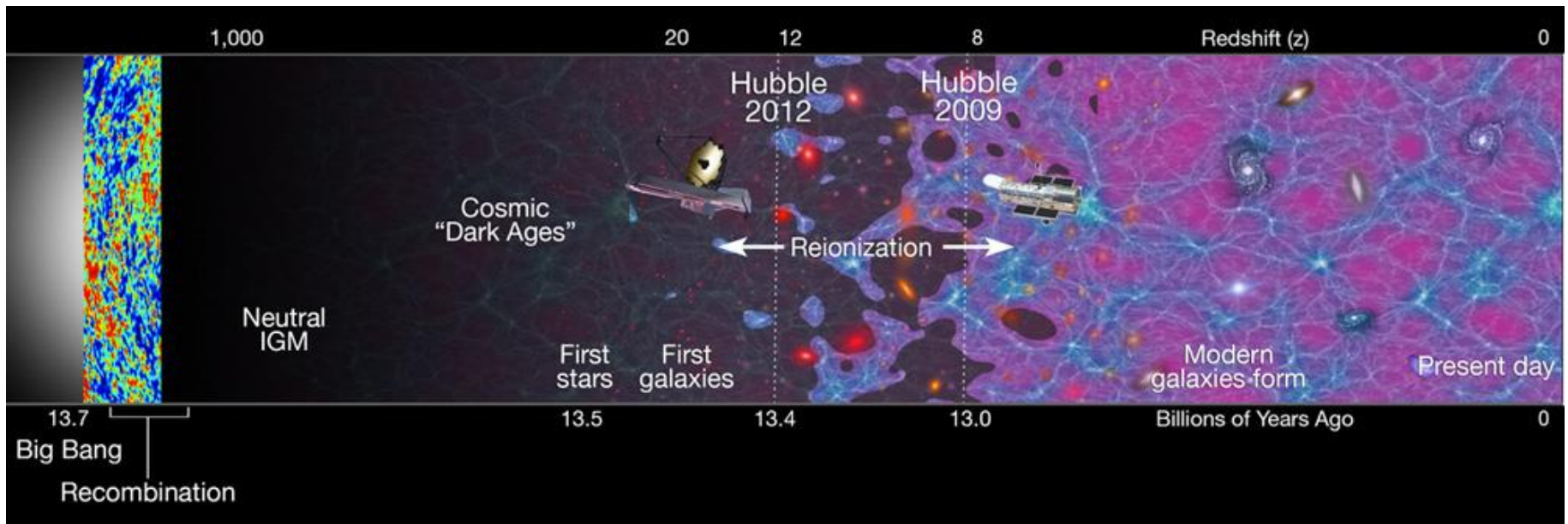


Effect of Lyman Limit Systems and Local Clumping Factor on the History of Cosmic Reionization

Alexander (Sasha) Kaurov
the University of Chicago

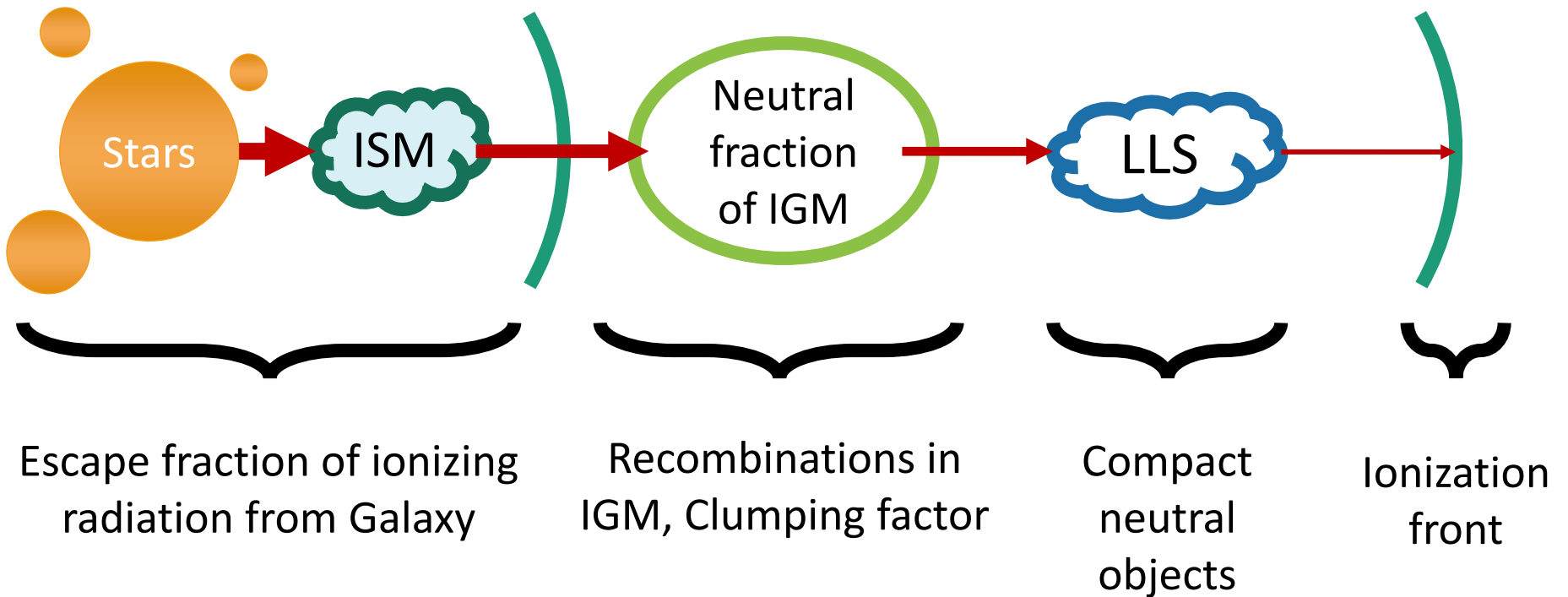
Kaurov & Gnedin (2013a,b)

History of cosmic reionization



Hubble Ultra Deep Field

Absorption of ionizing photons:



Ways to study reionization:

Reionization models

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graph TD; A[Reionization models] --> B[Homogeneous reionization]; A --> C[Inhomogeneous reionization]; B --> D[Analytic models]; C --> E[Semi-analytic and semi-numeric models]; C --> F[Numeric models];
```

Homogeneous reionization

Kuhlen & Faucher-Giguère (2012)

Analytic models

Furlanetto et al. (2004)

Inhomogeneous reionization

Semi-analytic and semi-numeric models

Zahn et al. (2011)

Numeric models

Paul Shapiro's talk

Ways to study reionization:

Reionization models

Homogeneous reionization

Kuhlen & Faucher-Giguère (2012)

Inhomogeneous reionization

Analytic models

Furlanetto et al. (2004)

Semi-analytic and semi-numeric models

Zahn et al. (2011)

Numeric models

Paul Shapiro's talk

How analytic model works?

Halo mass function

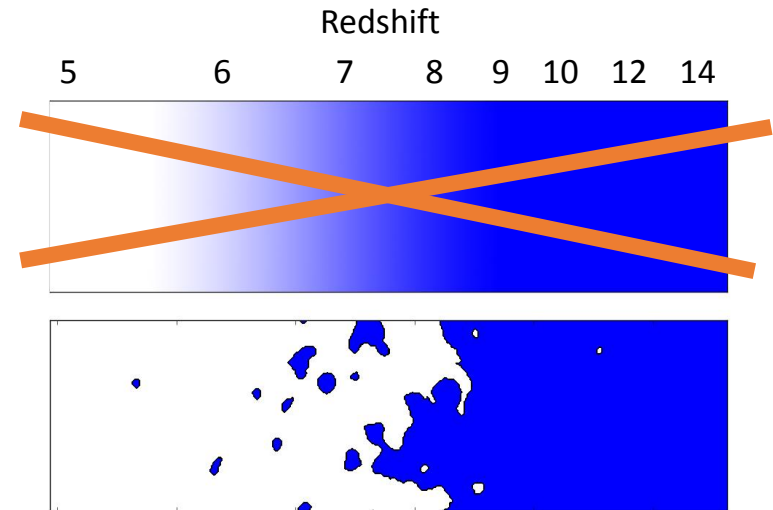
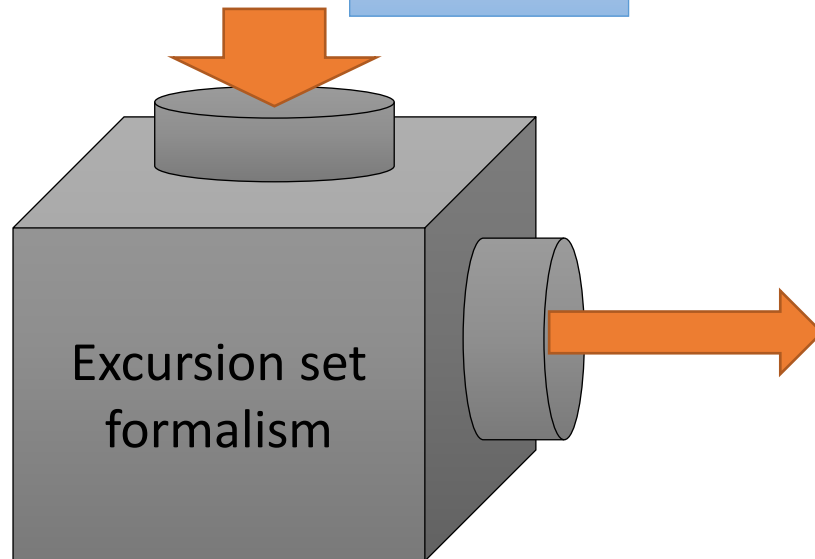
Lyman Limit Systems

Luminosity function

Clumping factor

Escape fraction

Halo bias



How analytic model works?

Halo mass function

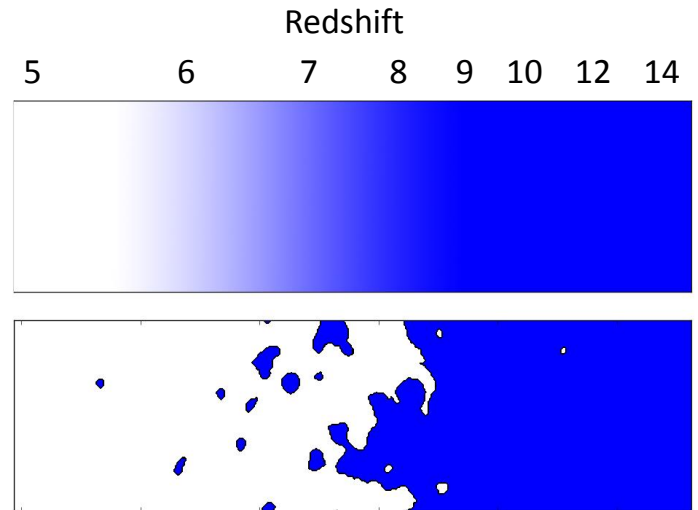
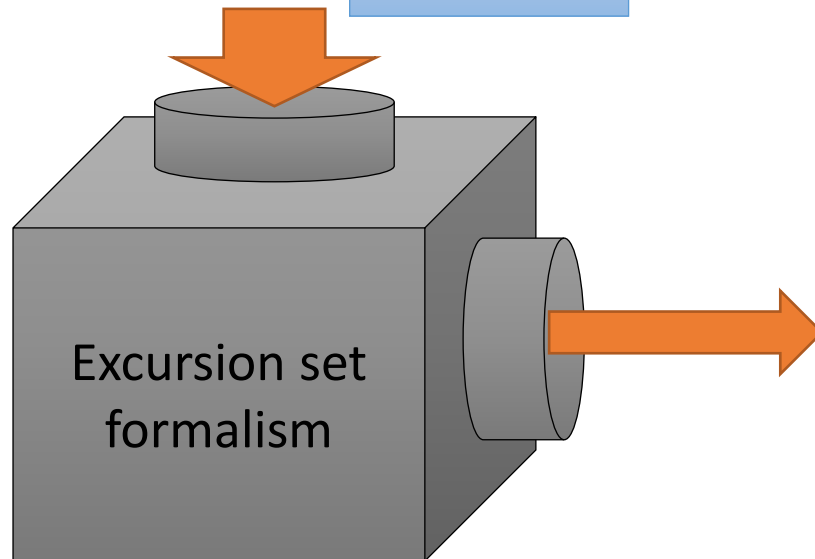
Lyman Limit Systems

Luminosity function

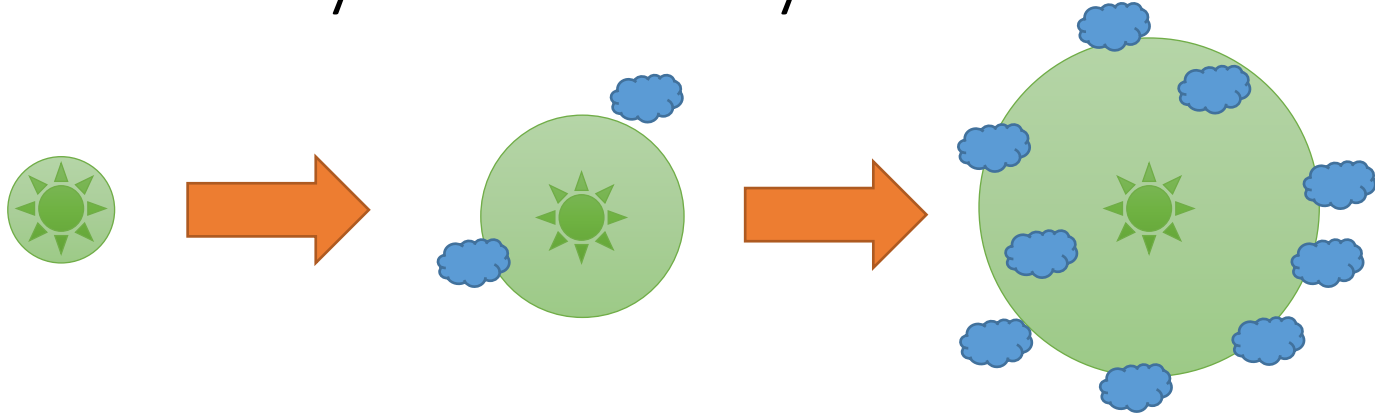
Clumping factor

Escape fraction

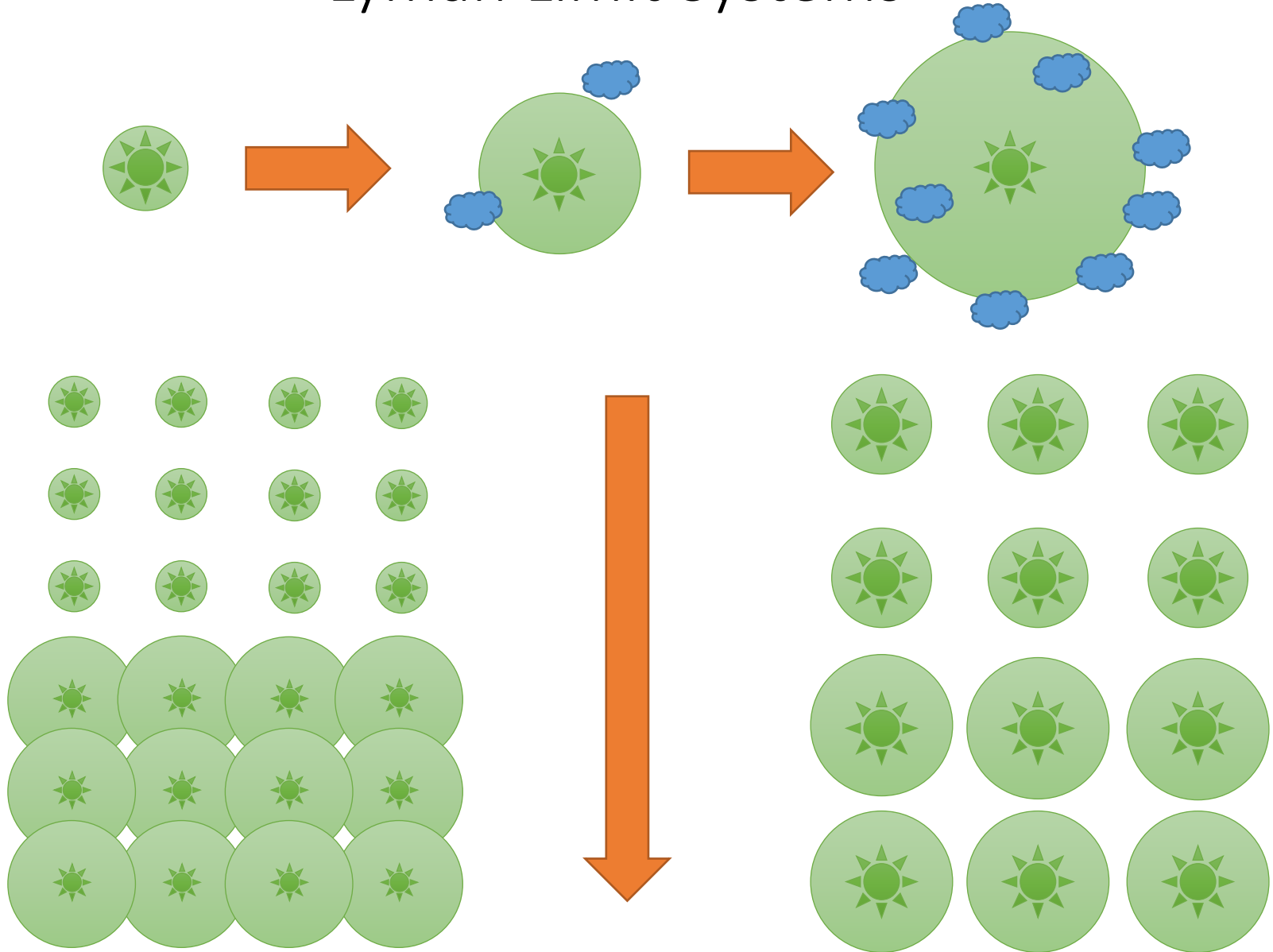
Halo bias



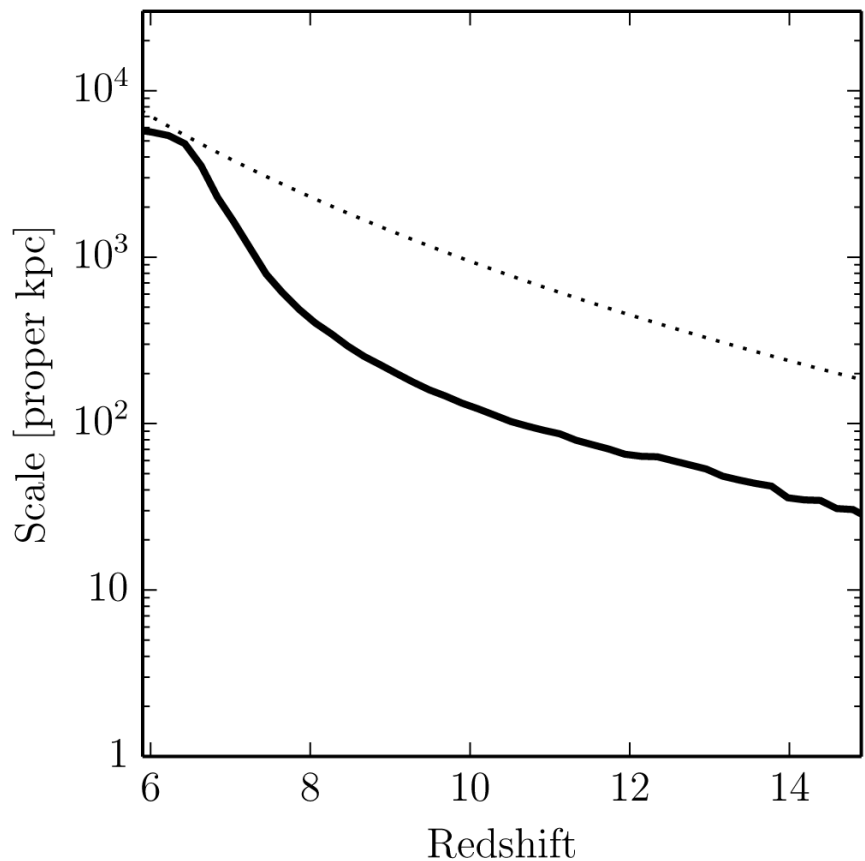
Lyman Limit Systems



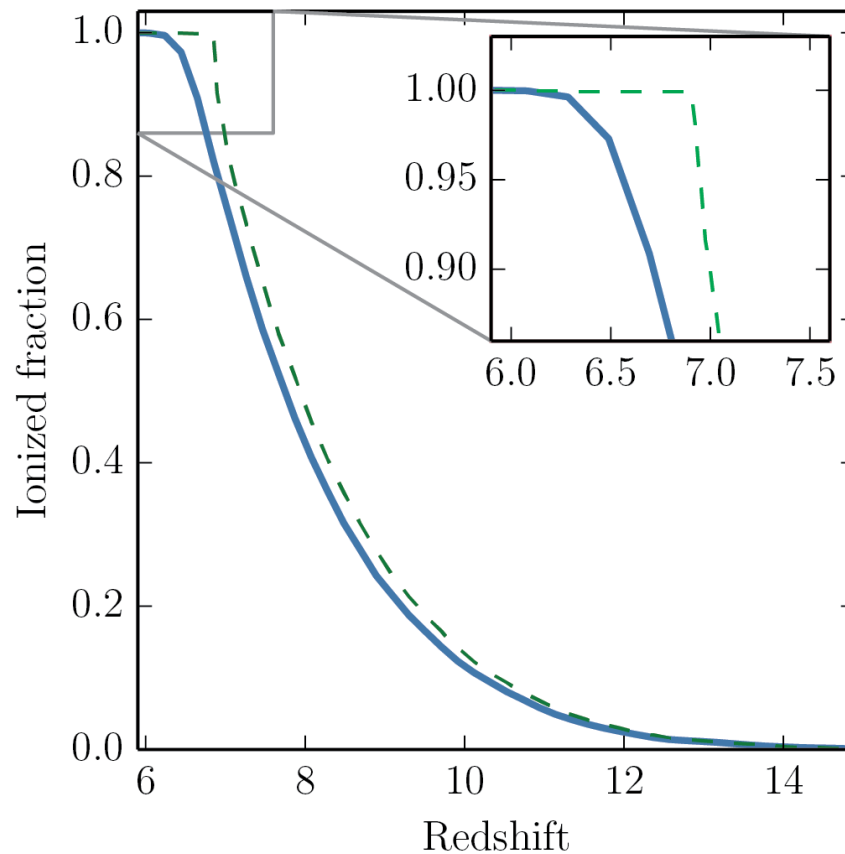
Lyman Limit Systems



Effect of Lyman Limit Systems

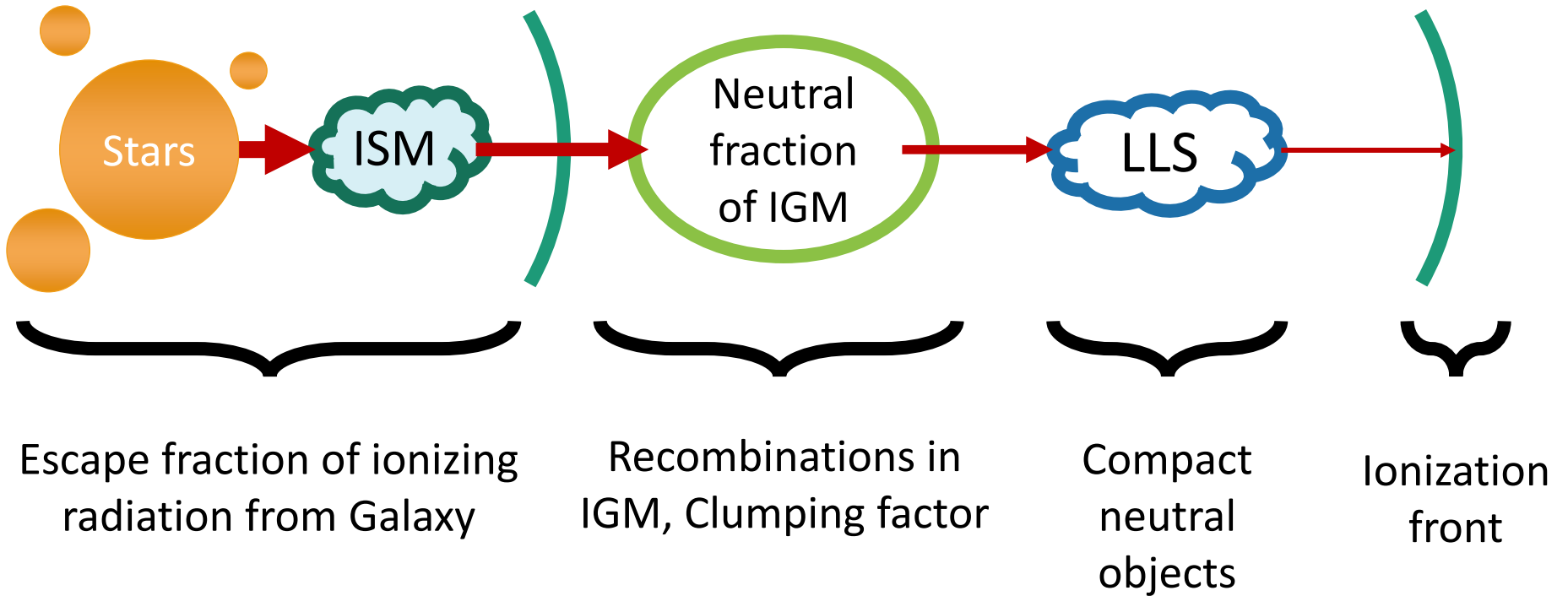


LLS mean free path
 Characteristic distance to ionization front



Without LLS
 Including LLS

Absorption of ionizing photons:



Clumping factor

- Number of ionizations per hydrogen atom:

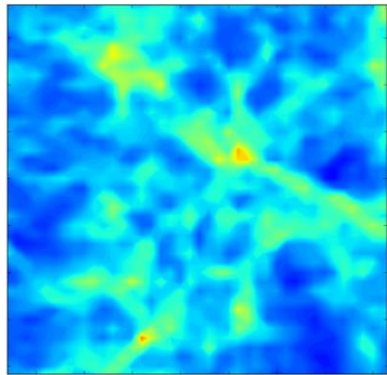
$$N_{i/H}(t) = 1 + \frac{1}{N_H} \int_0^t dt \int_V \alpha(T) n_e n_{\text{HII}} dV,$$

- **Clumping factor:**

$$N_{i/H}(t) = 1 + \int_0^t dt \alpha_A C_{\text{HII}}(t, V) \langle n_e \rangle_V \langle n_{\text{HII}} \rangle_V$$

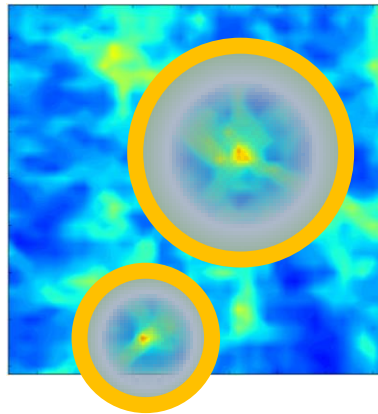

$$C_{\text{HII}}(t, V) \equiv \frac{\langle \alpha(T) n_e n_{\text{HII}} \rangle_V}{\alpha_A \langle n_e \rangle_V \langle n_{\text{HII}} \rangle_V}.$$

Filtering scale \rightarrow Clumping factor



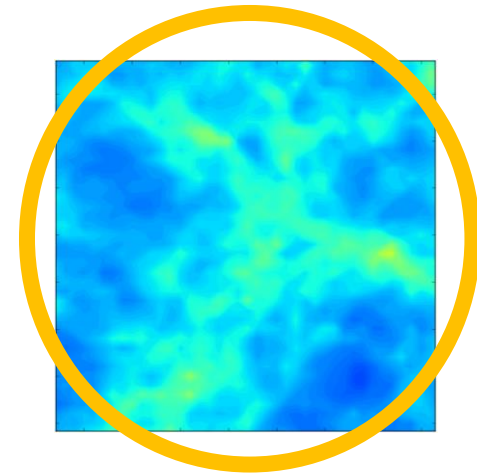

Gnedin & Hui (1998)

$T \uparrow$
 $x_{HII} \uparrow$



$$T \cong 2.5 \times 10^4 K$$

$1/k_F \uparrow$
 $C_b \downarrow$

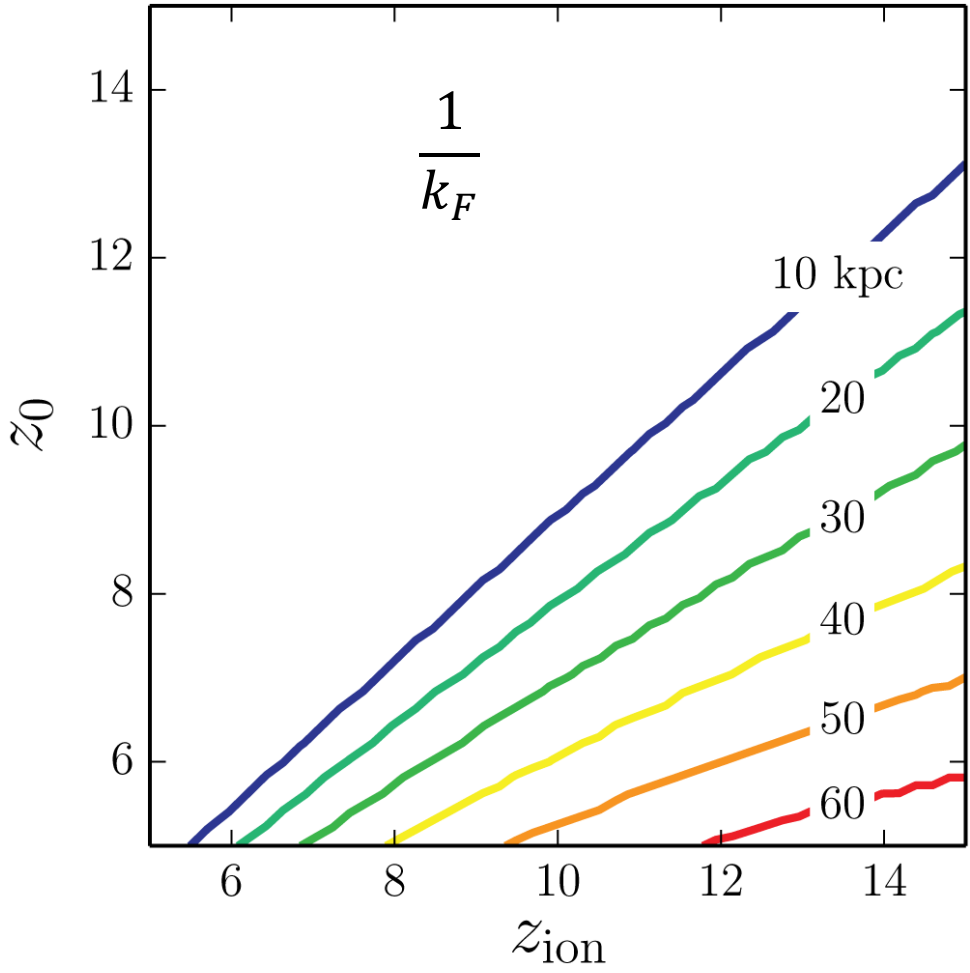


$$T \sim (1+z)^{-0.9}$$

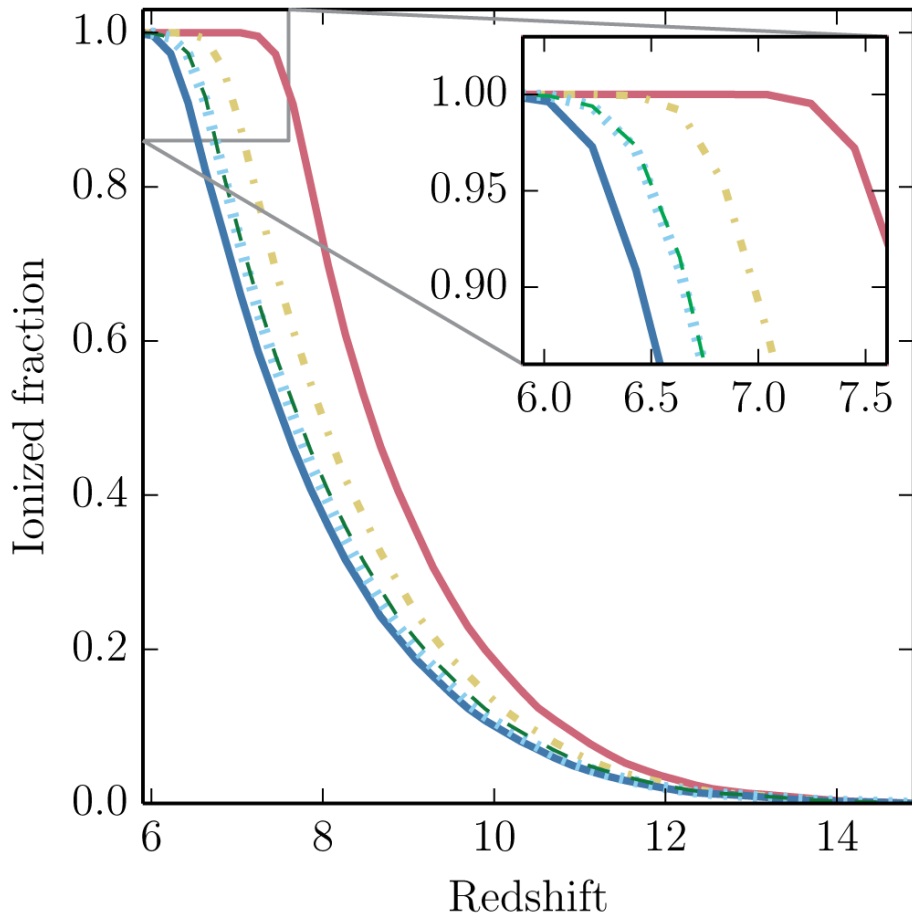
Filtering scale

(baryon overdensity) $\frac{\delta_b}{\delta_X} = 1 - \frac{k^2}{k_F^2}$
(DM overdensity)

If we consider a region which was ionized at redshift z_{ion} , then at redshift z_0 the filtering scale will be \rightarrow



Local clumping factor



$$C_{\text{HII}}^{\text{loc}}(\bar{\delta}, \sigma^2) = \frac{1}{\sqrt{2\pi(\sigma_\infty^2 - \sigma^2)}} \int_{-\infty}^{+\infty} d\delta e^{-\frac{(\delta - \bar{\delta})^2}{2(\sigma_\infty^2 - \sigma^2)}} \times (1 + \delta_{\text{HII}})^2,$$

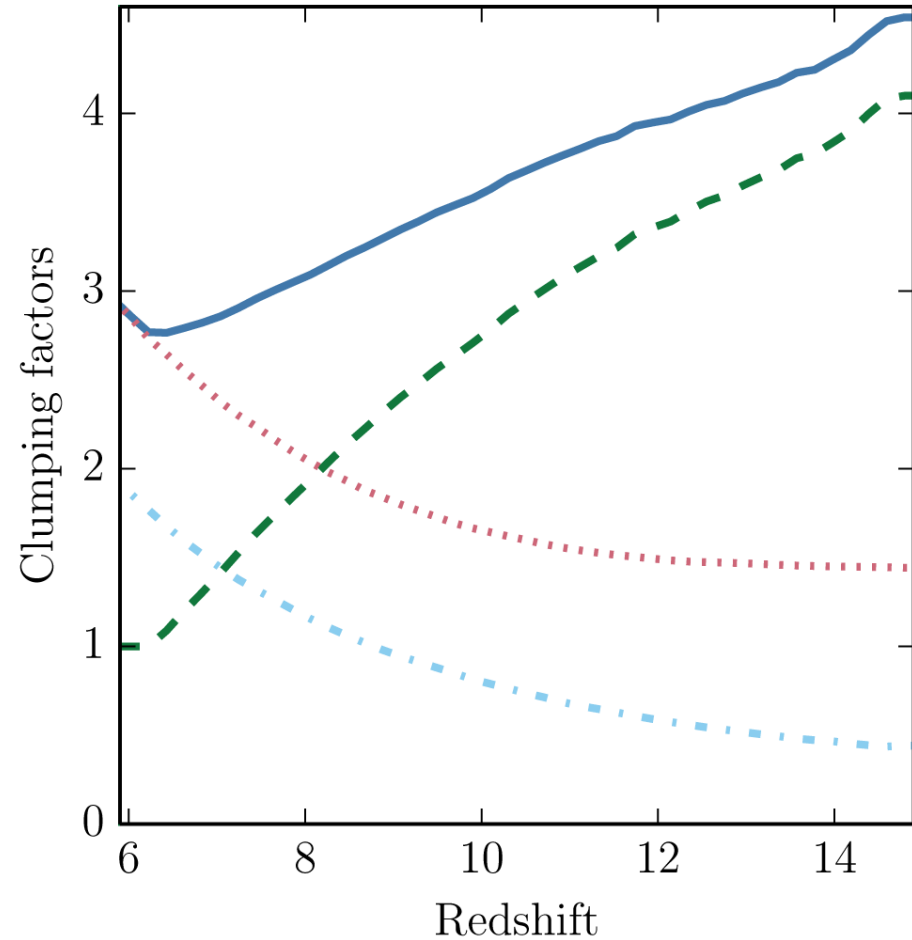
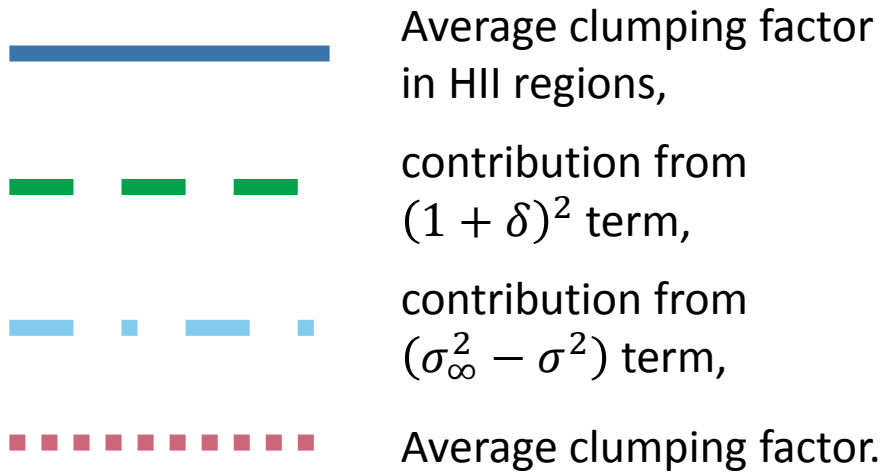
k_F goes into $\sigma_\infty(k_F)$

Clumping factor of HII regions:

$$C_{\text{HII}}^{\text{loc}}(\bar{\delta}, \sigma^2) = (1 + \bar{\delta})^2 + (\sigma_\infty^2 - \sigma^2).$$

- No recombinations
- - Uniform recombinations
- - Only $(1 + \delta)^2$ term
- - Only $(\sigma_\infty^2 - \sigma^2)$ term
- Full model

Global clumping factor



Conclusions

- Analytic models allow to study effects connected with morphology of reionization,
- Lyman Limit Systems slows down the very end of reionization and makes it more gradual,
- Clumping factor is not uniform and depends on the history of reionization,
- Our analytic results for clumping factor can be also applied for post-reionization epoch.

Thank you for your attention!