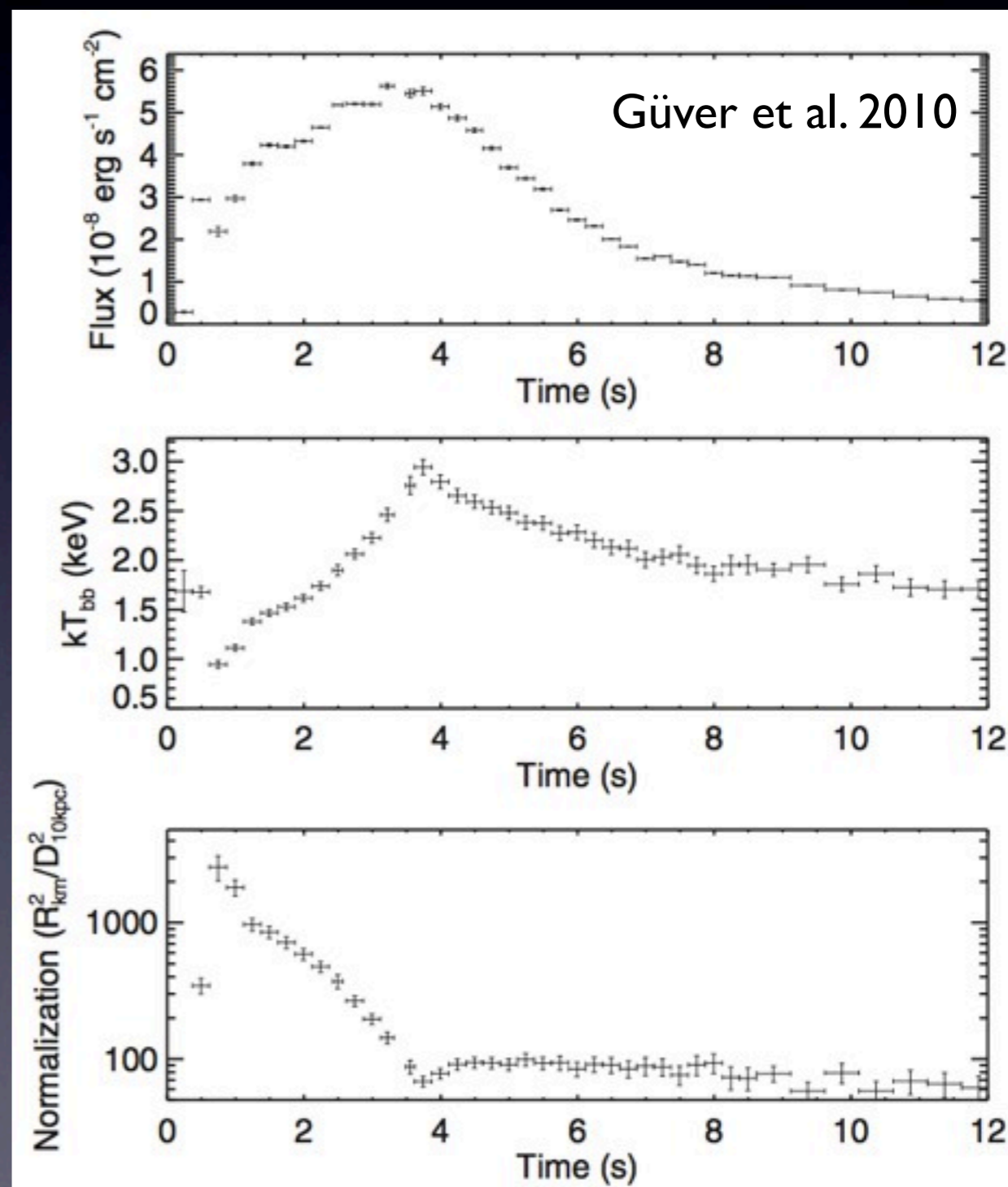
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qLMXBs inside globular clusters are observed with Chandra, and sometimes with XMM-Newton.

Chandra X-Ray Observatory



1" angular resolution

XMM-Newton

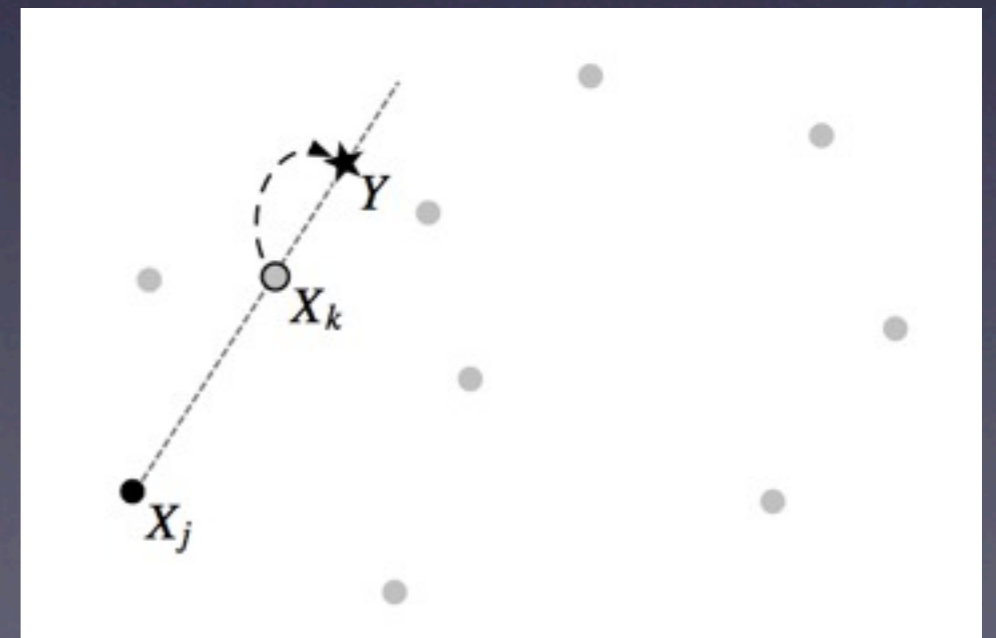


6" angular resolution  
4x more effective area  
than Chandra

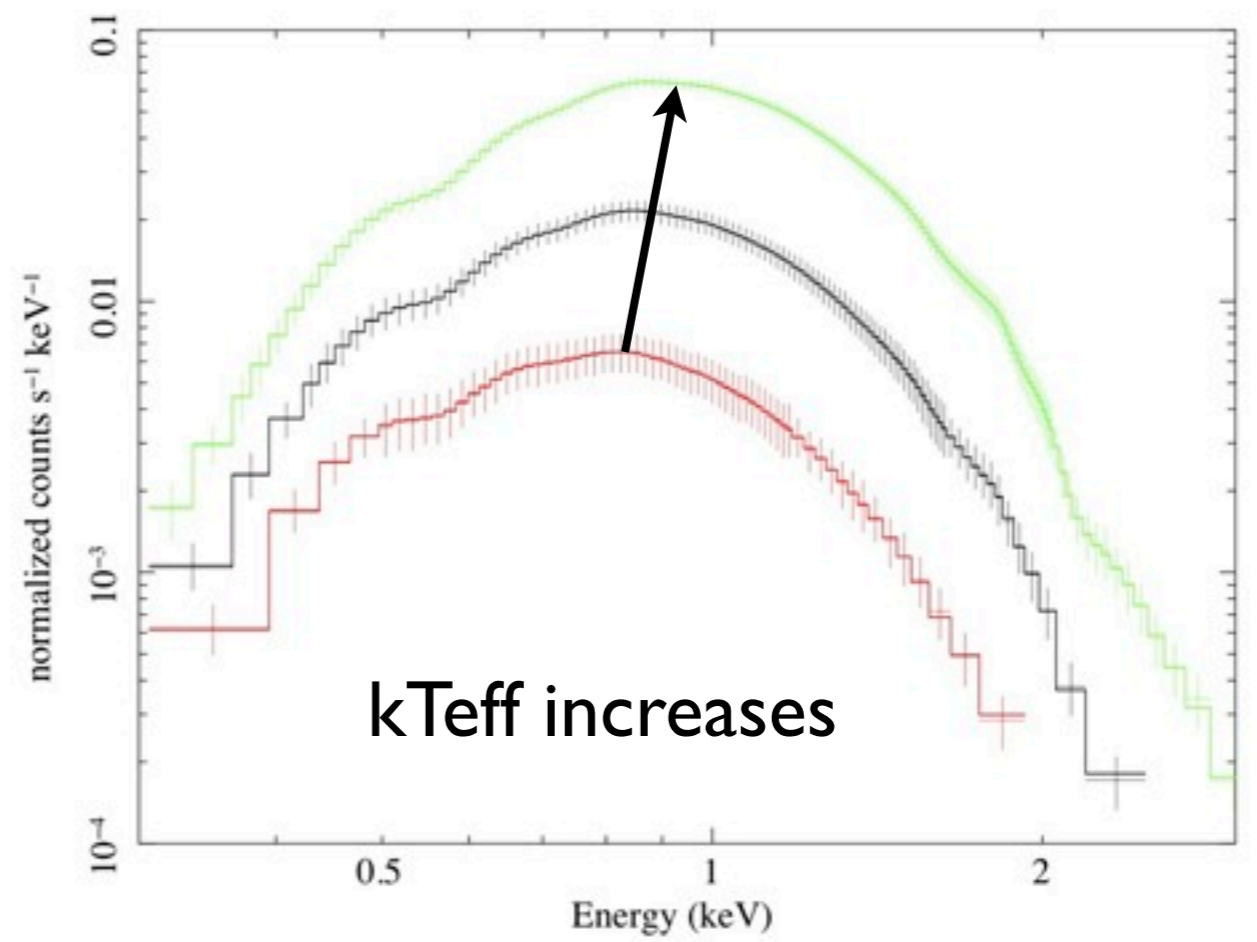
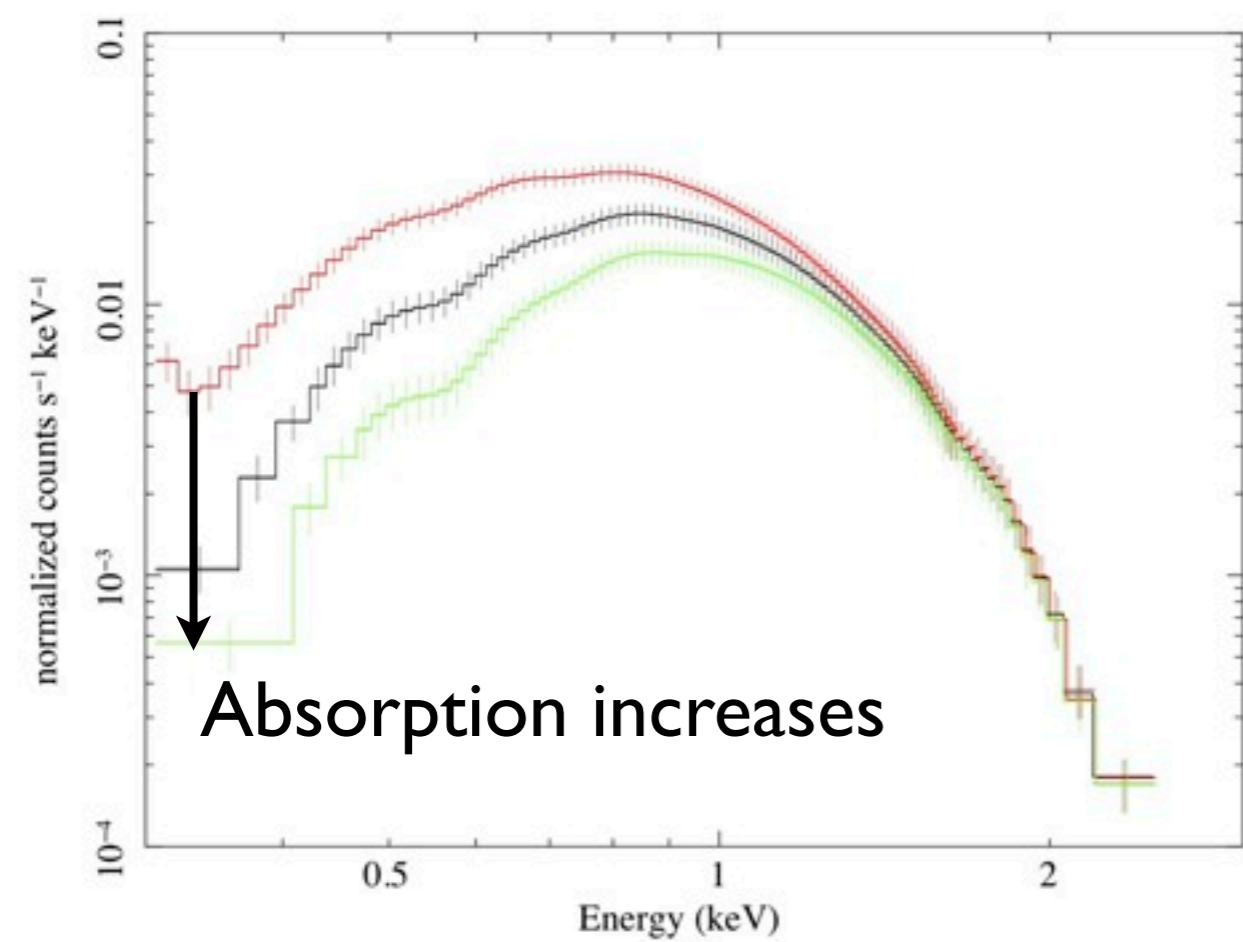
# A Markov Chain Monte Carlo approach is best for error estimation, and the addition of Bayesian priors.

- Because one cannot easily find the global minimum with standard  $\chi^2$  minimization technique
- Because one can include Bayesian priors for the distances
- Because one can easily obtain the marginalized posterior distribution for each parameter

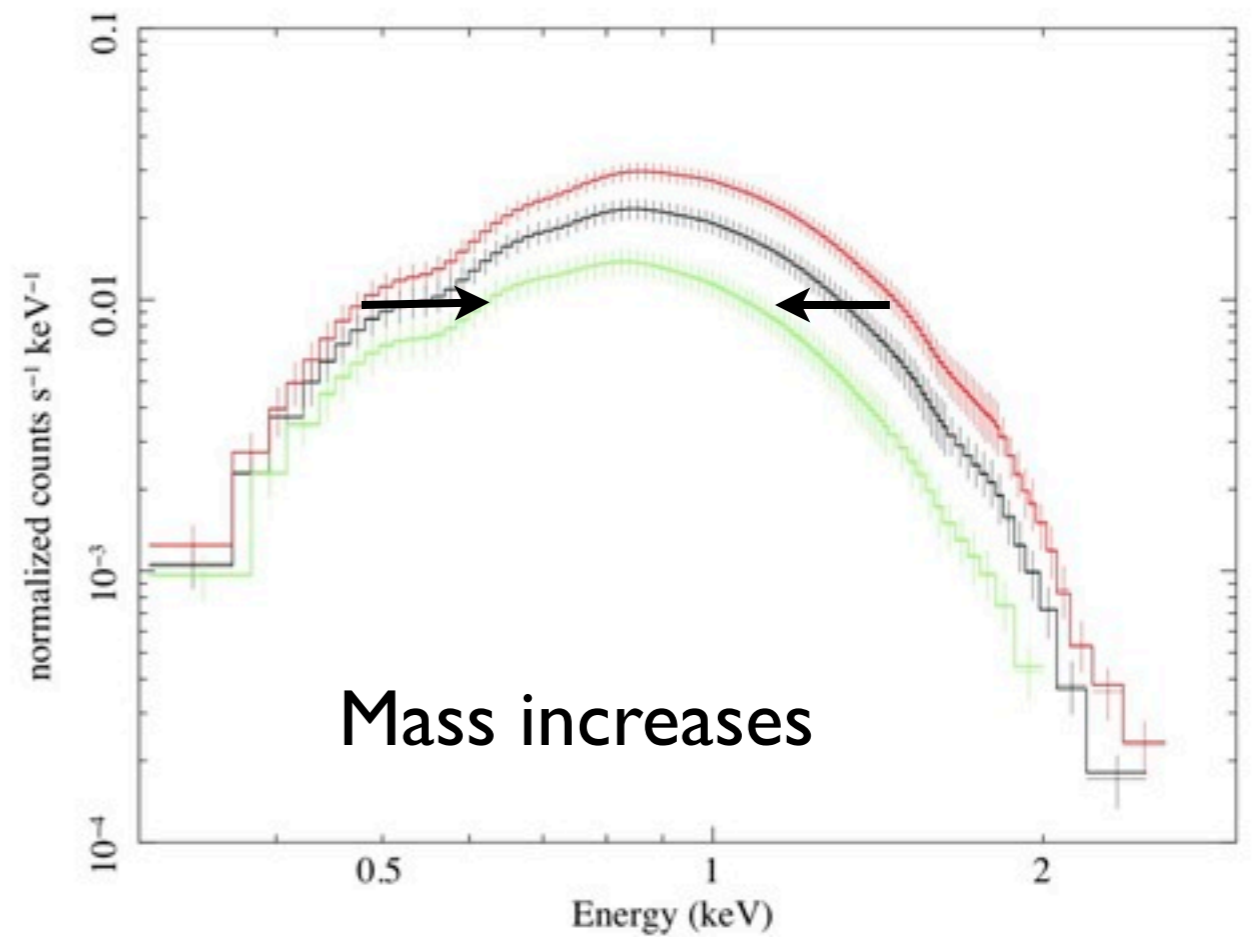
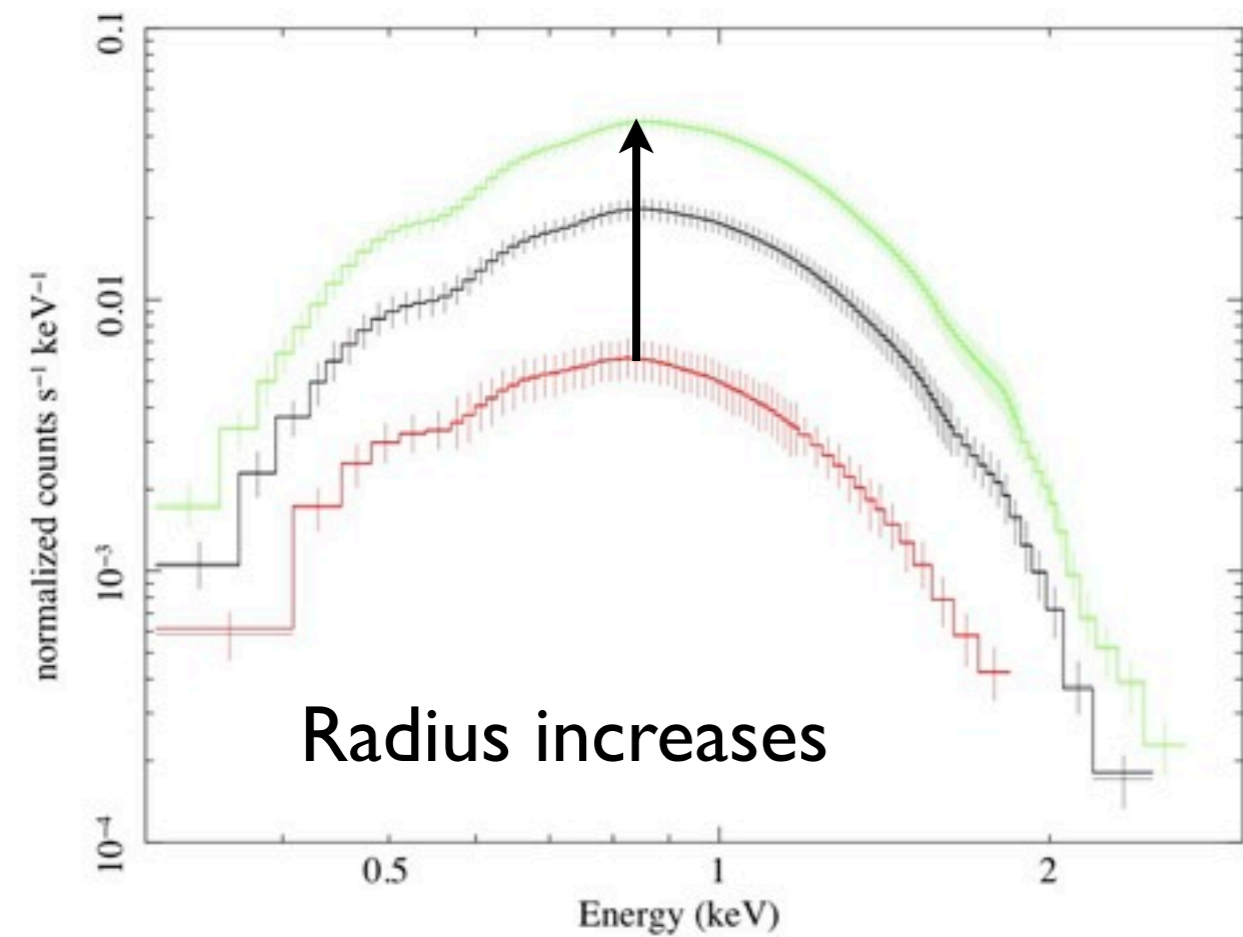
We use the “Stretch-Move” algorithm, instead of Metropolis-Hasting, because it is more appropriate (faster convergence) for elongated and curved distributions





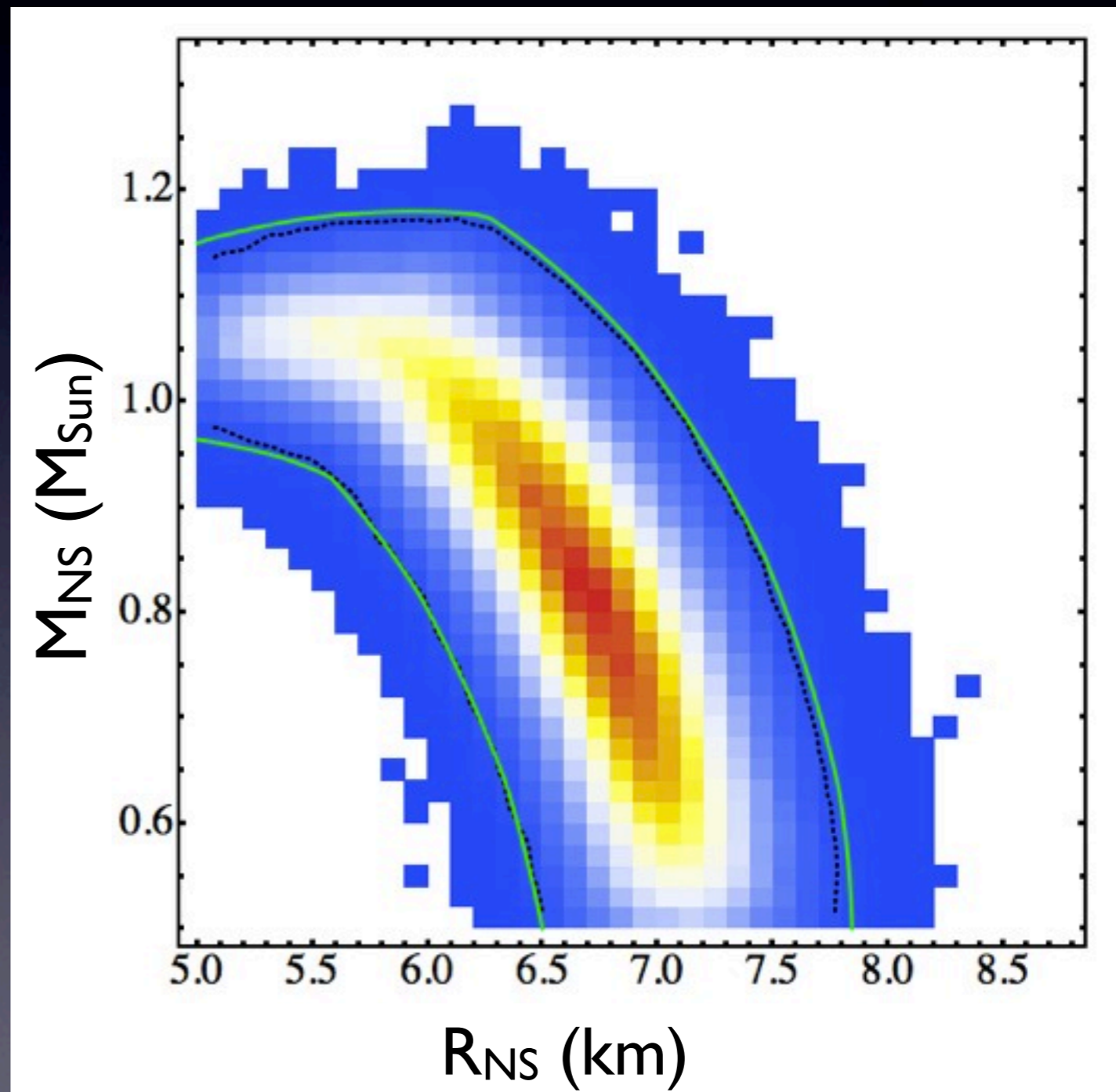


**Neutron stars properties are extracted from the spectra.**



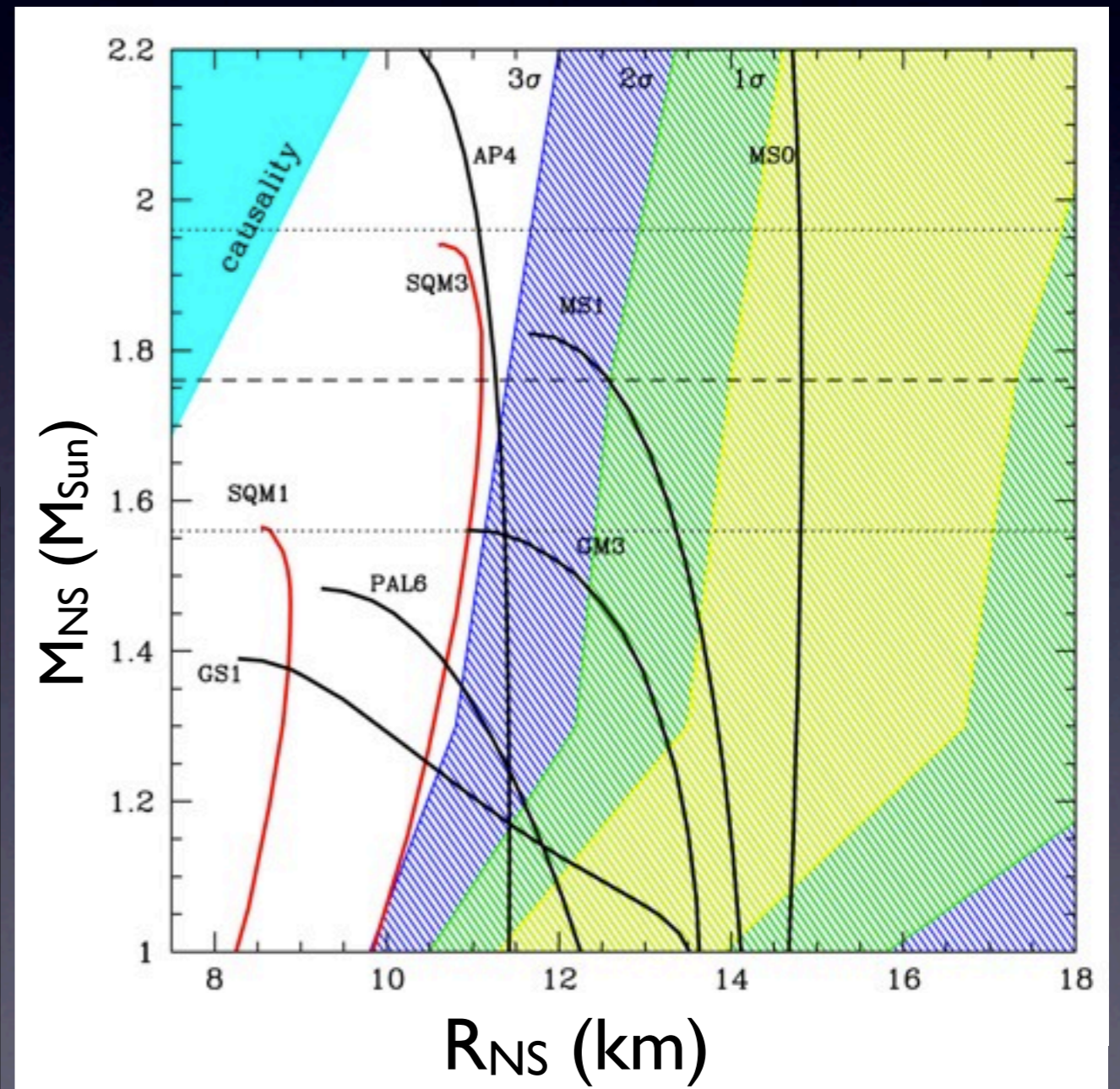
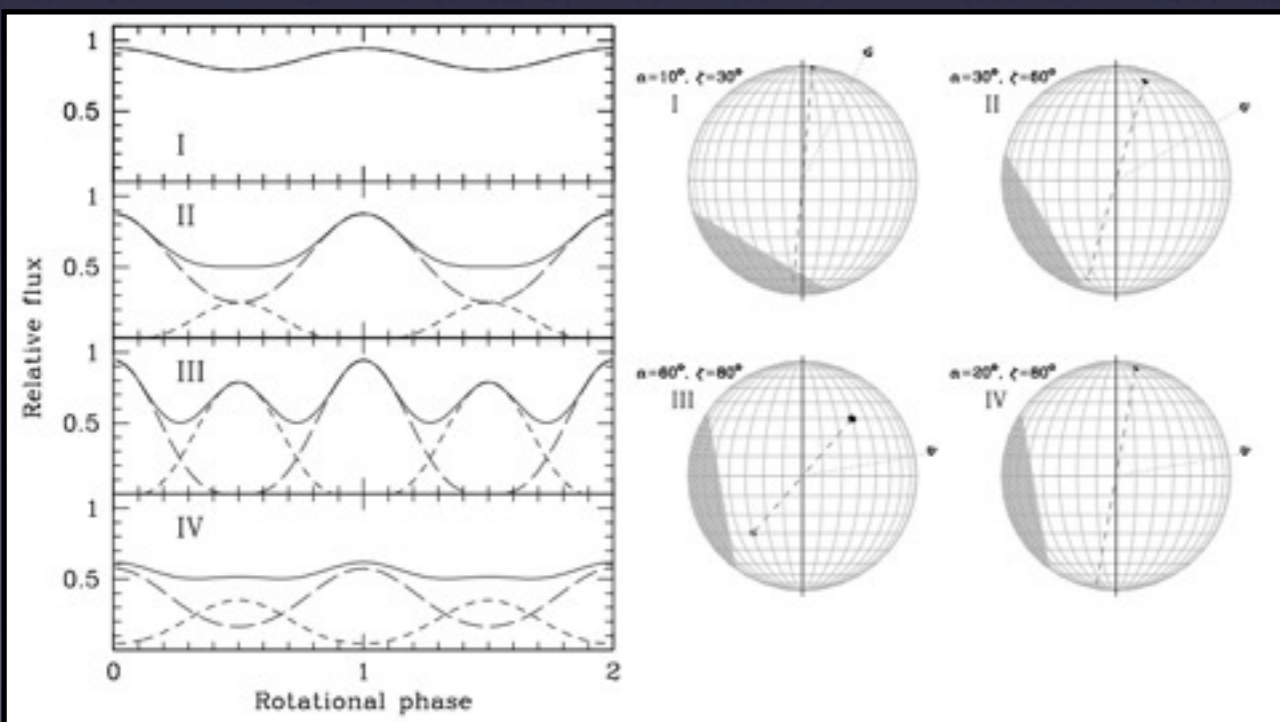
# Markov Chain Monte Carlo Simulations

The MCMC approach is first tested with one single qLMXB, to compare the results to the standard fitting with  $\chi^2$  Levenberg-Marquardt minimization



# Constraints from Neutron Star Observations

- Pulse-timing analysis of millisecond pulsars (Bogdanov et al. 2008, Bogdanov 2012)

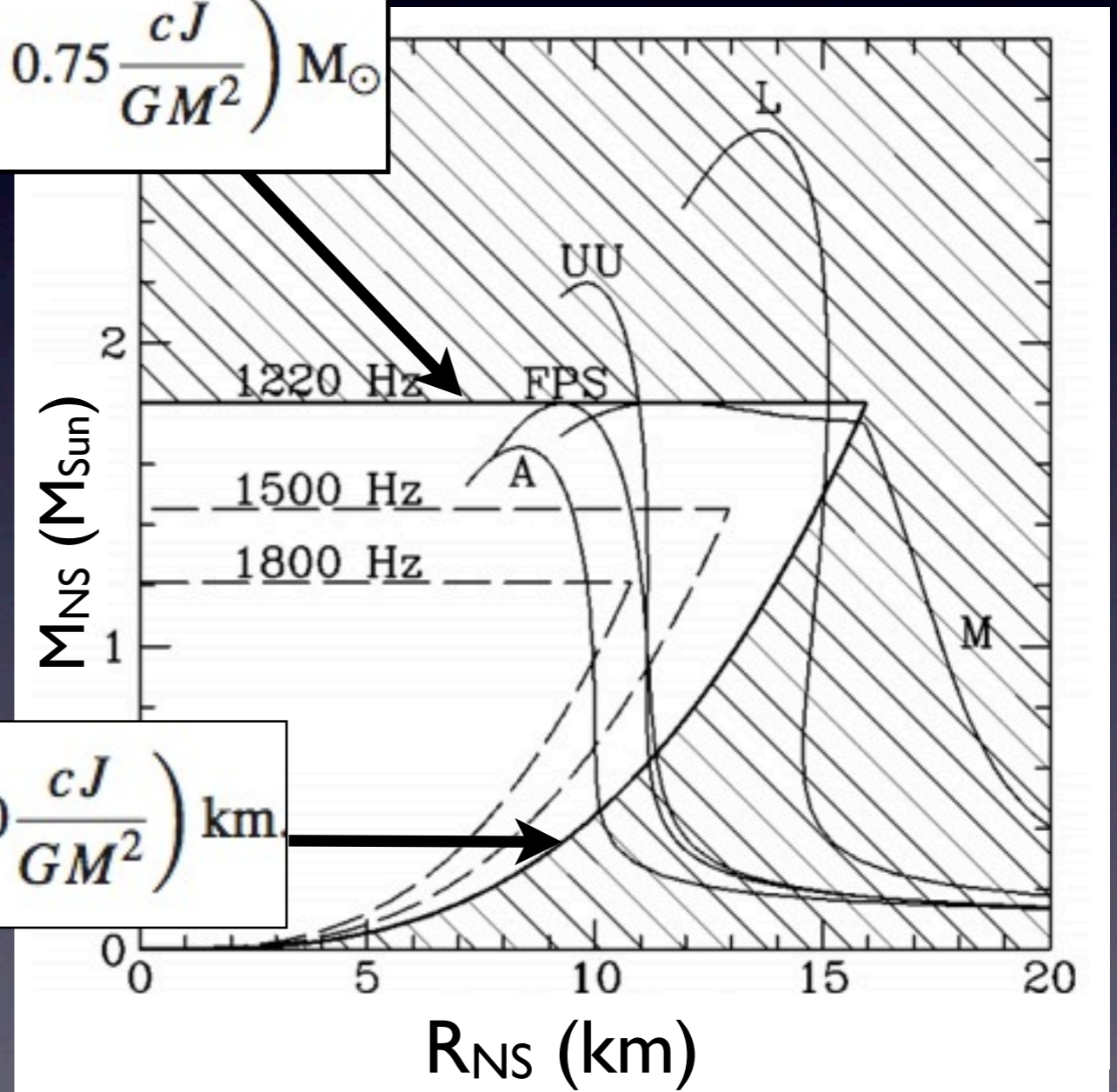


# Constraints from Neutron Star Observations

$$M \leq \left( \frac{2200 \text{ Hz}}{\nu_{\text{ISCO}}} \right) \left( 1 + 0.75 \frac{cJ}{GM^2} \right) M_{\odot}$$

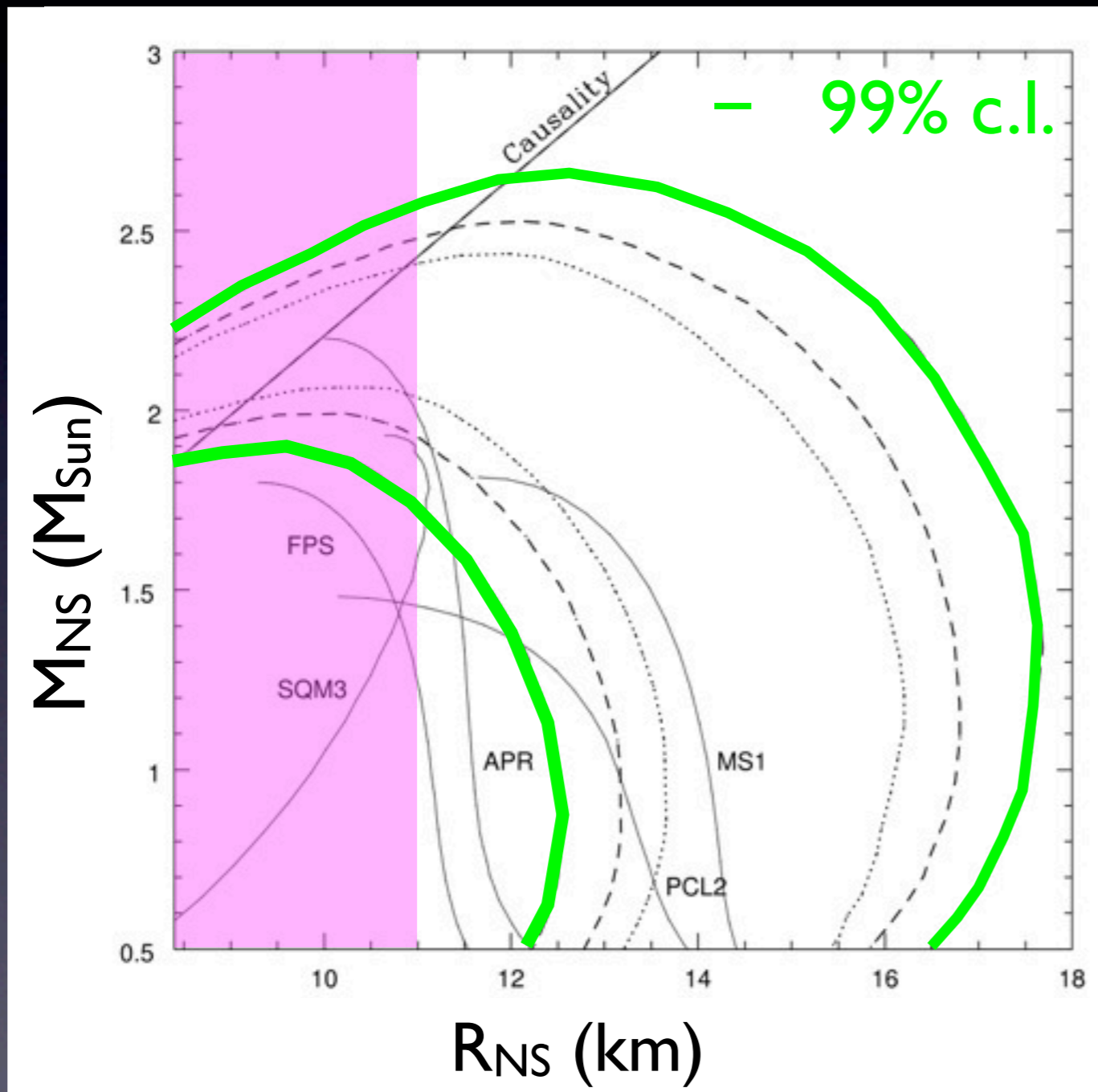
- Quasi-periodic oscillations in active binaries (Miller 1998, Méndez & Belloni 2007)

$$R \leq \left( \frac{1950 \text{ Hz}}{\nu_{\text{ISCO}}} \right) \left( 1 + 0.20 \frac{cJ}{GM^2} \right) \text{ km}$$



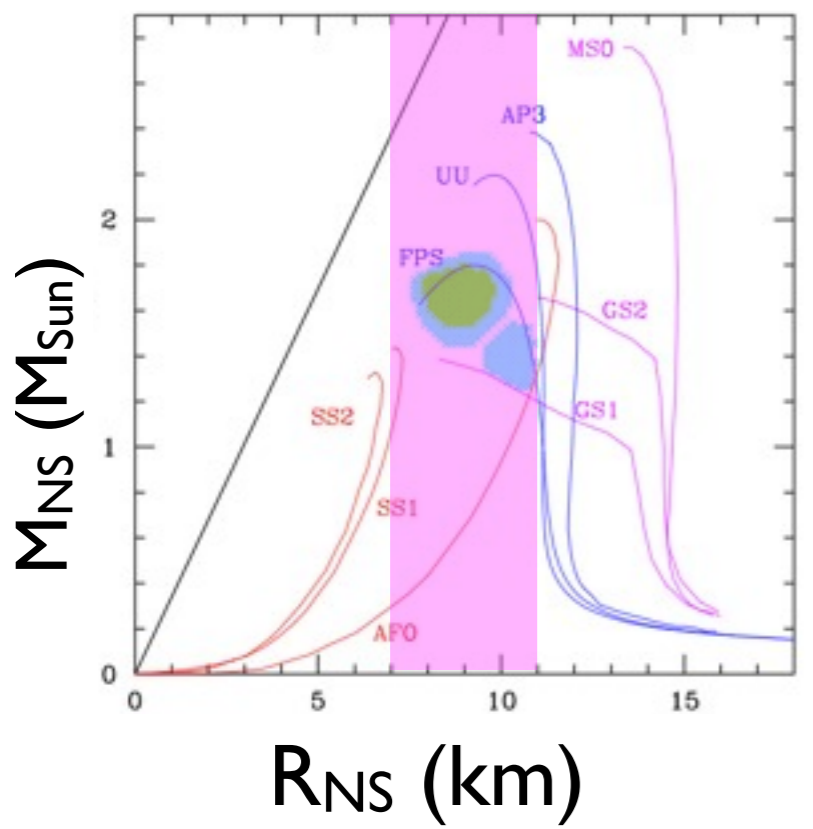
van der Klis 2000

# Previous $R_{NS}$ measurements

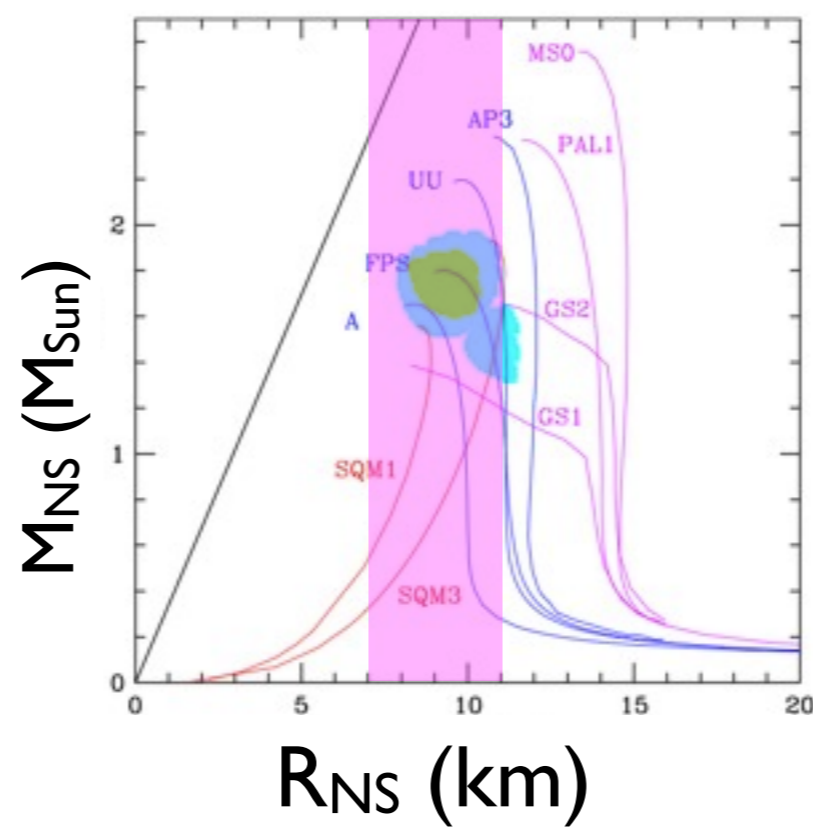


QLMXB 47Tuc X7 not used in our analysis because of a large pile-up fraction, with un-quantified uncertainties.

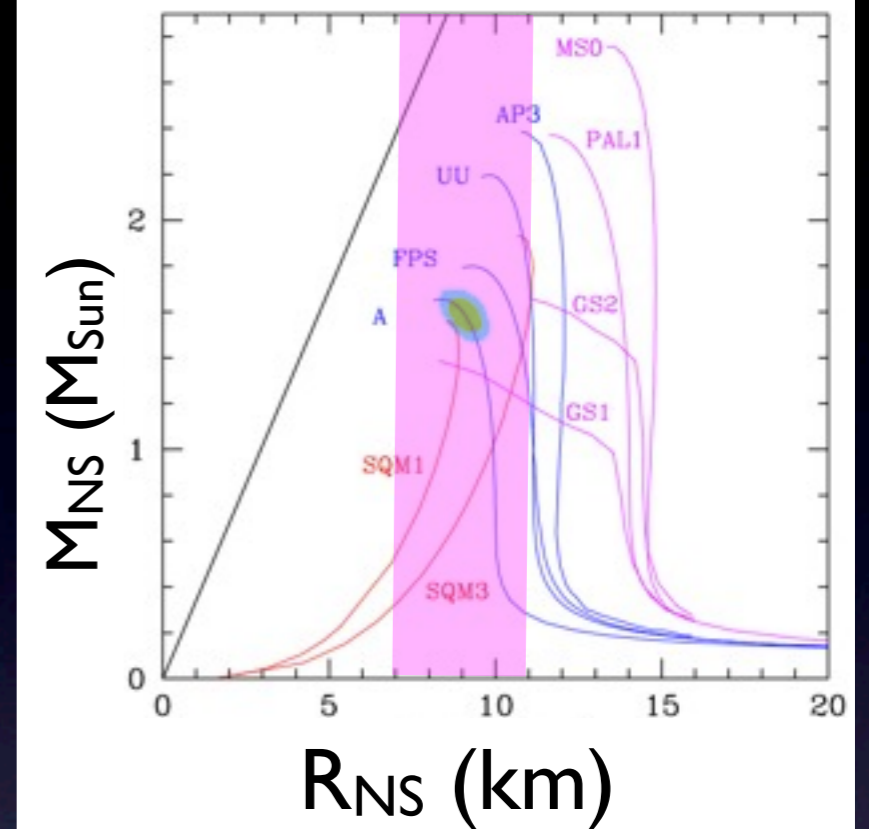
# Previous Rns measurements



EXO 1745-348  
Özel et al. 2009



4U 1608-53  
Güver et al. 2010a



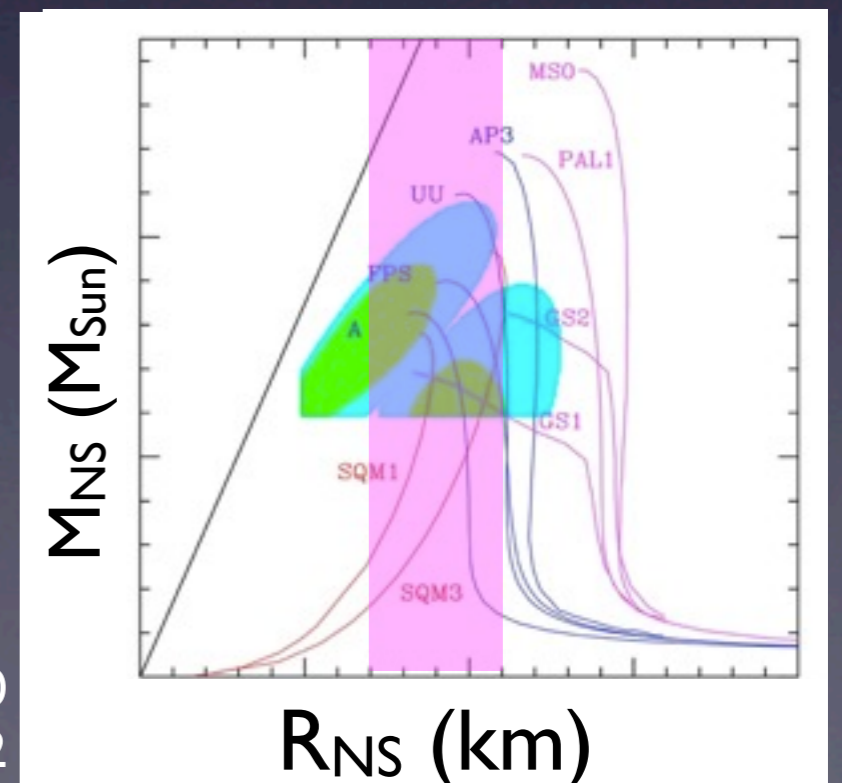
4U 1820-30  
Güver et al. 2010a

Type-I X-ray  
bursts with  
photospheric  
radius expansion  
(PRE)

$$F_{\text{Edd}} = \frac{GMc}{k_{\text{es}}D^2} \left(1 - \frac{2GM}{Rc^2}\right)^{1/2}$$

$$A = \frac{R^2}{D^2 f_c^4} \left(1 - \frac{2GM}{Rc^2}\right)^{-1}$$

KS 1731-260  
Özel et al. 2012

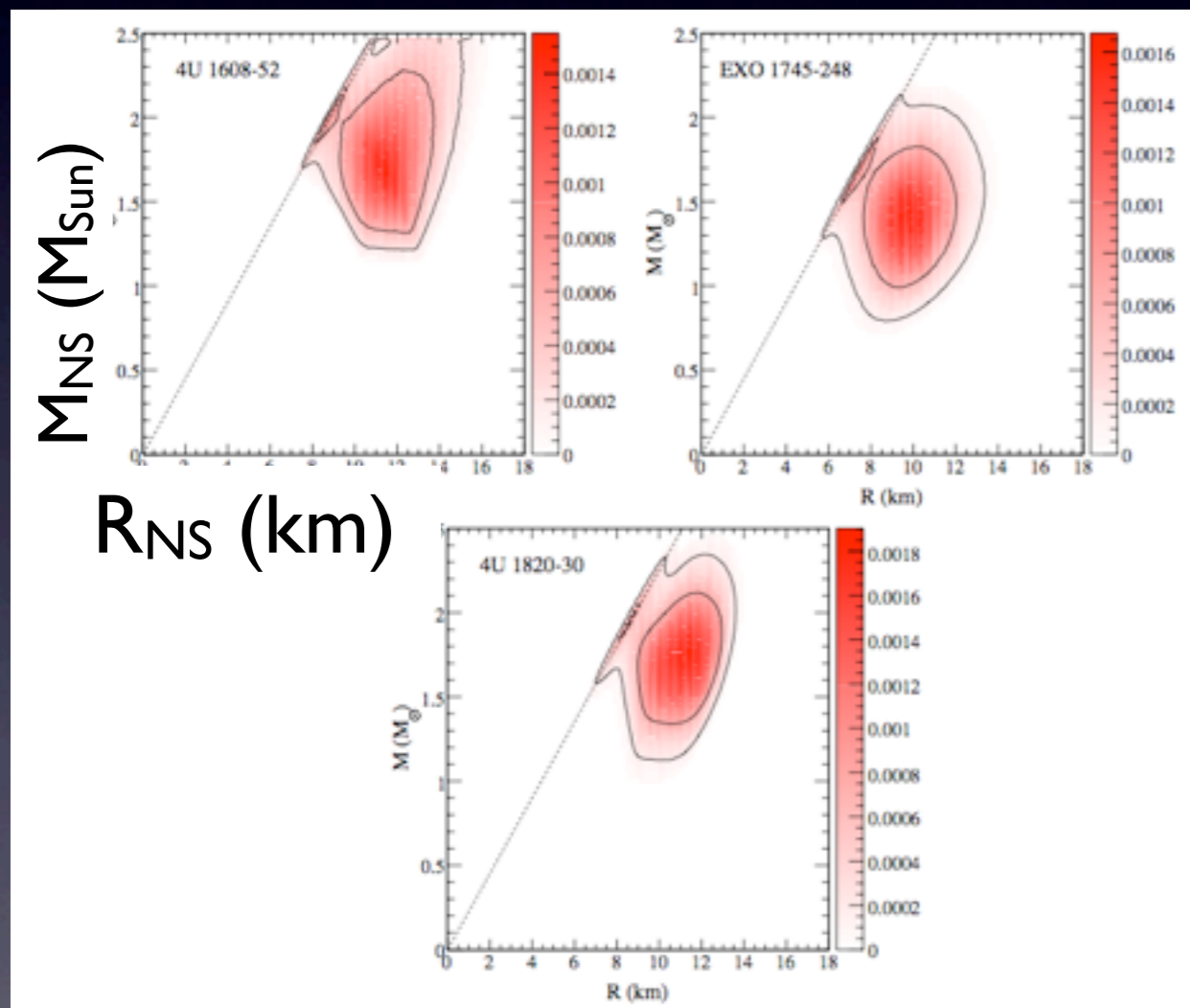


# Combining M-R constraints from neutron stars provides more stringent constraints.

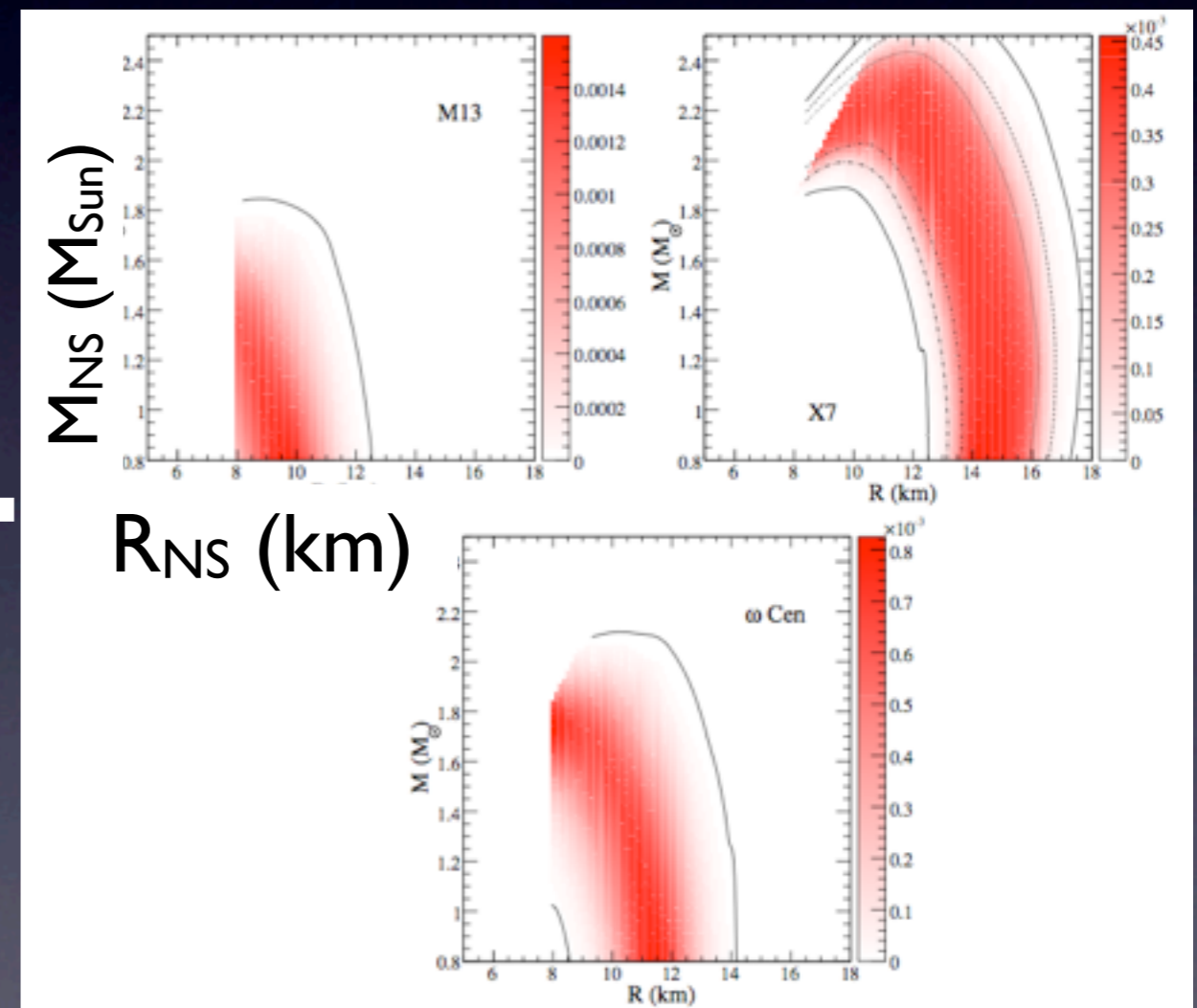
Steiner et al 2010, 2013

Type I X-ray bursts

Quiescent LMXBs



+



+ M-R contour of X-ray burst KSI731-260  
Özel et al. 2012

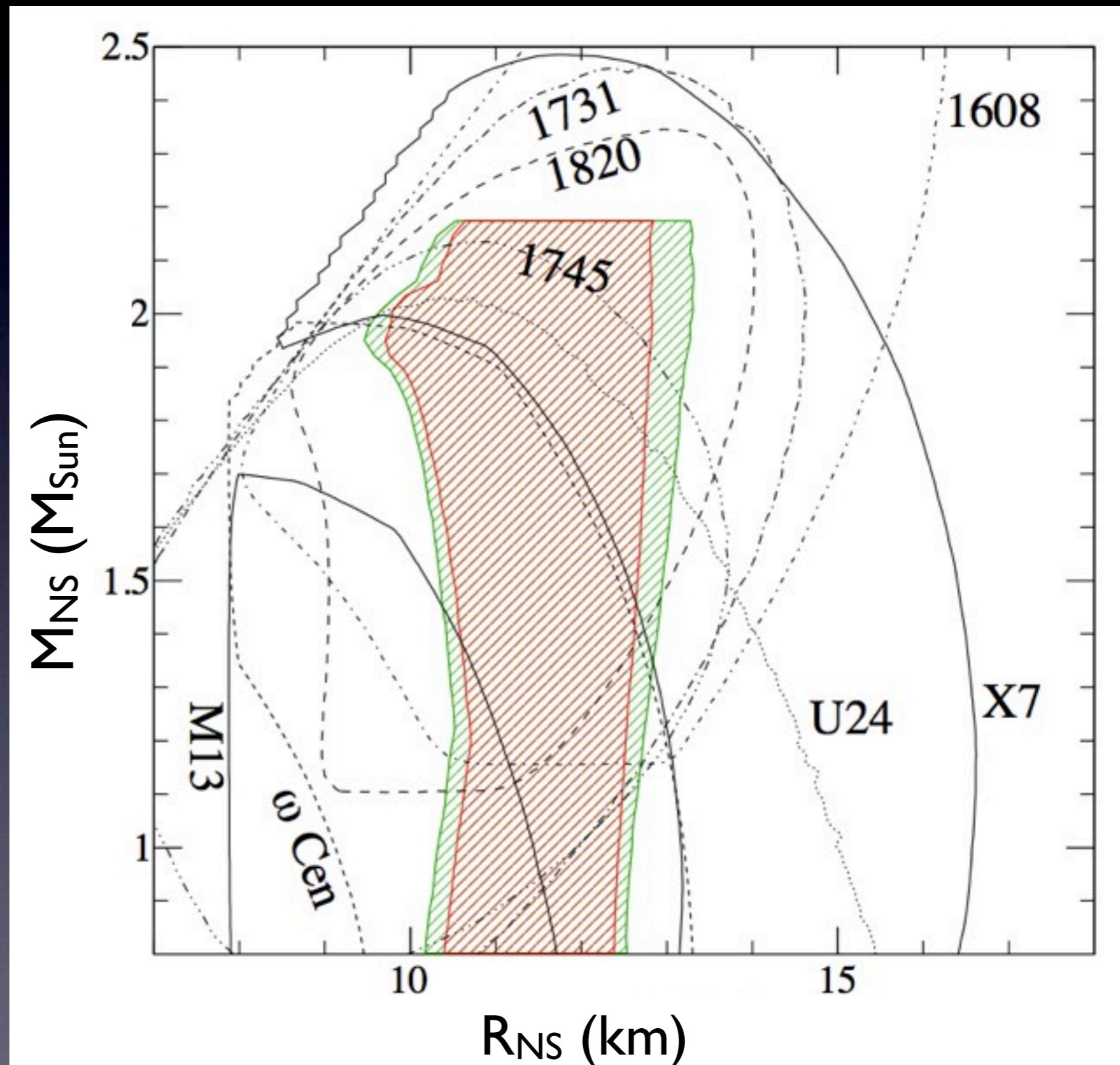
+ M-R contour of qLMXB in NGC6397  
from Guillot et al. 2011

# Combining M-R constraints from neutron stars provides more stringent constraints.

$R_{\text{NS}}$  is constrained between 10 and 13 km for a wide range of masses.

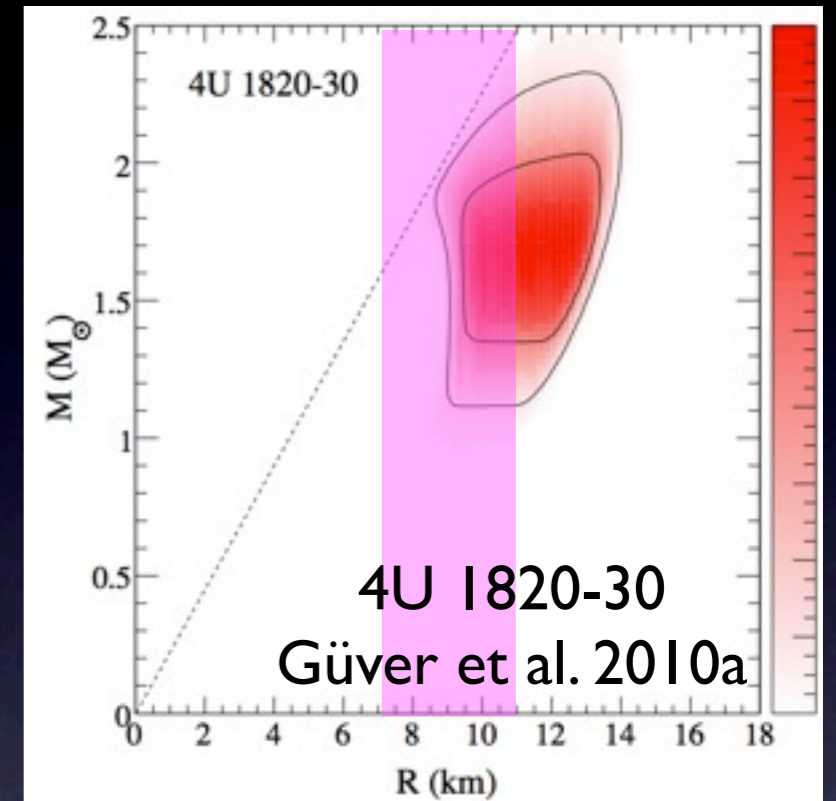
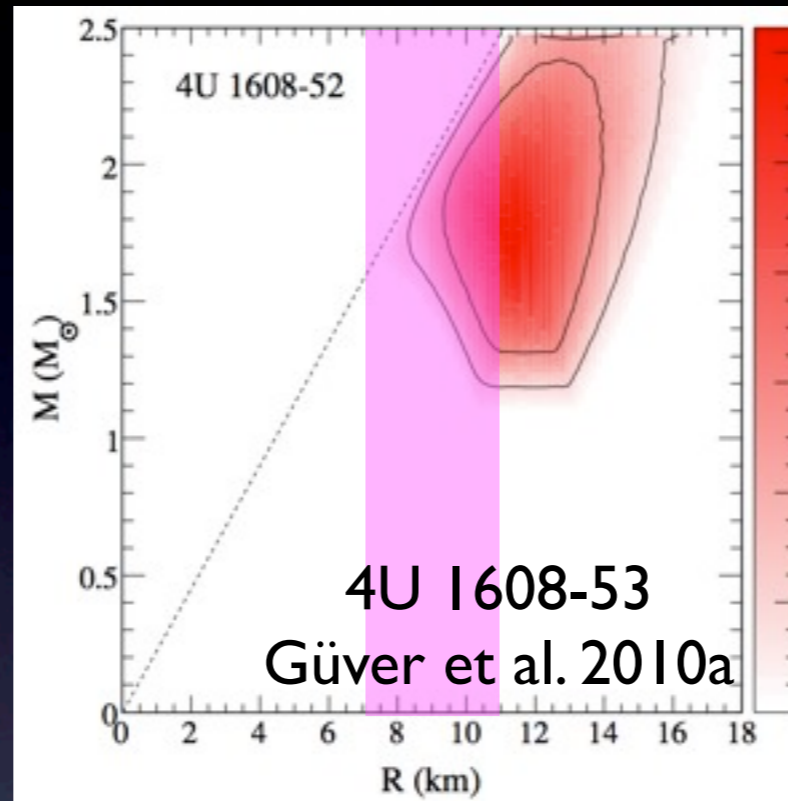
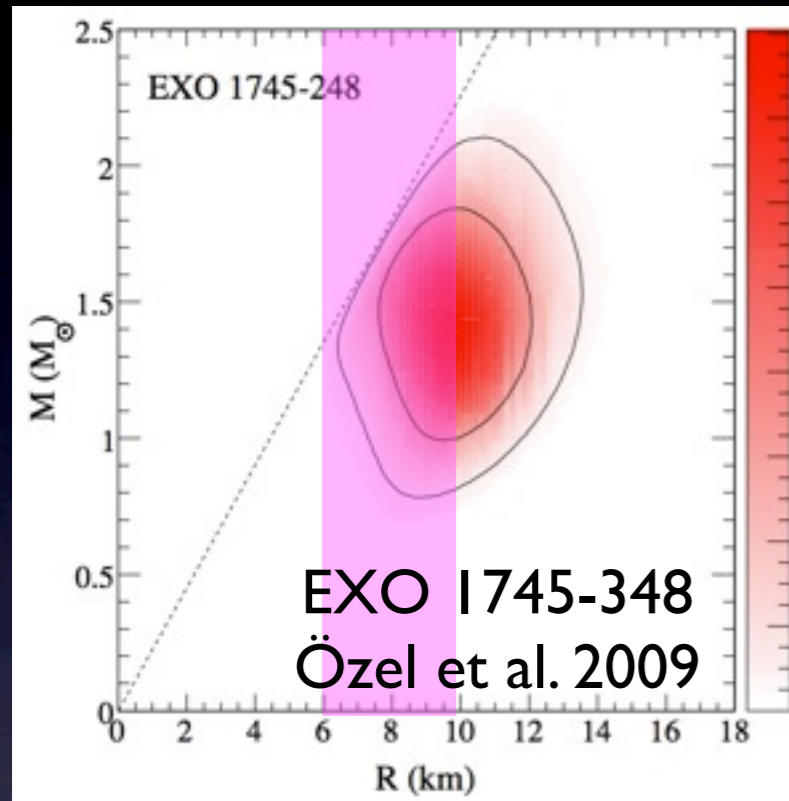
$R_{\text{NS}}$  is insensitive to the exclusion of extremum contours (like M13, or 47Tuc), or to the exclusion of type-I X-ray burst sources.

Steiner et al 2013





# Comparison with previous Rns measurements



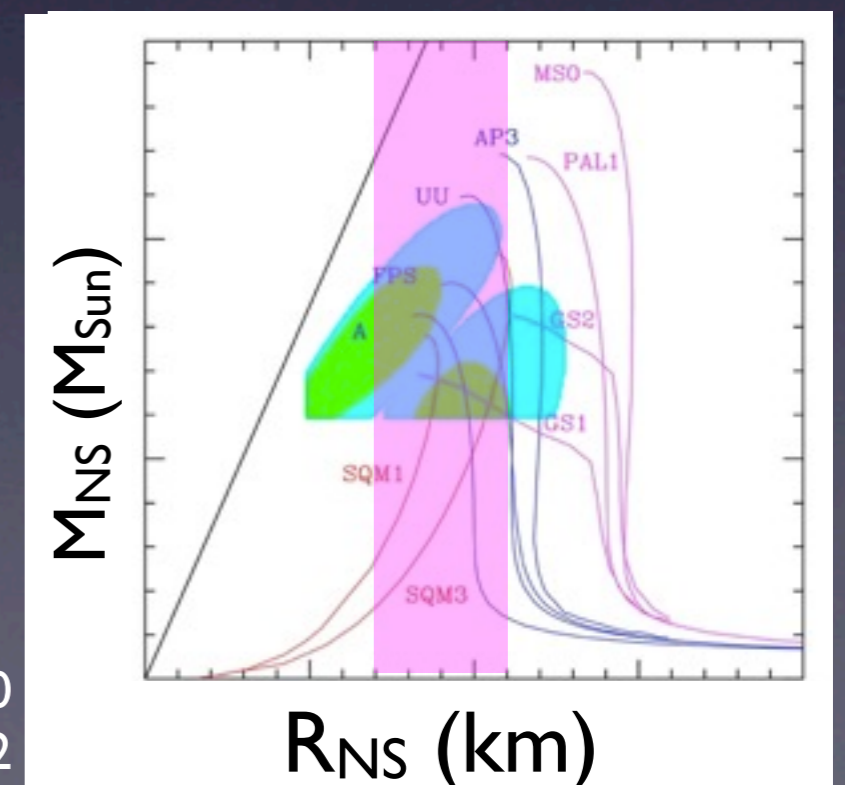
Confidence Region recalculated  
by Steiner et al. 2010

Type-I X-ray bursts  
with photospheric  
radius expansion

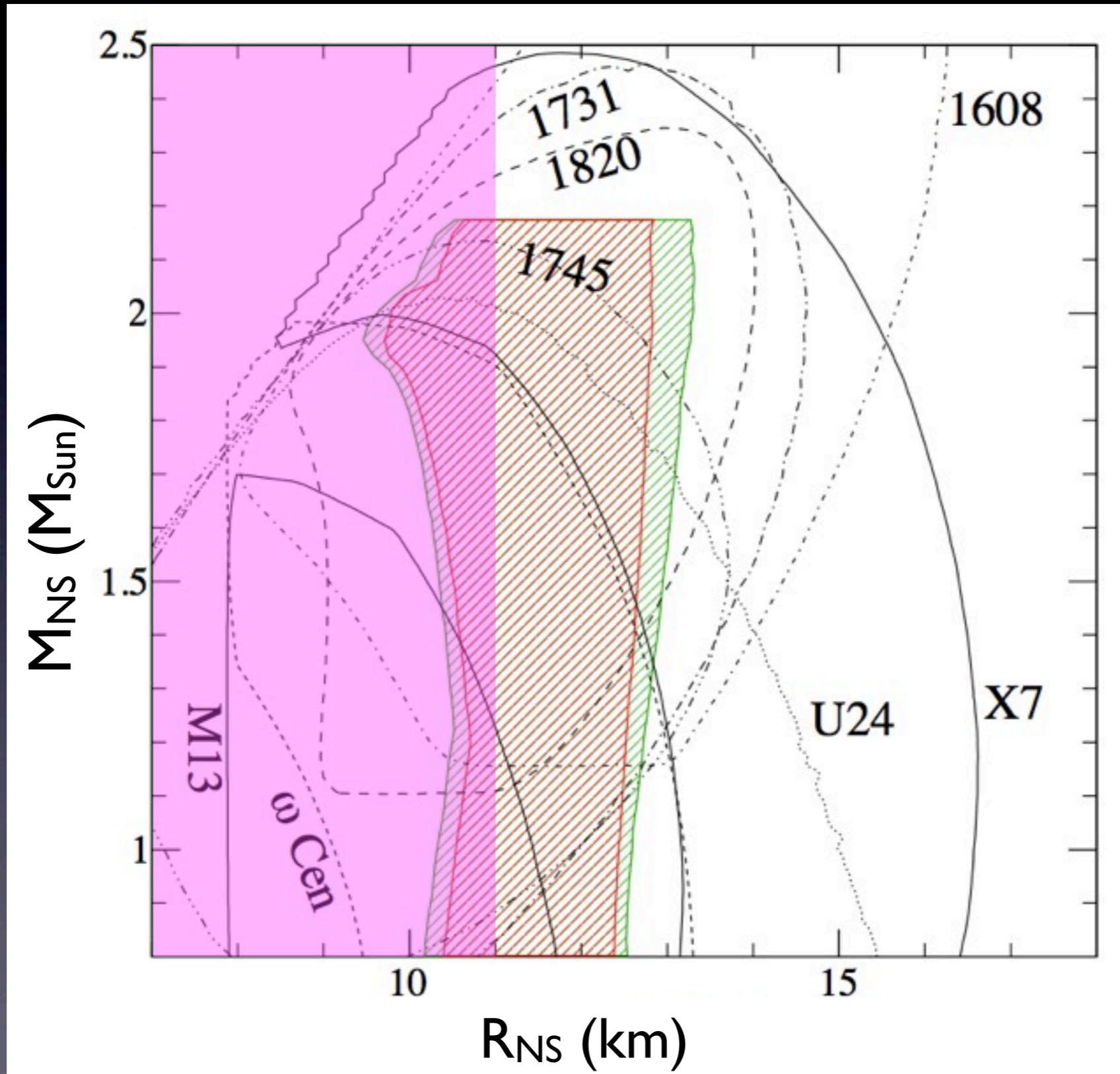
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KS 1731-260  
Özel et al. 2012

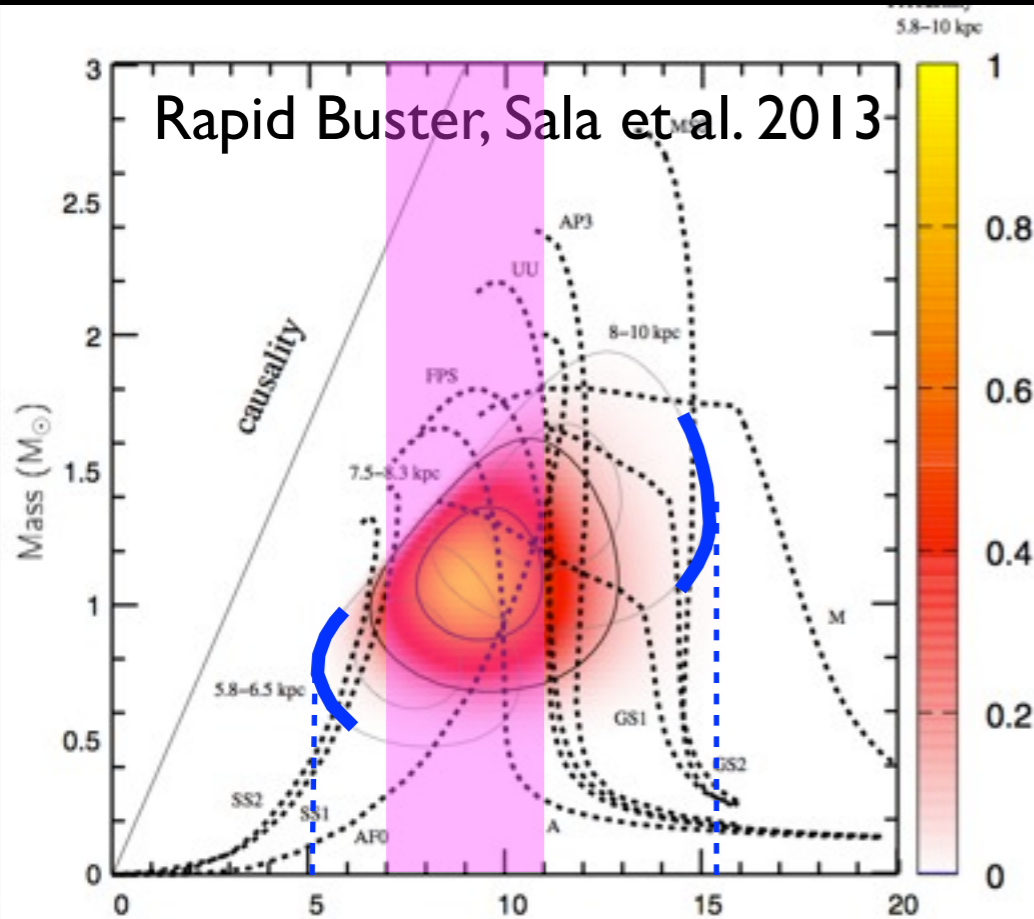


# Empirical Equation of State



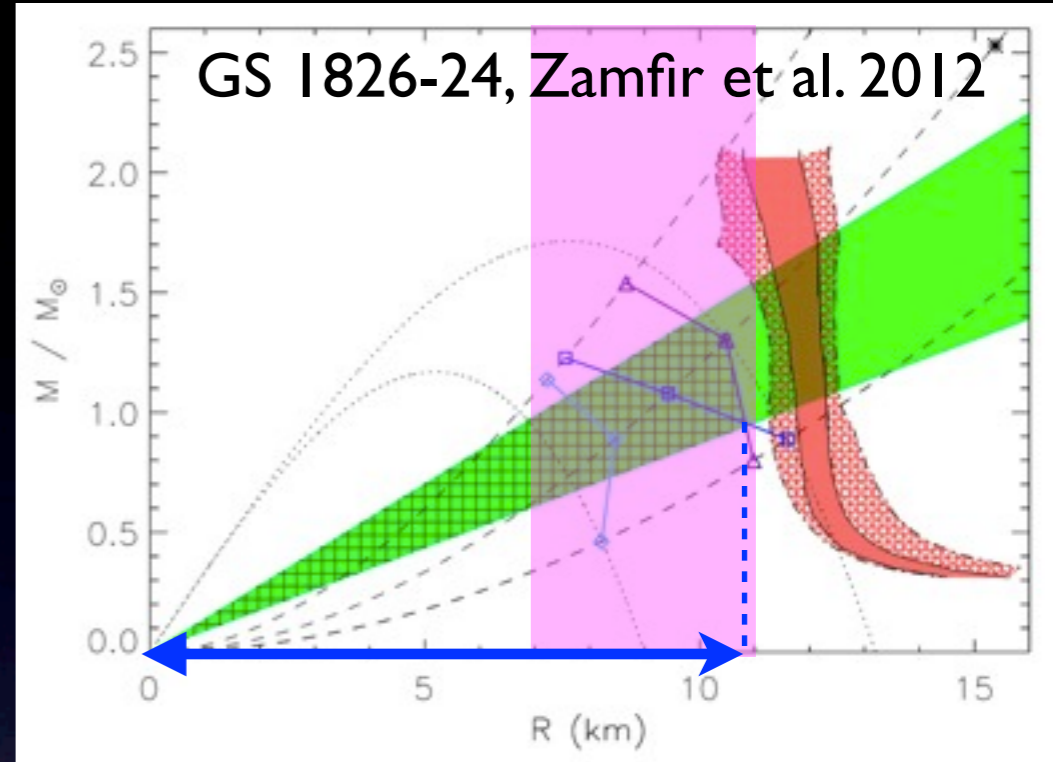
Steiner  
et al  
2013

# Previous Rns measurements

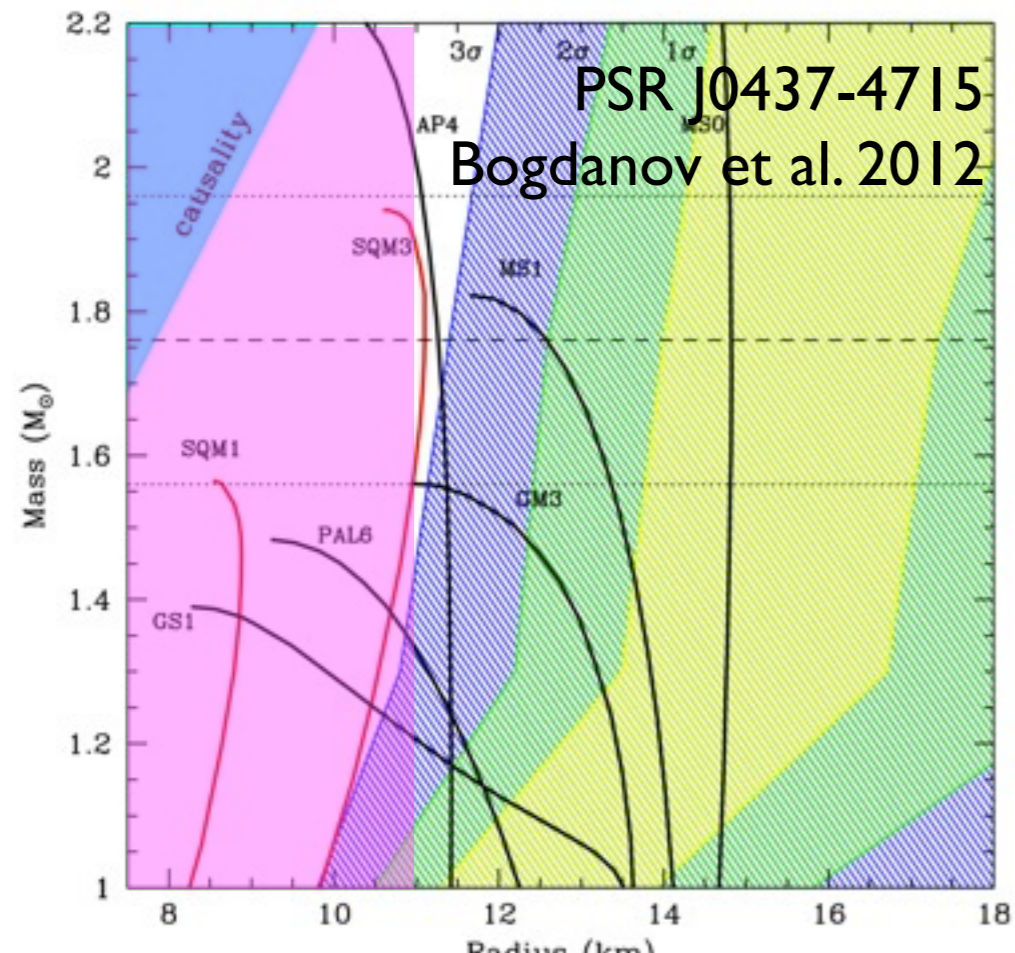


PRE type-I X-ray bursts.

Distance uncertainties seriously affect measurements



Sub-Eddington type-I X-ray bursts  
Distance independent measurement



Pulse timing analysis of a millisecond pulsar

